



Full Length Articles

Cryptocurrencies, currency competition, and the impossible trinity[☆]Pierpaolo Benigno^{a,*}, Linda M. Schilling^b, Harald Uhlig^c^a University of Bern, EIEF, CEPR, Switzerland^b Olin Business School Washington University in St Louis, CEPR, USA^c University of Chicago, NBER, CEPR, Chicago, USA

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ABSTRACT

We analyze a two-country economy with complete markets, featuring two national currencies as well as a global (crypto)currency. If the global currency is used in both countries, the national nominal interest rates must be equal and the exchange rate between the national currencies is a risk-adjusted martingale. Deviation from interest rate equality implies the risk of approaching the zero lower bound or the abandonment of the national currency. We call this result *Crypto-Enforced Monetary Policy Synchronization (CEMPS)*. If the global currency is backed by interest-bearing assets, additional and tight restrictions on monetary policy arise. Thus, the classic Impossible Trinity becomes even less reconcilable.

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1. Motivation

Globally usable cryptocurrencies are on the rise. 10 years after the introduction of Bitcoin, a Facebook-led consortium had sought to launch Diem, designed to appeal to the more than 2 billion world-wide Facebook users. Other companies are not far behind. While the Diem project itself has run into headwinds and may be scrapped altogether, it is not implausible that a privately issued and globally usable digital currency with widespread adoption will arise within the next two decades. Already, El Salvador has adopted Bitcoin as legal tender. Alternatively, one of the emerging central bank digital currencies may become a global means of payments in retail markets. Other means of payment have reached worldwide usage before, but the ease of

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use and the scope of these new digital currencies are about to create global currencies of an altogether different quality. How will they alter the financial landscape? How will this affect exchange rates and monetary policies of traditional currencies?

Global currencies are not a new phenomenon. The Spanish Dollar in the 17th and 18th centuries, gold during the gold standard period, the Pound Sterling prior to 1944, and the U.S. Dollar since then served as an internationally accepted unit of account. In dollarized countries, prices and contracts might be expressed in dollar, while the local currency often still serves as the main medium of exchange, with the occasional country, where expensive goods or even houses were indeed bought with suitcases of 100 dollar bills. The new cryptocurrencies, however, fully seek to become an internationally accepted means of payment, thus directly competing with national currencies for transaction purposes, even as prices are still expressed in, say, Dollars and Euros. We argue that this feature, together with the consequences for national monetary policies, is a qualitatively new phenomenon, see [Section 8](#).

We thus analyze a general and minimalistic framework of a two-country economy featuring a home, a foreign and a global (crypto)currency. Our focus is on the function of money as medium of exchange: currencies provide liquidity services. Interest-bearing bonds compete against money as a store of value. In [Section 7](#), we show that our framework nests a number of standard approaches in the monetary economics literature. Our approach thus encompasses a wide range of monetary approaches and strips them down to their key common component for the analysis at hand.

For the benchmark case that markets are complete, that liquidity services on currency are rendered immediately and that the global currency is used in both countries, we show that nominal interest rates must be equal ([Proposition 4.1](#)). We call this phenomenon a *crypto-enforced monetary policy synchronization (CEMPS)*. The escape options for central banks are unpleasant. Lowering the interest rate in order to deter the global currency from circulation at home risks being trapped at the zero lower bound. When increasing interest rates relative to the foreign interest rate, we show that the central bank risks the abandonment of its own national currency as a medium of exchange. If the global currency is backed by interest-bearing assets, additional and tight restrictions on monetary policy arise, see [Section 5](#). In particular, the central bank may be forced to the zero lower bound when the global currency consortium seeks to keep its currency in use per selecting appropriately low and competitive fees.

Our implications can be understood as a strengthened version of the Mundell-Fleming Trilemma ([Fleming, 1962](#); [Mundell, 1960, 1963](#)), or the *Impossible Trinity*. According to this cornerstone result in international economics, it is impossible to ensure a fixed exchange rate, free capital flows and an independent monetary policy all at the same time. In our framework, we allow for a flexible exchange rate and assume free capital flows: nevertheless, to defend the usage of their own national currency, presumably independent central banks have to coordinate their monetary policies. More broadly, our results are reminiscent of ([Rey, 2015](#)), where the Trilemma is transformed into a “Dilemma” or an “irreconcilable” duo. While the global financial cycle is the culprit in her analysis, on ours, it is the worldwide diffusion of a global currency. Furthermore, we contribute to the debate on how currency competition through globalization influences the central bank’s capacity to impact the economy, see [Romer \(2007\)](#).

1.1. Literature

Our paper contributes to three literature strands in particular. The first is the literature on the international role of currencies and the interdependence of monetary policies. The second is the literature on currency competition and the emerging literature on cryptocurrencies. Finally, we contribute to the monetary economics literature examining the role of money as a medium of exchange.

As for the first, the literature on international currencies and the interdependence of monetary policy, our paper is related to the classic contributions by [Mundell \(1960\)](#), [Fleming \(1962\)](#) and [Mundell \(1963\)](#), and the vast literature following it (see [Boughton \(2003\)](#), [Obstfeld et al. \(2003\)](#) for reviews and [Obstfeld and Rogoff \(1996\)](#) for a textbook treatment). Our result can be read as a sharp contrast to [Obstfeld and Rogoff \(2002\)](#), who argue that in an economy with integrated international financial markets, monetary policymakers have the ability to control their monetary instruments to achieve their target. Instead, our work shows that, under the same assumptions, having a global currency can constrain central banks in pursuing their objectives by limiting the impact of their monetary policy instruments. [Krugman, 1980](#), [Goldberg and Tille \(2008\)](#), [Rey \(2001\)](#), [Eichengreen et al. \(2017\)](#), [Amiti et al. \(2018\)](#), [Gopinath and Stein \(2018\)](#), [Maggiore et al. \(2019\)](#), [Gourinchas et al. \(2019\)](#), [Ilzetzki et al. \(2020\)](#), [Gopinath et al. \(2020\)](#) and [Bahaj and Reis \(2020\)](#) study the role of vehicle currencies, international currencies, global currencies and dominant currencies, emphasizing the unit of account function as well as the liquidity role played by securities denominated in these currencies. [Gopinath and Stein \(2018\)](#) justify the dominance of a currency on the basis of a higher share of trade settled in that currency. By contrast, we emphasize the medium of exchange function of money and the direct competition between the national and global currencies in that regard. Financial considerations are, instead, the reason that justifies, in our context, the dominance of a currency through the comparison of return differentials and other asset-pricing relationships. Another contribution of our work with respect to the above-mentioned literature is the analysis of the restrictions imposed by a global currency on international financial markets, relating them to the monetary policy followed by the single countries. Along these lines, [Ilzetzki et al. \(2020\)](#) argue that the limited role of the euro in international financial markets can be explained by the policy of the European Central Bank. [Benigno \(2019\)](#) focuses on a one-country model and shows that under competition to cryptocurrencies, the central bank can face some restrictions on interest rates and inflation if the government currency has to retain a role as a medium of exchange. We differ from his analysis by analyzing the consequences of cryptocurrency competition for the international monetary system by building on a general stochastic framework.

Our paper is closely related to the literature on currency competition, currency substitution and dollarization, Classic contributions are by [Girton and Roper. \(1981\)](#), who consider the impact of currency substitution on exchange rates, [Giovannini and](#)

Turtelboom. (1992), who examine various consequences of currency substitution, Matsuyama et al. (1993), who consider currency substitution in a two-country, two-currency model of random matching, the exchange rate indeterminacy result due to Kareken and Wallace (1981), and its stochastic version by Manuelli and Peck (1990). Uribe (1997) and Valev (2010) argue that currency substitution shows hysteresis and persistence due to network externalities. Schmitt-Grohé and Uribe (2000) examine currency substitution and their costs. Some of these insights have found a modern echo in the emerging literature on cryptocurrencies. Berentsen (1998) is an early example. Garratt and Wallace (2018) provide an extension of Kareken and Wallace (1981) to cryptocurrencies. Schilling and Uhlig (2019a) focus on implications of competition between a cryptocurrency and traditional fiat money, while Schilling and Uhlig (2019b) analyze the implications of goods-specific transaction costs. Fernández-Villaverde and Sanches (2019) and Chiu and Koepl (2019) analyze currency competition and monetary policy in a Lagos-Wright model. Our framework is considerably more general than all these contributions, allowing for interest-bearing bonds and nesting a number of classic monetary models. Our paper is close in spirit to Chahrour and Valchev (2019), who likewise emphasize the importance of an international medium of exchange. Brunnermeier and Niepelt (2019) pursue the implications of the equivalence between private and public money, in units of the same currency, while our emphasis is on the international context, on different currencies and, thus, has a different focus. Alesina and Barro (2001), Amidi et al. (2018), Maggiori et al. (2019), Gopinath et al. (2020), Bocola and Lorenzoni (2020), Christiano et al. (2021) and Uhlig and Xie (2021) concern the “unit of account” function of money, i.e. the pricing currency for firms and financial contracts, which is outside of the focus here. Edwards and I.Magendzo (2003) and recently Ju (2020) have examined the impact of currency substitution on economic performance.

Finally, we contribute to the monetary economics literature examining the role of money as medium of exchange. There are a variety of benchmark approaches that discuss a role of money, see, e.g., Walsh (2010) for an excellent textbook treatment. We take up several of these approaches in Section 7. Concerning the role of money as medium of exchange, the New Monetarist framework developed by Lagos and Wright (2005) has become the benchmark and has spawned a considerable literature. Lagos et al. (2017) provide an excellent survey and assessment. Among recent contributions, Fernández-Villaverde and Sanches (2019) and Chiu and Koepl (2019) employ the Lagos-Wright framework to analyze currency competition and cryptocurrencies. For our general and minimalistic framework, we abstract from the details of how money is used as a medium of exchange. All that we require is money offering “liquidity services”. In Section 7, we show that many benchmark approaches in the monetary economics literature, amongst others the Lagos-Wright approach, feature such liquidity services. Thus, the results derived in our abstract and minimalistic structure here apply to a large variety of classic settings.

There, moreover, exists a growing literature that analyze the functionality, feasibility and microincentives of individual cryptocurrencies and blockchain. Biais et al. (2019a, 2019b) analyze equilibria in proof-of-work protocols such as Bitcoin, Chiu and Koepl (2019) study Bitcoin's suitability as a payment system, Sockin and Xiong (2020) consider strategic complementarities in cryptocurrency investment when currency gives access to platform services, Ebrahimi et al. (2019) consider robust consensus protocols for blockchain-based distributed ledgers, Huberman et al. (2017) analyze revenue generation in the Bitcoin system, Leshno and Strack (2020) characterize Bitcoin as the unique reward scheme that satisfies anonymity, while neither giving incentive for consolidation nor for assuming fake identities, Prat and Walter (2021) use the Bitcoin-Dollar exchange rate for predicting the computing power of the Bitcoin network. William Cong and He. (2019) analyze implications of decentralized consensus via distributed ledger technology on competition. Garratt et al. (2019) analyze the role of cryptocurrency specific mining equipment for avoiding double spending attacks. This paper abstracts from microincentives and the possibility of attacks, and instead assumes full functionality and reliability of all currencies in this paper.

2. A simple framework

This section uses a simplified and non-stochastic framework in order to provide some intuition and to preview the main results of the general framework.

There are two countries, home and foreign, and three currencies: currency h and f in their respective countries and a global (crypto) currency g . While currency h can be used for transactions only in country h and the currency f only in country f , the global currency can be used in both countries. Money, either in a physical or digital form, provides non-pecuniary benefits, which we call liquidity services and yield liquidity premia. Let us assume that, when they are both used, the two currencies are perfect substitutes in providing liquidity services.

Let S_t be the exchange rate between currency h and f in date t , i.e. the amount of currency h needed to buy one unit of currency f . Let Q_t denote the amount of currency h needed to buy one unit of the global (crypto) currency. Likewise, let Q_t^* denote the amount of currency f needed to buy one unit of the global (crypto) currency. Therefore,

$$Q_t = S_t Q_t^* \quad (1)$$

At a generic time t , a resident in country h can acquire M_t units in currency h and G_t units in the global currency at the exchange rate Q_t in terms of home currency, implying an overall expenditure or total money holding

$$M_t^{\text{tot}} = M_t + Q_t G_t, \quad (2)$$

expressed in units of the domestic currency. For the foreign country f , we likewise obtain

$$M_t^{\text{tot}} = M_t^* + Q_t^* G_t^*, \quad (3)$$

where M_t^* are units in currency f and G_t^* are units in the global currency held abroad, with the exchange rate Q_t^* in terms of foreign currency. Note that we are assuming perfect substitutability: the extension to imperfect substitutability is explored in [Appendix 6.1](#). The total stock of global currency is the sum $G_t + G_t^*$, and it can be used in either country. The investor in country h receives non-pecuniary liquidity service benefits from the overall money expenditure M_t^{tot} deflated by the price of some generic consumption good (either tradeable or non-tradeable) for which money is exchanged. At time $t + 1$, the two monies deliver an overall payoff $M_t + Q_{t+1}G_t$, in units of the domestic currency. Since liquidity services provided by each currency are substitutes, the amount of services received is independent of the portfolio choice. Only if the returns on money are equal then agents are willing to hold both currencies in their portfolio. This is equivalent to saying that the exchange rate Q should be constant, $Q_{t+1} = Q_t$. Otherwise, one currency would dominate the other as a means of payment. This result is nothing more than a restatement of [Kareken and Wallace \(1981\)](#), additionally allowing the monies to provide liquidity services. The analysis can equivalently be applied to country f to obtain that the exchange rate Q^* should also be constant.

Our first result in the paper follows directly from the above analysis: when a global currency is used in both local markets, the exchange rate, S , between currency h and f has to be constant too, although h and f do not compete directly since h and f are not simultaneously accepted in the same local market. The monies h and f , however, compete indirectly through the global currency g which has worldwide acceptance, thereby creating a link between the two local currencies. This indirect competition then enforces equality of returns on h and f . To see this result, apply the constancy of Q and Q^* into (1).

Our second result states that simultaneous trade in global and local currencies requires the synchronization of monetary policies across countries, i.e., the nominal interest rates are equalized across countries. To see this result, we allow investors in each country to trade also in two nominal bonds denominated in currency h and f , respectively. In a non-stochastic economy, with frictionless capital markets, uncovered interest rate parity holds

$$\frac{1 + i_t}{1 + i_t^*} = \frac{S_{t+1}}{S_t} \quad (4)$$

in which i_t and i_t^* denote, respectively, the nominal interest rate in country h and f from period t to $t + 1$ on one-period bonds denominated in the respective currencies. Since the exchange rate S is constant, interest rates should be equal. [Fig. 1](#) summarizes the key relationship between interest rates and exchange rates.

As the next section will show, the result of equal nominal interest rates extends unchanged to a stochastic economy in the case where liquidity services of money are delivered at the same time money is held in the portfolio. The result of constant exchange rates generalizes to a stochastic economy with the qualification that the exchange rate between currency h and f follows instead a martingale when adjusting for risk, i.e. in the risk-neutral probability measure. In the stochastic setting, we will further show the equalization of the liquidity premia of money across countries.¹

Before turning to the more general framework, we discuss here which type of global currency is captured by our analysis. The emphasis is on cryptocurrencies, which are unlinked from any sovereign entity and could be worldwide adopted as medium of exchange rate. Any other currency, even sovereign one, could fit our framework if adopted in many countries. The global currency of our model can be in the form of digital or physical cash. As such, if adopted, it should provide similar liquidity services to the local currencies when competing in their markets. In particular, we think that perfect substitution captures in a better way the challenges of a digital, rather than a physical, global currency since, for its digital nature, it can be carried easily across borders and exchanged, to equally compete with local currencies, in all goods markets. We discuss, however, in [Section 6.1](#) how results change with imperfect substitutability and in [Section 8](#) we further discuss the comparison with other means of payments, as gold or dollars. Finally, it can be a purely fiat currency and not necessarily a stable or backed currency. However, in [Section 5](#), we also discuss the implications of competition coming from an asset-backed global currency.

3. A general framework

Our general stochastic multi-period framework is minimalistic on purpose, relying only on asset-pricing considerations to derive our key results. Our structure is broad enough to encompass a large variety of models and approaches of the monetary economics literature, see [Section 7](#). There are two countries h and f , each with their own home currency and a safe one-period nominal bond. There is also a global currency g . Agents in both countries can trade both bonds and can hold the global currency. The agent in country h can, in addition, hold currency h but not currency f . Vice versa, the agent in country f can hold currency f but not currency h . An important feature of our model is that whether a currency is used or not is an endogenous choice, depending on the monetary policy of the issuer and on the exchange rate between currencies.

The key assumption for obtaining our result is that markets are complete,² arbitrage-free and frictionless. As a consequence, a stochastic discount factor exists and is unique. Let $\mathcal{M}_{t+1}$ denote the nominal stochastic discount factor in units of currency h for

¹ Liquidity premia are in general monotone in the opportunity cost of holding money, i.e. the interest rate. Equal interest rates directly imply equal liquidity premia.

² The assumption can be weakened slightly, but would make the presentation more opaque.

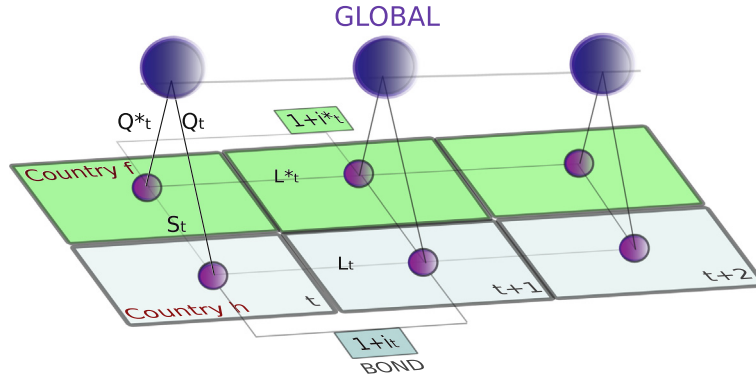


Fig. 1. International trade and money flow in time.

the agent in country h , and likewise let $\mathcal{M}_{t+1}^*$ denote the nominal stochastic discount factor in units of currency f for the agent in country f . An implication of complete markets is that the nominal discount factors in units of the two local currencies are connected through their exchange rate since they are equalized once expressed in the same unit of account.³

Assumption 3.1. Complete markets

$$\mathcal{M}_{t+1} = \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}}. \quad (5)$$

Consider a (non-monetary) asset offering a (possibly random) nominal return R_{t+1} in currency h . Since returns have a price of one (Cochrane, 2009), the indifference condition of an intertemporal utility maximizing agent implies the following standard asset pricing equation to value a random return R_{t+1} ,

$$1 = E_t[\mathcal{M}_{t+1} R_{t+1}]. \quad (6)$$

where $\mathcal{M}_{t+1}$ denotes the nominal stochastic discount factor. Thus, since a nominal one-period bond in country h pays a return $R_{t+1} = 1 + i_t$,

$$\frac{1}{1 + i_t} = E_t[\mathcal{M}_{t+1}] \quad (7)$$

and likewise for the bond in country f

$$\frac{1}{1 + i_t^*} = E_t[\mathcal{M}_{t+1}^*]. \quad (8)$$

Bonds and currencies are used for the intertemporal transfer of resources. Money needs to offer some liquidity services beyond the intertemporal transfer to be able to compete with interest-bearing bonds for investors. We shall therefore assume that, when used, currency h , as well as the global currency, pays a non-monetary liquidity service L_t to agents in country h per unit of currency, in addition to the intertemporal payoff. Note that, in our framework, a currency provides liquidity only when it is used, and that its usage is an endogenous choice. Likewise, we assume that currency f pays a liquidity premium L_t^* to agents in country f per unit of currency. For clarity and simplicity, we assume here that currency h and g in country h , as well as currency f and g in country f , are perfect substitutes. A detailed generalization and discussion of the case of imperfect substitutability is given in Section 6.1.

In a full model specification such as given in Section 7, these liquidity services are endogenously determined through optimal consumption choices of households under, for instance, cash-in advance constraints or money-in-the-utility function. In all of these models, money is held across periods from t to $t + 1$, and the particular model structure determines whether the services are rendered in period t (“immediately”) or in $t + 1$ (“with delay”). For the benchmark case here we assume the former, but return to the latter in Appendix. In contrast, we shall think of nominal interest rates on bonds as exogenously set policy instruments.

³ For the generality of this result see Obstfeld (2007).

Assumption 3.2. Liquidity immediacy

The purchase of currency h and g in country h at t yields an immediate liquidity premium L_t receivable in t . Analogously, the time t purchase of currency f and g in country f at t yields an immediate liquidity premium L_t^* receivable in t .

The date- t (post-liquidity) price of a unit of currency h , expressed in units of the same currency equals unity, by definition. Standard asset pricing considerations then deliver

$$1 \geq L_t + E_t[\mathcal{M}_{t+1}]. \quad (9)$$

Whenever (9) holds with equality, agents in country h are willing to accept currency h at its unitary price, since they are exactly compensated by the liquidity premium plus the discounted future value of the payoff, see terms on the right hand side of Eq. (9). In case of a strict inequality, the current price of currency h is too high compared to the expectations on future price developments such that agents are not willing to hold or purchase the currency. Note that we do not allow for short sale.

If a national currency is accepted, then liquidity services provided by this currency stand in a one-to-one relationship with the nominal interest rate paid on bonds, compare (9) to (7), because the nominal interest is the opportunity cost of holding money for transaction purposes. Likewise, for a unit of the global (or crypto) currency, trading at a price of Q_t in terms of units of currency h , we obtain

$$Q_t \geq L_t Q_t + E_t[\mathcal{M}_{t+1} Q_{t+1}], \quad (10)$$

where this equation holds with equality, if the global currency is used in country h , i.e. if agents are compensated for the price Q_t of a global currency exactly by the liquidity premium plus the discounted future value of the payoff, on the right hand side of Eq. (10). The price cannot be lower than the right hand side, since otherwise agents in country h would seek to acquire the currency and bid up its value. The price can be higher, however, if the global currency is not used in country h . We implicitly rule out short sales or, more precisely, rule out that short-sold currencies render negative liquidity premia. Combining (7) and (9), we obtain

$$\frac{i_t}{1 + i_t} \geq L_t, \quad (11)$$

which holds with equality when currency h is used and therefore describes a monotone relationship between the nominal interest rate and the liquidity services. For the foreign country, we likewise obtain

$$1 \geq L_t^* + E_t[\mathcal{M}_{t+1}^*] \quad (12)$$

$$Q_t^* \geq L_t^* Q_t^* + E_t[\mathcal{M}_{t+1}^* Q_{t+1}^*], \quad (13)$$

$$\frac{i_t^*}{1 + i_t^*} \geq L_t^*. \quad (14)$$

In the analysis that follows we stick to the following assumption.

Assumption 3.3. Non-negative liquidity premia

The liquidity premia are non-negative, i.e. $L_t \geq 0$ and $L_t^* \geq 0$.

This assumption, together with Eqs. (11) and (14), implies that $i_t \geq 0$ and $i_t^* \geq 0$, i.e., imply a zero lower bound for nominal interest rates. Moreover, we assume that at least one currency is used in each country while bonds cannot serve as medium of exchange.⁴

Assumption 3.4. Currency usage

In each country, at least one currency is used. That is, in country h , at least one out of inequalities (9) and (10) holds with equality. In country f , at least one out of inequalities (12) and (13) holds with equality.

Additionally, it is reasonable to impose that at least one out of (10) or (13) holds with equality, but we are not making use of that restriction. We make the assumption that the global currency has a positive value in the time period t under consideration.

⁴ We abstract from the issue of existence of non-monetary equilibria, which naturally arises in monetary models of fiat money.

Assumption 3.5. Global currency is valued

$$Q_t > 0 \quad \text{and} \quad Q_t^* > 0 \quad (15)$$

Given the triangular relationship among exchange rates, $Q_t = S_t Q_t^*$, it follows that $Q_t > 0$ if and only if $Q_t^* > 0$. Thus, the currency being valued in one country necessarily spills over to the other country.

Some additional terminology shall prove useful. For a generic random variable X_{t+1} , define the risk adjusted expectation $\bar{E}_t[X_{t+1}]$ in country h as

$$\bar{E}_t[X_{t+1}] \equiv \frac{E_t[\mathcal{M}_{t+1} X_{t+1}]}{E_t[\mathcal{M}_{t+1}]}, \quad (16)$$

and the risk adjusted expectation $\bar{E}_t^*[X_{t+1}]$ in country f as

$$\bar{E}_t^*[X_{t+1}] \equiv \frac{E_t[\mathcal{M}_{t+1}^* X_{t+1}]}{E_t[\mathcal{M}_{t+1}^*]}. \quad (17)$$

As a consequence of market completeness and bond pricing, (5), (7) and (8), we obtain uncovered interest parity (UIP), when using the risk-adjusted measure or risk neutral probability distribution,

$$\frac{\bar{E}_t[S_{t+1}]}{S_t} = \frac{1 + i_t}{1 + i_t^*} \quad (18)$$

$$\frac{\bar{E}_t^*[S_{t+1}^*]}{S_t^*} = \frac{1 + i_t^*}{1 + i_t} \quad (19)$$

where $S_t^* = 1/S_t$. Note that UIP holds irrespective of whether there is a global currency or not. UIP and the associated risk premia have received considerable attention in the literature, see e.g. Engel (2016). Here we obtain it as a consequence of free capital markets.

4. Main results**Proposition 4.1. Stochastic Economy under Liquidity Immediacy**

Assume liquidity immediacy, complete markets, and that the global currency is valued. If all currencies are used in both countries, i.e. if equations (9), (10), (12) and (13) hold with equality, then

1. the nominal interest rates are equalized $i_t = i_t^*$;
2. the liquidity premia are equal $L_t = L_t^*$;
3. the nominal exchange rate S_t between currency h and f follows a martingale, using risk adjusted expectations of country h ;
4. the nominal exchange rate $S_t^* = 1/S_t$ between currency f and h follows a martingale, using risk adjusted expectations of country f .

Proof. [Proposition 4.1] The competition between currency h and the global currency, i.e. (9) and (10) with equality, the complete-market assumption (5) and finally the competition between currency f and the global currency, i.e. (12) and (13) with equality, deliver

$$E_t[\mathcal{M}_{t+1}] = E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] = E_t\left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*}\right] = E_t[\mathcal{M}_{t+1}^*] \quad (20)$$

Eqs. (9) and (12) now imply $L_t = L_t^*$ and thus $i_t = i_t^*$, per Eqs. (11) and (14). The martingale properties of the exchange rate follow from Eqs. (18) and (19) together with $i_t = i_t^*$. $\square$

Proposition 4.1 says that, with complete markets, global usage of the global currency, and simultaneous usage of the local currency, monetary policies must be perfectly synchronized. But does Proposition 4.1 mean that the central banks in the two countries have no choice but to accept this fate of coordinated monetary policy? When central banks in Home and Foreign are independent, they can set their interest rates distinctly from one another. Proposition 4.1 can also be read the other way around.

If $i_t \neq i_t^*$, then at least one of the presumptions has to be violated: either the global currency is not used in at least one country or one of the national currencies is not in use or both. The central bank in country h may then contemplate pursuing a policy that makes sure that the global currency is not used in country h , i.e. that (10) remains an inequality.

Proposition 4.2. Escaping global currency adoption

Assume liquidity immediacy, complete markets, and that the global currency is valued. Assume that both local currencies are used in their corresponding countries, i.e. equations (9) and (12) hold with equality. Independently of whether the global currency is used or not in country f , if $i_t < i_t^*$, then

1. the global currency is not adopted in country h ;
2. the liquidity premia satisfy $L_t < L_t^*$;
3. the nominal exchange rate S_t between currency h and f follows a supermartingale, using risk adjusted expectations in country h ;
4. the nominal exchange rate $S_t^* = 1/S_t$ between currency f and h follows a submartingale, using risk adjusted expectations in country f .

The proof is in Appendix A.1. To understand the economics behind this result, it is important to acknowledge not only the competition between the currency h respectively f and the global currency but also the countrywide competition between the bond and currency and the role of the frictionless foreign exchange-rate market. The proof has three parts. First, since the nominal interest rate in country f is higher than the nominal interest rate in country h , liquidity services in country f are higher than in country h . Second, the competition between the national currencies and the global currency yields upper bounds on the risk-adjusted return of the global currency. The bound is sharper, if the nominal interest rate is higher, i.e. in country f , and it binds, if the global currency is adopted. Third, by frictionless foreign exchange-rate markets and the no arbitrage condition, the risk-adjusted return on the global currency has to be equal in countries h and f . As a consequence, the country with the weaker constraint on that return does not adopt the global currency.

The proposition shows that there is an escape hatch indeed, but only to one side. Starting from an equilibrium in which the global currency is used in both countries, by lowering the risk-free interest rate in currency h below that in currency f , the central bank in country h lowers the opportunity costs of holding the domestic currency and thus makes it more attractive than the global currency as a means of payment, crowding out the global currency in country h . Proposition B.1 in the appendix shows that an analogous deterrence-result holds in the case of imperfect substitutability of currencies, allowing distinct liquidity services of national and global currency.

This escape hatch is not particularly attractive, however. Nominal interest rates can only be lowered to zero. Furthermore, a rat race between the two central banks may eventually force both to stick to the zero lower bound forever or at low interest rates.⁵ Some may applaud this as the ultimate and global implementation of the Friedman rule, while others may fear deflationary spirals and macroeconomic damage. Either way, these are surely dramatic consequences of the circulation of a global currency.

The next Proposition analyzes the opposite scenario, in which the home central bank raises its rates above the foreign one. When the global currency is used in country f , this leads to the abandonment of the home currency as a medium of exchange: presumably an even less attractive option for the home central bank. Our stark result here might be thought of as a version of dollarization going hand-in-hand with high local currency inflation rates or hyperinflations: the latter can perhaps be thought of as a “slo-mo” version of abandoning the currency.

Proposition 4.3. Losing medium-of-exchange property

Assume liquidity immediacy, complete markets, and that the global currency is used in country f , i.e. equation (13) holding with equality. If the central bank in country h sets $i_t > i_t^*$, then currency h is abandoned in country h and the global currency takes over (currency substitution). Currency h would also be abandoned in country h if the central bank sets $i_t = i_t^*$ and only currency g is used in country f .

The proof is in Appendix A.2. We call the collection of the three results in Propositions 4.1, 4.2 and 4.3 *Crypto-Enforced Monetary Policy Synchronization (CEMPS)*. They demonstrate that introducing a global currency in a free international capital market constitutes a constraint on the Impossible Trinity. Under free capital flows and without a global currency, uncovered interest parity and the classic Impossible Trinity result provides the home central bank with a choice: it can give up on either a pegged exchange rate or monetary policy independence. Our result shows that introducing a global currency implies a further restriction, when it becomes a perfect substitute for the local currencies. Either the monetary policy of the central banks can no longer be independent or central banks risk the crowding out of their own currency. Additionally, the exchange rate is now a risk-adjusted martingale and not necessarily a peg, see also Manuelli and Peck (1990) and Schilling and Uhlig (2019a). The classical Impossible Trinity thus becomes even less reconcilable. With currency substitution, the countries' nominal interest rates are equalized independently of whether the economy is stochastic or deterministic.

⁵ In a one-country model Benigno (2019) shows that if the central bank keeps the inflation target below the growth rate of private currency, then it can maintain the monopoly power on the medium of exchange. However, cryptocurrencies' issuance is in general engineered with quite low, or zero, growth rates so that inflation targets set by central banks should be close to zero or below.

To conclude this analysis, it is important to emphasize that the results of this section have abstracted from the monetary policy followed by the issuer of the global currency. This can be characterized by fully developing the different monetary models – all nested in our general framework – that we present in Section 6. In this abstraction, it should be understood that when the global currency is perfect substitute of the local currency, in providing liquidity services, is because of the underlying monetary policy. On the other side, this section has been more explicit on the monetary policy of the local currencies showing that their stance determines their relative value with respect to other currencies and therefore whether they are going to be used as a medium of exchange. In the next section, when we treat the case of an asset-backed global currency, we will instead provide more details on how its issuer can control the value of its currency relative to the local one.

5. Special case: asset-backed global currencies

This section is motivated by the fairly recent proposal by a Facebook-led consortium to launch a new global currency called Diem. While the Diem project itself has undergone considerable changes since its inception as Libra and may be scrapped altogether, it is not implausible that a privately issued and globally usable digital currency of widespread use and backed by a basket of assets emerges in the near future. We therefore analyze the consequences of introducing a global currency backed by a basket of risk-free securities denominated in government currencies. In our framework, suppose that the issuing consortium backs the global currency by safe bonds denominated in currency h . Moreover, assume that the consortium is ready to buy and sell any amount of the global currency at a fixed price Q_t . When issuing the amount Δ_t of the global currency at some date t , the consortium invests the proceeds $\Delta_t Q_t$ in the safe bonds of country h . In period $t + 1$, the consortium receives the interest payments on the bonds. The consortium keeps a portion of the date $t + 1$ portfolio value as a per-period asset management fee, assumed to be $\phi_t \Delta_t Q_t$ for some $\phi_t \geq 0$ set in t . One may wish to think of these fees as profits paid to the shareholders of the consortium. The consortium then sets the new price Q_{t+1} , again trading any amount of the global currency at that price and investing their client's funds in home safe bonds. The return that accrues to the global currency between t and $t + 1$, i.e., the bond return after applying the management fee, can be redeemed at the global currency's price Q_{t+1} or is reinvested. In order to credibly promise the repurchase of the global currency for a price Q_{t+1} at $t + 1$ and assuming no profits beyond the asset management fee, assets and liabilities have to grow at the same rate,

$$Q_{t+1} = (1 + i_t - \phi_t) Q_t \quad (21)$$

Note that for $i_t \geq \phi_t$ the price of the global currency then increases over time $Q_{t+1} \geq Q_t$.

Proposition 5.1. Asset backed global currency

Assume that the global currency is valued.

1. If $\phi_t < i_t$, then currency h is crowded out and only the global currency is used in country h . Moreover, $L_t = \frac{\phi_t}{1+i_t}$.
2. If $\phi_t = i_t$, both currency h and the global currency coexist in country h .
3. If $\phi_t > i_t$, then only currency h is used in country h .

The proof is in Appendix A.3. From the results in Proposition 5.1, we can generate more striking implications if we assume the fee to apply in the form of a fixed portion of the interest payments, $\phi_t = \kappa i_t$ for some parameter $0 \leq \kappa \leq 1$. Then

1. If $\kappa < 1$, then $i_t \leq \phi_t$ only holds for $i_t = 0$. Moreover, $i_t = 0$ implies $\phi_t = 0$ and the global currency is used together with the local currency in country h .
2. If $\kappa = 1$ (or $\phi_t = i_t$), then the price Q_t for the global currency is fixed (Stablecoin) and both currencies are used.

A useful reading of the above results from a central-banking perspective is the following. For local currency h to remain in usage, the nominal interest rate has to undercut or match the management fee ϕ . The proposition therefore suggests that an interesting Bertrand-type game could unfold. The home central bank may seek to undercut the fee charged by the consortium, in order to drive the global currency out of usage at home. But without usage, the global currency consortium cannot earn any revenue from the fees: it would be better off by lowering its fees in response.⁶ In the limit, this dynamic could result in both parties ratcheting down the “price” for their currencies to their marginal costs of issuance. If these marginal costs are zero or near zero, an assumption often made in the literature, then one obtains a zero interest rate policy and a zero fee. Put differently, currency competition between currency h and the global currency leads to the establishment of the celebrated Friedman rule to keep interest rates at zero, thereby setting the private costs of holding the currencies equal to the social cost of its production. There is a large literature establishing conditions under which the Friedman rule is optimal, see Woodford (1990). More generally, if one

⁶ The consortium may not care if country h is small. It presumably would care, though, if the country was large and economically important or a large and important currency union.

currency has higher marginal production costs than the other, then the resulting zero profit condition for this higher-cost currency will dictate the resulting limit. From the consortium's perspective, the nominal interest rate on the backing asset provides an upper bound on the fee that can be charged while maintaining usage of the global currency.

These results are also reminiscent of the view in Hayek, 1976, that unfettered competition can align private incentives with social objectives. To extract rents from liquidity services, currency issuers have to supply better money than others by keeping its value high and, therefore, inflation low. But then competition kicks in, driving rents to zero and eliminating liquidity premia so that the better money also serves the social benefits. Benigno (2019) presents a model of currency competition obtaining the same result under free entry. Our insights are related to the analysis in Marimon et al. (2003), who likewise emphasize that cheap inside monies place tight upper bounds on inflation rates there or nominal interest rates here.

6. Robustness

In this section, we study the robustness of our results by relaxing two important assumptions we made: (1) the perfect substitutability between the local and the global currency; (2) complete international financial markets.

6.1. Imperfect substitutability of currencies

The main model assumes that, within a country, the liquidity services on the national and the global currency are identical. We generalize this feature in this section to allow for imperfect substitutability.⁷ This requires a bit more structure and notation. As in Section 2, let M_t^{tot} denote the total money holdings in country h at time t , expressed in units of the domestic currency. In Section 2 and implicitly in the general framework of Section 3, we have assumed that total money in a country is the sum of the nominal amount of the domestic currency as well as the nominal value of the global currency used in the country, see Eqs. (2) and (3). More generally, assume now that

$$M_t^{\text{tot}} = a(M_t, Q_t G_t) \quad (22)$$

$$M_t^{*,\text{tot}} = a(M_t^*, Q_t^* G_t^*) \quad (23)$$

for some concave, non-negative, twice continuously differentiable constant-returns-to-scale function $a(\cdot, \cdot)$ with strictly positive partial derivatives and with $0 = a(0, 0)$, aggregating the two money components to the total money stock. For the linear specification $a(m, g) = m + g$, we obtain (2) and (3). A nonlinear $a(\cdot, \cdot)$ captures the idea that the national currency may be relatively more useful for certain transactions, while the global currency is more useful for others. Define the real value of the money stocks as

$$m_t^{\text{tot}} = \frac{M_t^{\text{tot}}}{P_t}, \quad m_t = \frac{M_t}{P_t}, \quad g_t = \frac{Q_t G_t}{P_t}, \quad m_t^{*,\text{tot}} = \frac{M_t^{*,\text{tot}}}{P_t^*}, \quad m_t^* = \frac{M_t^*}{P_t^*}, \quad g_t^* = \frac{Q_t^* G_t^*}{P_t^*}.$$

Due to constant returns to scale, Eqs. (22) and (23) can then alternatively be written as

$$m_t^{\text{tot}} = a(m_t, g_t) \quad (24)$$

$$m_t^{*,\text{tot}} = a(m_t^*, g_t^*) \quad (25)$$

Assume that the aggregate stock of total real money m^{tot} provides a benefit $v(m^{\text{tot}})$ and assume that λ_t is the Lagrange multiplier on the nominal date- t budget constraint, where either type of money as well as the bonds are acquired. These assumptions arise directly in a money-in-the-utility formulation as in Section 7.2, when allowing for the same imperfect substitutability as here. They likewise arise in a Lagos-Wright model as in Section 7.1 or a cash-in-advance model as in Section 7.3 with some work. Let $a_{1,t}$ and $a_{2,t}$ denote the partial derivatives $a_1(m_t, g_t)$ and $a_2(m_t, g_t)$ of a with respect to the first respectively second argument and evaluated at m_t and g_t . Likewise, let $a_{1,t}^*$ and $a_{2,t}^*$ denote the partial derivatives $a_1(m_t^*, g_t^*)$ and $a_2(m_t^*, g_t^*)$ of a with respect to the first respectively second argument and evaluated at m_t^* and g_t^* . The first-order conditions with respect to $M_t \geq 0$ and $G_t \geq 0$ are

$$\lambda_t \geq v'(m_t^{\text{tot}}) \frac{a_{1,t}}{P_t} + \beta E_t[\lambda_{t+1}] \quad (26)$$

⁷ See also the transaction-costs-based approach in Schilling and Uhlig (2019b) as well as the closely related analysis in the undergraduate honors thesis by Kei Irizawa, University of Chicago 2020.

$$Q_t \lambda_t \geq v'(m_t^{\text{tot}}) \frac{Q_t a_{2,t}}{P_t} + \beta E_t[\lambda_{t+1} Q_{t+1}] \quad (27)$$

Note that these partial derivatives are identical to one in the linear case (2) and (3). With $\mathcal{M}_{t+1} = \beta \lambda_{t+1} / \lambda_t$ and with liquidity services L_t of total money defined⁸ as

$$L_t = \frac{v'(m_t^{\text{tot}})}{P_t \lambda_t} \quad (28)$$

Eqs. (26) and (27) take the more familiar form

$$1 \geq L_t a_{1,t} + E_t[\mathcal{M}_{t+1}] \quad (29)$$

$$1 \geq L_t a_{2,t} + E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] \quad (30)$$

with the partial difference terms $a_{1,t}$ and $a_{2,t}$ generalizing the benchmark perfect-substitutability case. For the foreign country, we have likewise

$$1 \geq L_t^* a_{1,t}^* + E_t[\mathcal{M}_{t+1}^*] \quad (31)$$

$$1 \geq L_t^* a_{2,t}^* + E_t\left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*}\right] \quad (32)$$

Define $\alpha_t = \alpha(m_t, g_t, m_t^*, g_t^*)$ as

$$\alpha_t = \frac{a_{1,t}}{a_{2,t}} / \frac{a_{1,t}^*}{a_{2,t}^*} = \frac{a_1(m_t, g_t)}{a_2(m_t, g_t)} / \frac{a_1(m_t^*, g_t^*)}{a_2(m_t^*, g_t^*)} \quad (33)$$

in⁹ $[0, \infty]$ as the relative marginal rates of currency substitution. Note that $\alpha_t \equiv 1$ in the linear benchmark case (2) and (3). We now obtain a generalization of Proposition 4.1.

Proposition 6.1. Imperfect currency substitutability

Given the additional assumptions here, complete markets, $Q_t > 0$, $Q_t^* > 0$ and that equations (29), (30), (31), (32) hold with equality,

1. the nominal interest rates satisfy

$$\frac{i_t}{1+i_t} = \alpha_t \frac{i_t^*}{1+i_t^*} \quad (34)$$

2. the liquidity premia for the global currency are equal: $L_t a_{2,t} = L_t^* a_{2,t}^*$.

The proof is in Appendix A.4. Note that α_t is endogenous and may depend on the choice of the nominal interest rates i_t and i_t^* by the central banks. Thus, (34) is merely an equilibrium relationship and not a constraint on monetary policy. However, Eq. (34) implies bounds on the interest rates. Suppose that for some $\bar{m} > 0$ and $\bar{g} > 0$, we have $m_t \leq \bar{m}$ and $g_t \leq \bar{g}$ in all equilibria. As an example, $\bar{m} = \bar{g}$ would be the lowest upper bound for real transactions in a cash-in-advance economy. Proceed likewise for the foreign country. Define

$$\underline{\alpha} = \alpha(\bar{m}, 0, 0, \bar{g}^*) \text{ and } \bar{\alpha} = \alpha(0, \bar{g}, \bar{m}^*, 0). \quad (35)$$

In the benchmark linear case, $\alpha = \bar{\alpha} = 1$.

⁸ This is similar to (66).

⁹ As is conventional, we tacitly assume that division by ∞ results in 0 and vice versa.

Lemma 6.1. Bounds for α

$$\alpha \leq \alpha_t \leq \bar{\alpha} \quad (36)$$

The proof is in [Appendix A.5](#). Thus, under the assumptions of [Proposition 6.1](#),

$$\alpha \frac{i_t^*}{1+i_t^*} \leq \frac{i_t}{1+i_t} \leq \bar{\alpha} \frac{i_t^*}{1+i_t^*} \quad (37)$$

or

$$\left(\frac{1+i_t^*}{\alpha i_t^*} - 1 \right)^{-1} \leq i_t \leq \begin{cases} \left(\frac{1+i_t^*}{\bar{\alpha} i_t^*} - 1 \right)^{-1}, & \text{if } \bar{\alpha} \frac{i_t^*}{1+i_t^*} < 1 \\ \infty, & \text{if } \bar{\alpha} \frac{i_t^*}{1+i_t^*} \geq 1 \end{cases} \quad (38)$$

One can read either equation as a constraint on the domestic monetary policy interest rate i_t , given the foreign interest rate i_t^* as well as the two bounds α and $\bar{\alpha}$: outside these bounds, the assumptions of [Proposition 6.1](#) must be violated. To further clarify this, we generalize [Proposition 4.3](#).

Proposition 6.2. Losing medium-of-exchange property with imperfect currency substitutability

Given the additional assumptions here and complete markets, $Q_t > 0$, $Q_t^* > 0$, if the global currency g and local currency f are used in country f^{10} and if the central bank in country h sets

$$\frac{i_t}{1+i_t} > \alpha(0, g_t, m_t^*, g_t^*) \frac{i_t^*}{1+i_t^*}, \quad (39)$$

then currency h is abandoned in country h and the global currency takes over (currency substitution).

The proof is in [Appendix A.6](#). While Eq. (39) is generally tighter than the right hand side of (37), it requires knowledge of the equilibrium variables g_t , m_t^* and g_t^* . For the benchmark linear specification $a(m, g) = m + g$, we have $\alpha(0, g_t, m_t^*, g_t^*) = 1$ and again obtain the result in [Proposition 4.3](#) that it is sufficient to raise the interest rate in country h just above that of the foreign country to lose medium-of-exchange properties for currency h . Generally, results depend on the functional form of the money aggregator. One interesting implication, though, is that currency h is always abandoned whenever $i_t > 0$ and $i_t^* = 0$, provided $\alpha(0, g_t, m_t^*, g_t^*)$ is finite. The latter requirement, however, cannot be taken for granted as the second part of the following corollary shows.

Corollary 6.1. Functional forms

Under the assumptions of [Proposition 6.2](#)

1. Suppose that the aggregator functions take the form

$$a(m, g) = m + g + \psi \frac{mg}{m+g} \quad (40)$$

for some $\psi \geq 0$. Then equations (37, 38) and [Proposition 6.2](#) hold with

$$\underline{\alpha} = \frac{1}{(1+\psi)^2} \text{ and } \bar{\alpha} = (1+\psi)^2 \quad (41)$$

for equation (36) as well as

$$1 \leq \alpha(0, g_t, m_t^*, g_t^*) = (1+\psi) \frac{1+\psi(s_t^*)^2}{1+\psi(1-s_t^*)^2} \leq \bar{\alpha} \quad (42)$$

for equation (39), where $s_t^* \equiv m_t^*/(g_t^* + m_t^*)$ is the share of the foreign currency in the total value of currencies used abroad.

¹⁰ i.e. Eqs. (31) and (32) hold with equality.

2. Suppose that the aggregator function is the CES function

$$a(m, g) = \left(m^{\frac{\eta-1}{\eta}} + \gamma g^{\frac{\eta-1}{\eta}} \right)^{\frac{\eta}{\eta-1}} \quad (43)$$

where $\eta > 0$ is the elasticity of substitution and where $\gamma > 0$ is a share parameter. Then

$$\alpha_t = \left(\frac{g_t}{m_t} / \frac{g_t^*}{m_t^*} \right)^{1/\eta}, \quad (44)$$

Eqs. (37, 38) and Proposition 6.2 hold with

$$\underline{\alpha} = 0 \text{ and } \alpha(0, g_t, m_t^*, g_t^*) = \bar{\alpha} = \infty \quad (45)$$

for equations (36) and (39), with the exception that $\alpha(0, g_t, 0, g_t^*)$ is undefined. Holding m_t^*, g^* and $i_t^* > 0$ fixed, equation (34) implies

$$\frac{g_t}{m_t} \rightarrow \frac{g_t^*}{m_t^*} \left(\frac{1 + i_t^*}{i_t^*} \right)^{\eta} \text{ for } i_t \rightarrow \infty, \quad (46)$$

i.e. the value of the home currency in use does not vanish relative to the value of the global currency in use at home, even as the home nominal interest rate diverges. Conversely $g_t/m_t \rightarrow 0$ as $i_t \rightarrow 0$, i.e. the role of the global currency vanishes as the home interest rate approaches the zero lower bound.

Proof. Calculate. $\square$

The first part of the corollary provides a money aggregator in Eq. (40) such that the national currency is not essential. Although currencies are imperfect substitutes, a sufficiently high nominal interest rate i_t in country h will necessarily lead to abandoning the home currency as a medium of exchange, provided the foreign interest rate i_t^* or the foreign currency share s_t^* is sufficiently low. Domestic monetary policy may wish avoid that. This is then a version of the crypto-enforced monetary policy synchronization, though softened by the wriggle room up to the interval $\alpha_t \in [(1 + \psi)^{-2}, (1 + \psi)^2]$.

Conversely, if home money is essential, $a_1(0, g_t) = \infty$, and if $L_t > 0$, then the home currency will never be abandoned, no matter what domestic monetary policy does: for any $g_t \geq 0$, there is some $m_t > 0$, so that (29) holds with equality. The CES specification (43) of the second part of the corollary exhibits this special case. There, it is perhaps a bit more surprising, that the domestic home currency will continue to play a sizable role, even if domestic monetary policy i_t veers far from the foreign monetary policy i_t^* , provided the latter is not at the zero lower bound, see Eq. (46).

Monetary policy makers should not take too much comfort in that latter case, however. Money is a means to an end. Payment systems evolve. It is hard to see a priori, why home money ought to be essential. The more easily domestic money can be substituted, the stronger the force for monetary policy synchronization. Pulling the levers of independent domestic monetary policy too much might unleash the market place innovations, which ultimately render home currency superfluous as a means of payment. Central banks would do well to pay attention.

The generalization to the case, where each country has its own aggregator function a in Eq. (22) and a^* in Eq. (23) is straightforward. This allows us to illustrate what happens, if the relative usefulness of the global currency differs across countries. We do so for the benchmark linear case. We obtain the following version of our main result, i.e. of Proposition 4.1.

Corollary 6.2. Suppose that the aggregator functions take the linear form

$$\begin{aligned} a(m, g) &= m + \xi g \\ a^*(m^*, g^*) &= m^* + \xi^* g^* \end{aligned}$$

for some constants $\xi > 0$ and $\xi^* > 0$. Assume complete markets, $Q_t > 0$, $Q_t^* > 0$ and that (29, 30), (31, 32) all hold with equality. Then

$$\frac{i_t}{1 + i_t} = \frac{\xi^*}{\xi} \frac{i_t^*}{1 + i_t^*} \quad (47)$$

The proof is in Appendix A.7. In particular, the corollary shows that Proposition 4.1 remains unchanged, if $\xi = \xi^* > 0$, i.e., if the global currency offers liquidity services in proportion to the domestic currencies, and these proportions are the same. A more detailed discussion is provided in appendix.

6.2. Incomplete markets

In this section, we relax the assumption of complete markets, by allowing for imperfect risk sharing at the international level. We put some structure by assuming that in each country households can trade in risk-free nominal bonds denominated in the two local currencies.

Assumption 6.1. Incomplete markets

Assume that agents in both countries can trade nominal bonds denominated in currency h and f . Therefore the following asset-pricing conditions hold

$$\frac{1}{1+i_t} = E_t[\mathcal{M}_{t+1}]$$

$$\frac{1}{1+i_t^*} = E_t\left[\mathcal{M}_{t+1} \frac{S_{t+1}}{S_t}\right]$$

in country h and

$$\frac{1}{1+i_t^*} = E_t[\mathcal{M}_{t+1}^*]$$

$$\frac{1}{1+i_t} = E_t\left[\mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}}\right]$$

in country f .

Given the above assumption, we can prove the following Proposition.

Proposition 6.3. Incomplete Markets

Given Assumption 6.1, $Q_t > 0$, $Q_t^* > 0$ and that all currencies are used in both countries, i.e. if equations (9), (10) and their foreign-country counterparts hold with equality, then the nominal interest rates satisfy

$$\frac{1}{1+i_t^*} = \frac{1}{1+i_t} + \text{cov}_t\left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} - \mathcal{M}_{t+1}\right) \quad (48)$$

The proof is in [Appendix A.8](#). Incomplete markets create a departure from our main result of equalization of interest rates in the presence of a global currency. However, this departure is limited since it depends only on a covariance term and, therefore, to a first-order approximation it becomes negligible. The covariance that matters is between the exchange rate of the global currency and the uninsurable risk in international financial markets, captured by the deviation from the complete-market assumption.

With complete markets, a higher interest rate in country h with respect to f was crowding out the home currency for the liquidity role. Here, it would be still consistent with the coexistence of the local currency h with the global currency, provided the covariance in (48) is positive, i.e.

$$\text{cov}_t\left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}}\right) > \text{cov}_t\left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}\right).$$

The condition says that the global currency provides better insurance in country f rather than h , i.e. its h -denominated return $Q(t+1)/Q(t)$ is higher in country f rather than country h , when resources are needed there as indicated by $\mathcal{M}_{t+1}^* S_t/S_{t+1}$ as opposed to the necessities at home indicated by $\mathcal{M}_{t+1}$. In equilibrium, the higher risk premium in h is offset by the lower opportunity cost i_t of holding money, see Eq. (48).

With the caveat of the milder linkage between nominal interest rates given by (48), we would still get that at relatively higher interest rates the local currency is abandoned as a medium of exchange in its country while, at relatively lower rates, it crowds out the global currency.

7. Examples

In the previous sections, we presented our results using a general framework with a generic notation for the stochastic discount factors and the liquidity services. We now provide several examples of models which put more structure on preferences and constraints. We consider four different models: 1) a Lagos-Wright monetary model; 2) a money-in-utility function model; 3) a cash-in-advance-constraint model in which the “credit” market opens before the “cash” market; 4) a cash-in-advance-constraint model in which the “cash” market opens before the “credit” market. The first three models can be cast in the framework of Section 3 in which liquidity services are received at the same time money is held in the agents’ portfolio. Model 4) deals with the case of delayed liquidity services, which is discussed in its more general form in Appendix.

7.1. Lagos-Wright model

We describe the home country: the description of the foreign country is exactly parallel. There are infinitely many periods. Each period has two subperiods. In the morning, there is a centralized market (CM), while there is a decentralized market (DM) in the afternoon. There is a continuum of agents. In the CM market, all agents meet and trade monies, assets, as well as a morning consumption good enjoyed according to a linear utility function. Denote the morning consumption by c_t . Negative consumption denotes production. In the decentralized market of the afternoon, agents meet pairwise randomly. Each agent chooses the quantity $q \geq 0$ of a good they wish to produce, experiencing disutility $-w(q)$ in doing so. We normalize $w(0) = 0$. Production of a strictly positive quantity is only useful, if the agent they meet happens to like that good. From the perspective of each agent, this happens with probability σ . In that case, we call the producing agent the “seller”, and the other agent the “buyer”. We assume that buyers can only trade money against goods in the DM; they cannot use other assets such as bonds. Agents therefore have to decide on the quantities M_t and G_t of the home and global monies to acquire earlier in the CM to allow trading in the DM. If they do not meet a seller, agents will hold their monies until the CM in the next period. If they meet a seller, they will make the seller a take-it-or-leave-it offer (TIOLI) of $(q_t, \tilde{M}_t, \tilde{G}_t)$. That is, the buyer offers to purchase a quantity q_t in return for currency amounts $\tilde{M}_t$ and $\tilde{G}_t$. The seller can either accept or reject that offer. Periods are discounted at rate β . We assume that aggregate shocks will be drawn at “dawn”, before the CM opens. There are no further shocks within a period. Given the stochastic sequence $(c_t, q_t)_{t=t_0}^{\infty}$ for some agent, with $c_t \in \mathbf{R}$ and $q_t \geq 0$, a buyer agent enjoys utility

$$E_0 \sum_{t=0}^{\infty} \beta^t \left(c_t + \mathbf{1}_{\text{“buyer” in } t} u(q_t) - \mathbf{1}_{\text{“seller” in } t} w(q_t) \right)$$

where $\mathbf{1}_{\text{“buyer” in } t}$ and $\mathbf{1}_{\text{“seller” in } t}$ are indicator functions taking the value 1 or 0, depending on whether the agent is a buyer resp. a seller in period t in a match with a successful completion of DM trading. Note here that q_t is consumption from the perspective of the buyer and production from the perspective of the seller. Let $1/P_t$ be the CM price in terms of the morning good of a unit of home currency. Put differently, one unit of the morning good costs P_t units of the home currency, which is the conventional notation. One unit of the global currency costs Q_t units of the home currency in the morning market. We assume that $u'(0) = \infty$ and $w'(0) < \infty$: this assures that buyers and sellers will strike a deal at a strictly positive quantity $q_t > 0$. Given the linearity of preferences in c_t , the nominal stochastic discount factor relevant for pricing assets from one morning to the next is therefore

$$\mathcal{M}_{t+1} = \beta \frac{P_t}{P_{t+1}}. \quad (49)$$

As usual, a riskless nominal bond will offer a nominal interest rate i_t , satisfying

$$1 = E_t[\mathcal{M}_{t+1}(1 + i_t)]$$

Consider the decentralized market or DM in t and a seller. For a unit of the home currency, he can buy $1/P_{t+1}$ morning goods in $t + 1$, yielding expected utility $E_t[\beta/P_{t+1}]$ when discounted to the DM. Similarly, a unit of the global currency yields discounted utility $E_t[\beta Q_{t+1}/P_{t+1}]$. The seller is therefore indifferent between rejecting the offer versus accepting to produce q_t units of the good for receiving $\tilde{M}_t$ units of home currency as well as $\tilde{G}_t$ units of the global currency, iff

$$w(q_t) = E_t \left[\beta \frac{1}{P_{t+1}} \right] \tilde{M}_t + E_t \left[\beta \frac{Q_{t+1}}{P_{t+1}} \right] \tilde{G}_t. \quad (50)$$

The buyer enters the DM, holding M_t units of the home currency and G_t units of the global currency. He values the remaining currencies after transacting with the seller just as much as the seller values received currencies. The buyer makes a TIOLI offer

$(q_t, \tilde{M}_t, \tilde{G}_t)$, evaluating the tradeoff between purchasing goods now against the opportunity costs of spending tomorrow. The buyer thus solves

$$\max_{q_t, \tilde{M}_t, \tilde{G}_t} u(q_t) - E_t \left[\beta \frac{1}{P_{t+1}} \right] \tilde{M}_t - E_t \left[\beta \frac{Q_{t+1}}{P_{t+1}} \right] \tilde{G}_t, \quad (51)$$

subject to keeping the seller at his indifference point (50) and subject to not spending more cash than is available,

$$0 \leq \tilde{M}_t \leq M_t, \quad (52)$$

$$0 \leq \tilde{G}_t \leq G_t. \quad (53)$$

It is immediately clear that we only need to keep track of the total utility equivalent of available currency and spent currency,

$$m_t = E_t \left[\beta \frac{1}{P_{t+1}} \right] M_t + E_t \left[\beta \frac{Q_{t+1}}{P_{t+1}} \right] G_t, \quad (54)$$

$$\tilde{m}_t = E_t \left[\beta \frac{1}{P_{t+1}} \right] \tilde{M}_t + E_t \left[\beta \frac{Q_{t+1}}{P_{t+1}} \right] \tilde{G}_t. \quad (55)$$

Therefore, the buyer's problem can be written as

$$v(m_t) = \max_{q_t, \tilde{m}_t} u(q_t) - \tilde{m}_t \quad (56)$$

$$\text{s.t. } w(q_t) = \tilde{m}_t \quad (57)$$

$$\tilde{m}_t \leq m_t \quad (58)$$

The solution is

$$u'(q_t) = w'(q_t) \quad (59)$$

if the currency constraint $\tilde{m}_t \leq m_t$ is slack and

$$w(q_t) = m_t$$

if not. In that case, the latter equation provides an implicit function $q_t = q(m_t)$, and implies

$$w'(q_t)q'(m_t) = 1. \quad (60)$$

Armed with these insights, we see that

$$v'(m_t) = 0 \quad (61)$$

if the currency constraint is slack and

$$v'(m_t) = u'(q(m_t))q'(m_t) - 1 = \frac{u'(q_t)}{w'(q_t)} - 1 \quad (62)$$

if not. With (59), we see that (62) holds, regardless of whether the currency constraint is slack or not. In the CM, the buyer can obtain home currency of quantity M_t at a utility cost M_t/P_t and global currency of quantity G_t at a utility cost $Q_t G_t/P_t$. We can thus proceed to use the indirect utility function $v(m)$ to formulate the CM problem for the buyer as maximizing

$$-\frac{M_t}{P_t} - \frac{Q_t G_t}{P_t} + \sigma v\left(E_t\left[\beta \frac{1}{P_{t+1}}\right] M_t + E_t\left[\beta \frac{Q_{t+1}}{P_{t+1}}\right] G_t\right) + \left(E_t\left[\beta \frac{1}{P_{t+1}}\right] M_t + E_t\left[\beta \frac{Q_{t+1}}{P_{t+1}}\right] G_t\right) \quad (63)$$

Define

$$L_t = \sigma E_t[\mathcal{M}_{t+1}] \left(\frac{u'(q_t)}{w'(q_t)} - 1 \right) \quad (64)$$

Differentiating (63) with respect to M_t as well as G_t and exploiting (49) yields the two first order conditions as claimed.

$$\begin{aligned} 1 &= L_t + E_t[\mathcal{M}_{t+1}] \\ Q_t &= L_t Q_t + E_t[\mathcal{M}_{t+1} Q_{t+1}] \end{aligned}$$

7.2. Money-in-the-utility-function model

The model follows the Sidrauski-Brock framework extended to allow for multiple currencies. Consumers preferences in Home country have the form

$$E_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} \left\{ U(C_t) + V\left(\frac{M_t^{\text{tot}}}{P_t}\right) \right\} \quad (65)$$

where $M_t^{\text{tot}} = M_t + Q_t G_t$ as in Eq. (2), where β is the rate of time preferences with $0 < \beta < 1$, C is a consumption good and P its price in units of currency h . We can also assume more generally that C represents a bundle of goods. Consumers enjoy utility from consumption through a concave function $U(\cdot)$ strictly increasing in C and from real money balances by holding currency h , M , and the global currency G . The utility $V(\cdot)$ increases weakly in real money balances but may exhibit a satiation point at a finite level of real money balances; Q_t is the price of the global currency in units of currency h . Consistently with the general framework of Section 3, consumers can invest in four securities: i) a risk-free bond denominated in currency h , B_h , paying an interest rate i ; ii) a risk-free bond denominated in currency f , B_f , paying an interest rate i^* ; iii) nonnegative amounts of money $M \geq 0$ in units of currency h and iv) nonnegative amounts $G \geq 0$ of the global money. Consumers can also trade in a complete set of state-contingent securities, spanning all states of nature. We omit these securities from the presentation of the consumer's budget constraint. The nominal exchange rate between currency h and f is denoted by S , as in the main text; let T denote lump-sum transfers received from the government in units of currency h while T_g are the transfers from the issuer of global money in units of the global currency. Finally, Y is the home endowment of good C . Preferences in country f are specular, with appropriate starred variables. Consumers are subject to the following budget constraint and wealth process

$$B_{h,t} + S_t B_{f,t} + M_t + Q_t G_t = W_t + P_t(Y_t - C_t) + T_t + Q_t T_{g,t},$$

$$W_t = M_{t-1} + Q_t G_{t-1} + (1 + i_{t-1}) B_{h,t-1} + (1 + i_{t-1}^*) S_t B_{f,t-1}.$$

In the preferences (65) domestic and global monies are perfect substitutes. Note that our general model in appendix Section 6.1 also allows for imperfect substitutability. While we allow the short sales of bonds, as in the main text, we impose a short-sale constraint on the global currency and currency h , i.e. $G \geq 0$ and $M \geq 0$. The first-order conditions with respect to B_h , B_f , M , G are

$$\frac{U_C(C_t)}{P_t} \frac{1}{1 + i_t} = E_t \left\{ \beta \frac{U_C(C_{t+1})}{P_{t+1}} \right\}$$

$$\frac{U_C(C_t)}{P_t} \frac{1}{1 + i_t^*} = E_t \left\{ \beta \frac{U_C(C_{t+1})}{P_{t+1}} \frac{S_{t+1}}{S_t} \right\}$$

$$\frac{U_C(C_t)}{P_t} \geq \frac{1}{P_t} V_m \left(\frac{M_t^{\text{tot}}}{P_t} \right) + E_t \left\{ \beta \frac{U_C(C_{t+1})}{P_{t+1}} \right\}$$

$$\frac{Q_t U_C(C_t)}{P_t} \geq \frac{Q_t}{P_t} V_m \left(\frac{M_t^{\text{tot}}}{P_t} \right) + E_t \left\{ \beta \frac{Q_{t+1} U_C(C_{t+1})}{P_{t+1}} \right\},$$

with the last two equations holding with equality for an interior solution in which $M \geq 0$ and $G \geq 0$, respectively. As in the main text, at least one should hold with equality. In the above conditions, $U_C(\cdot)$ and $V_m(\cdot)$ are the partial derivatives of the respective functions. These equations can be cast in the notation of [Section 3](#) by noting that the stochastic discount factors are

$$\mathcal{M}_{t+1} = \beta \frac{U_C(C_{t+1})}{U_C(C_t)} \frac{P_t}{P_{t+1}} \quad \mathcal{M}_{t+1}^* = \beta \frac{U_C(C_{t+1}^*)}{U_C(C_t^*)} \frac{P_t^*}{P_{t+1}^*}$$

and the liquidity premia are

$$L_t = \frac{V_m \left(\frac{M_t^{\text{tot}}}{P_t} \right)}{U_C(C_t)} \quad \text{and} \quad L_t^* = \frac{V_m \left(\frac{M_t^{\text{tot}*}}{P_t^*} \right)}{U_C(C_t^*)}, \quad (66)$$

where $M_t^{\text{tot}*}$ is defined in (3). Note that liquidity services endogenously satisfy additivity and immediacy. Note that complete markets imply that

$$\frac{U_C(C_t)}{P_t} = k \frac{U_C(C_t^*)}{S_t P_t^*}$$

for some positive parameter k . In the case where purchasing power parity holds, $P_t = S_t P_t^*$, marginal utilities of consumption are proportional across countries. When all currencies are used, [Proposition 4.1](#) applies and therefore $L_t = L_t^*$. Another implication is that the marginal utilities of real money balances $V_m(\cdot)$ are equalized across countries.

7.3. Cash-in-advance model, type I

Consider a cash-in-advance model with the timing of [Lucas and Stokey \(1987\)](#), in which the “credit” market opens before the “cash” market. Consumers living in country h have the following preferences

$$E_{t_0} \sum_{t=t_0}^{\infty} \beta^{t-t_0} U(C_{T,t}, C_{N,t}) \quad (67)$$

in which C_T and C_N are, respectively, a traded and non-traded good and β , with $0 < \beta < 1$, is the intertemporal discount factor; $U(\cdot, \cdot)$ is a concave function, strictly increasing in both arguments. Preferences in country f are similar with variables denoted by a star. Each period is divided into two sub-periods. In the first sub-period financial markets are open and the consumer's budget constraint is given by

$$B_{h,t} + S_t B_{f,t} + M_t + Q_t G_t = W_t + T_t + Q_t T_{g,t} \quad (68)$$

in which W_t is the nominal wealth, which remains after taking into account the purchases of goods in the previous period

$$W_t = (1 + i_{t-1}) B_{h,t-1} + (1 + i_{t-1}^*) S_t B_{f,t-1} + M_{t-1} + Q_t G_{t-1} + P_{T,t-1} (Y_{T,t-1} - C_{T,t-1}) + P_{N,t-1} (Y_{N,t-1} - C_{N,t-1}). \quad (69)$$

Y_T and Y_N are the endowments of the traded and non-traded goods, and P_T and P_N the respective prices. In the second subperiod of period t , the “cash” market opens and non-traded goods can be purchased following this constraint

$$M_t^{\text{tot}} \geq P_{N,t} C_{N,t}. \quad (70)$$

where $M_t^{\text{tot}} = M_t + Q_t G_t$ as in Eq. (2). Budget constraints can be written specularly for the consumers living in country f .

The first-order conditions with respect to B_h , B_f , M , G are

$$\frac{\lambda_t}{1 + i_t} = E_t \{ \beta \lambda_{t+1} \} \quad (71)$$

$$\frac{\lambda_t}{1 + i_t^*} = E_t \left\{ \beta \lambda_{t+1} \frac{S_{t+1}}{S_t} \right\} \quad (72)$$

$$\lambda_t \geq \mu_t + \beta E_t \{ \lambda_{t+1} \} \quad (73)$$

$$\lambda_t Q_t \geq \mu_t Q_t + \beta E_t \{ \lambda_{t+1} Q_{t+1} \} \quad (74)$$

with the last two equations holding with equality for an interior solution $M_t > 0$ and $G_t > 0$, respectively; λ_t and μ_t are the multipliers associated with constraints (68) and (70), respectively. Moreover, the first-order conditions with respect to C_N and C_T imply that

$$\frac{U_{C_N}(C_{T,t}, C_{N,t})}{P_{N,t}} = \mu_t + \beta E_t \{ \lambda_{t+1} \}, \quad (75)$$

$$\frac{U_{C_T}(C_{T,t}, C_{N,t})}{P_{T,t}} = \beta E_t \{ \lambda_{t+1} \}, \quad (76)$$

where $U_{C_T}(\cdot, \cdot)$ and $U_{C_N}(\cdot, \cdot)$ are the derivatives of function $U(\cdot, \cdot)$ with respect to the first and second arguments, respectively. We can now map this model in the notation of the general framework of Section 3 by noting that the stochastic discount factors are given by

$$\mathcal{M}_{t+1} = \frac{\beta \lambda_{t+1}}{\lambda_t} \quad \mathcal{M}_{t+1}^* = \frac{\beta \lambda_{t+1}^*}{\lambda_t^*}$$

while the liquidity premia can be written instead as

$$L_t = \frac{\mu_t}{\lambda_t} \quad L_t^* = \frac{\mu_t^*}{\lambda_t^*}.$$

Using first-order conditions (73), (75) and (76), we can also write the nominal stochastic discount factors

$$\begin{aligned} \mathcal{M}_{t+1} &= \beta \frac{U_{C_N}(C_{T,t+1}, C_{N,t+1})}{U_{C_N}(C_{T,t}, C_{N,t})} \frac{P_{N,t}}{P_{N,t+1}} \\ \mathcal{M}_{t+1}^* &= \beta \frac{U_{C_N}(C_{T,t+1}^*, C_{N,t+1}^*)}{U_{C_N}(C_{T,t}^*, C_{N,t}^*)} \frac{P_{N,t}^*}{P_{N,t+1}^*} \end{aligned}$$

and the liquidity premia as

$$\begin{aligned} L_t &= \frac{U_{C_N}(C_{T,t}, C_{N,t}) - \frac{P_{N,t}}{P_{T,t}} U_{C_T}(C_{T,t}, C_{N,t})}{U_{C_N}(C_{T,t}, C_{N,t})} \\ L_t^* &= \frac{U_{C_N}(C_{T,t}^*, C_{N,t}^*) - \frac{P_{N,t}^*}{P_{T,t}^*} U_{C_T}(C_{T,t}^*, C_{N,t}^*)}{U_{C_N}(C_{T,t}^*, C_{N,t}^*)}. \end{aligned}$$

As in the case of money-in-the-utility function, liquidity services endogenously satisfy additivity and immediacy. The results of Proposition 4.1 apply in the case that all currencies are used. Additional results can be derived in this particular example. Note first that market completeness implies that $\lambda_t = \kappa \lambda_t^*$ for some positive constant κ and at all t , which in the context of the above model can also be written as

$$\frac{U_{C_N}(C_{T,t}, Y_{N,t})}{P_{N,t}} = k \frac{U_{C_N}(C_{T,t}^*, Y_{N,t}^*)}{S_t P_{N,t}^*}. \quad (77)$$

¹¹ The result that $\lambda_t = \kappa \lambda_t^*$ implies (77) is driven by the fact that money allows the insurance of any movement in the price of non-traded goods in the cash constraint (70).

Under appropriate assumptions on the initial distribution of wealth, the constant k can be set equal to 1.¹¹ In (77), we have substituted equilibrium in the non-traded goods market, $C_{N,t} = Y_{N,t}$ and $C_{N,t}^* = Y_{N,t}^*$. Moreover, combining first-order conditions (71), (73), (75) and (76) it is possible to obtain that

$$\frac{U_{C_N}(C_{T,t}, Y_{N,t})}{U_{C_T}(C_{T,t}, Y_{N,t})} = (1 + i_t) \frac{P_{N,t}}{P_{T,t}} \quad \frac{U_{C_N}(C_{T,t}^*, Y_{N,t}^*)}{U_{C_T}(C_{T,t}^*, Y_{N,t}^*)} = (1 + i_t^*) \frac{P_{N,t}^*}{P_{T,t}^*},$$

Using $i_t = i_t^*$ and (77) with $k = 1$ in the above conditions, we obtain that

$$\frac{U_{C_T}(C_{T,t}, Y_{N,t})}{U_{C_T}(C_{T,t}^*, Y_{N,t}^*)} = \frac{P_{T,t}}{S_t P_{T,t}^*}. \quad (78)$$

Assume that the law-of-one price holds for traded goods, $P_{T,t} = S_t P_{T,t}^*$, and consider the special case in which $Y_{N,t} = Y_{N,t}^*$. Then (78) implies perfect cross-country risk-sharing of the consumption of traded goods, $C_{T,t} = C_{T,t}^*$. Using this result in (77), we also obtain that the law-of-one price holds for non-traded goods $P_{N,t} = S_t P_{N,t}^*$, for which the equalization of the nominal interest rates is key.

7.4. Cash-in-advance model, type II

Consider a cash-in-advance model with a different timing, in which the “cash” market now opens before the “credit” market. Preferences of consumers living in country h are similar to (67). Each period is divided into two sub-periods. In the first sub-period the non-traded good can be purchased subject to the following constraint,

$$M_{t-1} + Q_t G_{t-1} \geq P_{N,t} C_{N,t} \quad (79)$$

in which variables follow previous definitions. After the “cash” market closes, in the second sub-period of period t the “credit” market opens and consumers are subject to the following constraint,

$$B_{h,t} + S_t B_{f,t} + M_t + Q_t G_t + P_{T,t} C_{T,t} + P_{N,t} C_{N,t} = +P_{T,t} Y_{T,t} + P_{N,t} Y_{N,t} + T_t + Q_t T_{g,t} + W_t \quad (80)$$

where

$$W_t \equiv (1 + i_{t-1}) B_{h,t-1} + (1 + i_{t-1}^*) S_t B_{f,t-1} + M_{t-1} + Q_t G_{t-1}.$$

Budget constraints can be specularly written for the consumers in country f . The first-order conditions with respect to B_h , B_f , M , G are

$$\frac{\lambda_t}{1 + i_t} = E_t \{ \beta \lambda_{t+1} \}$$

$$\frac{\lambda_t}{1 + i_t^*} = E_t \left\{ \beta \lambda_{t+1} \frac{S_{t+1}}{S_t} \right\}$$

$$\lambda_t \geq \beta E_t \{ \mu_{t+1} + \lambda_{t+1} \}$$

$$\lambda_t Q_t \geq \beta E_t \{ (\mu_{t+1} + \lambda_{t+1}) Q_{t+1} \}$$

with the last two equations holding with equality for an interior solution $M_t > 0$ and $G_t > 0$, respectively. In the above conditions, λ_t and μ_t are the multipliers associated with constraints (80) and (79), respectively. Moreover, the first-order conditions with respect to C_N and C_T imply that

$$\frac{U_{C_N}(C_{T,t}, C_{N,t})}{P_{N,t}} = \mu_t + \lambda_t, \quad (81)$$

$$\frac{U_{C_T}(C_{T,t}, C_{N,t})}{P_{T,t}} = \lambda_t. \quad (82)$$

Note that in this model liquidity premia are received with a one-period delay. Therefore, this example can be mapped in the notation of the general framework presented in Appendix by noting that the stochastic discount factors are given by

$$\mathcal{M}_{t+1} = \frac{\beta \lambda_{t+1}}{\lambda_t} \quad \mathcal{M}_{t+1}^* = \frac{\beta \lambda_{t+1}^*}{\lambda_t^*}$$

while liquidity premia are

$$L_{t+1} = \frac{\mu_{t+1}}{\lambda_{t+1}} \quad L_{t+1}^* = \frac{\mu_{t+1}^*}{\lambda_{t+1}^*}.$$

Using first-order conditions (81) and (82), we can further write the stochastic discount factors and the liquidity premia as

$$\begin{aligned} \mathcal{M}_{t+1} &= \beta \frac{U_{C_T}(C_{T,t+1}, C_{N,t+1})}{U_{C_T}(C_{T,t}, C_{N,t})} \frac{P_{T,t}}{P_{T,t+1}} \\ \mathcal{M}_{t+1}^* &= \beta \frac{U_{C_T^*}(C_{T,t+1}^*, C_{N,t+1}^*)}{U_{C_T^*}(C_{T,t}^*, C_{N,t}^*)} \frac{P_{T,t}^*}{P_{T,t+1}^*} \end{aligned}$$

and

$$\begin{aligned} 1 + L_{t+1} &= \frac{U_{C_N}(C_{T,t+1}, C_{N,t+1})}{U_{C_T}(C_{T,t+1}, C_{N,t+1})} \frac{P_{T,t+1}}{P_{N,t+1}} \\ 1 + L_{t+1}^* &= \frac{U_{C_N^*}(C_{T,t+1}^*, C_{N,t+1}^*)}{U_{C_T^*}(C_{T,t+1}^*, C_{N,t+1}^*)} \frac{P_{T,t+1}^*}{P_{N,t+1}^*}. \end{aligned}$$

The results of Proposition A.1 and Corollary A.1 apply to this model.

8. Are gold and dollar global currencies?

One may wonder whether the emphasis on cryptocurrencies as emerging global currencies is misplaced. Is gold not already a globally acceptable means of payment? Isn't the Dollar already a global currency? The purpose of this section is to shed some light on these questions, complementing the literature discussion in Section 1.1. We investigate them more deeply in the companion paper Benigno et al. (2022).

8.1. Gold

First, consider the case of gold. Nowadays, it is hard or even impossible to make payments directly with gold: it is rare to find a shop which would accept it as a means of payment. The reasons can be verification issues (measurement of purity), the risk of fraud, the lack of normalization (size of a gold bar), or the inconvenience due to its weight. Moreover, gold offers benefits beyond those of a fiat currency: gold can be turned into jewelry or used for a variety of medical or industrial purposes. In addition, random findings of gold act as exogenous shocks to the gold supply and thus its price. This may also impede the gold's store of value functionality (see the abandonment of the Gold Standard). In sum, gold is rarely used as a medium of exchange, which is the focus and the basis for our analysis. For that reason, gold does not constitute a global currency, as analyzed in this paper.

8.2. Dollarization

Next, consider the Dollar. Indeed, international invoicing is often done in terms of Dollar, see Gopinath et al. (2020), and the Dollar serves as a vehicle currency, see e.g. Rey (2001). These papers, however, emphasize the "unit of account" function of money. "Dollarization" often means only the invoicing in terms of Dollar, thus concerning the numeraire function of money, and not its usage as a medium of exchange. However, in some countries often plagued by high inflation rates, physical Dollars are regularly used as a means of payment. As such, this type of Dollarization implies substitution mechanisms with a local currency similar to those emphasized in this work. Though, there are some caveats to consider. Dollarization is an asymmetric phenomenon for which Dollar circulates together with a local currency. On the opposite, the local currency does not circulate in U.S. Our analysis on restraining monetary policy also applies to this context. For the local currency to circulate with the Dollar, its interest rate should be capped by the Dollar interest rate. Monetary policy in the dollarized economy then becomes constrained, but not the U.S. monetary policy. Similarly, the literature on Dollarization

¹² For two recent examples, note that the "sand dollar" CBDC issued by Bahamas is only available to its residents so far. Likewise, China has declared that it does not wish for its emerging e-yuan to circulate internationally. Whether e.g. the e-yuan will remain a strictly national currency remains to be seen, of course.

has found that the return on the two currencies competing in a local market should be the same, e.g. [Giovannini and Turtelboom. \(1992\)](#), restating, therefore, [Kareken and Wallace \(1981\)](#) result. [Uribe \(1997\)](#), instead, provides a model in which the decision to adopt Dollars depends on the degree of dollarization. In this way, multiple equilibria arise and the value of the inflation rate can discriminate the prevailing equilibrium, full dollarization or absence of dollarization. In any case, our analysis differs from this literature since it considers competition coming from a global currency, which does not necessarily belong to any jurisdiction, in markets in which local sovereign currencies are circulating. In this context, we derive implications for the local currencies' monetary policies and exchange rates by looking at their relationship from an international perspective rather than just focusing on the national dimension. Indeed, we derive restrictions on cross-country interest rates and exchange rates – something that has not been the focus of the literature on dollarization. Whereas Dollars or another sovereign currency could as well represent the global currency of our model, a worldwide adoption of sovereign currencies in its paper form has not been seen so far. By contrast, a crypto-currency, unlinked at birth from any sovereign entity, may dramatically alter the financial landscape, once it becomes widely adopted as a medium of exchange in advanced countries through the World-Wide-Web. Similarly, central bank digital currencies may become global means of payments, depending on the particular arrangements chosen by the issuing central bank.¹²

9. Conclusion

Starting from a general framework, we analyze a two-country economy featuring a home, a foreign and a global (crypto)currency. For the benchmark case that markets are complete, that the global currency is used in both countries and that currency liquidity services are immediate, we show that nominal interest rates must be equal and that the exchange rate between the home and the foreign currency is a risk-adjusted martingale. We call this phenomenon *Crypto-Enforced Monetary Policy Synchronization (CEMPS)*. It adds a further restriction to the classic Impossible Trinity. We discuss the dangers for monetary policies that seek to circumvent this restriction. We characterize the implications for the exchange rate dynamics and the pricing dynamics of the global currency. If the global currency is backed by interest-bearing assets, additional and tight restrictions on monetary policy arise. We demonstrate that our general framework encompasses a number of classic monetary models, such as the Lagos-Wright model, models featuring money-in-the-utility function, and cash-in-advance models. In the appendix, we extend our results to the case of delayed liquidity services. There, we also discuss the general case where currencies are not perfect substitutes, providing robustness of our global currency deterrence result. We conclude that the introduction of a globally used currency may substantially change the landscape of international monetary policy.

Appendix A. Proofs

A.1. Proof of [Proposition 4.2](#)

Proof. [[Proposition 4.2](#)] We have

$$E_t \left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t} \right] = E_t \left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*} \right] \leq 1 - L_t^* = E_t[\mathcal{M}_{t+1}^*] = \frac{1}{1 + i_t^*} < \frac{1}{1 + i_t} = E_t[\mathcal{M}_{t+1}] = 1 - L_t$$

The first step follows by market completeness. The second and third step follow from equality in [\(12\)](#) and inequality in [\(13\)](#): since the global currency may or may not be in use in country f , it yields a weakly lower risk-adjusted return than currency f in country f . The fourth step uses Eq. [\(8\)](#). The fifth step, the inequality sign, is implied by the assumption $i_t < i_t^*$. The sixth step uses Eq. [\(7\)](#) and the final step follows from the assumption that currency h is used in country h , i.e. [\(9\)](#) holds with equality. Thus, $E_t \left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t} \right] < 1 - L_t$ and the global currency is not used in country h . We directly see that $L_t < L_t^*$ from our derivation. By market completeness $E_t \left[\mathcal{M}_{t+1} \frac{S_{t+1}}{S_t} \right] = E_t[\mathcal{M}_{t+1}^*] < E_t[\mathcal{M}_{t+1}]$ where the last step follows from the derivation above. Therefore, S_t follows a supermartingale in the country- h risk-adjusted measure. Vice versa, $E_t[\mathcal{M}_{t+1}^*] < E_t[\mathcal{M}_{t+1}] = E_t \left[\mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} \right]$. Thus, with $S^* = 1/S$, $E_t[\mathcal{M}_{t+1}^*] < E_t \left[\mathcal{M}_{t+1}^* \frac{S_{t+1}}{S_t} \right]$ and also the exchange rate from the perspective of country f follows a submartingale. $\square$

A.2. Proof of [Proposition 4.3](#)

Proof. [Proposition 4.3] We have

$$\begin{aligned} E_t[\mathcal{M}_{t+1}] &= \frac{1}{1+i_t} < \frac{1}{1+i_t^*} = E_t[\mathcal{M}_{t+1}^*] \\ &\leq 1-L_t^* = E_t\left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*}\right] = E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] \leq 1-L_t \end{aligned}$$

Here the first step uses Eq. (7). The second step uses the policy set in the two countries, $i_t \geq i_t^*$, the third step Eq. (8). The fourth step and inequality follows because currency f may or may not be used in country f . The fifth step uses that the global currency is used in country f . The sixth step uses completeness of markets and the last step uses that the global currency may or may not be adopted in country h . Altogether, $E_t[\mathcal{M}_{t+1}] < 1-L_t$ for $i > i^*$. Alternatively, $E_t[\mathcal{M}_{t+1}^*] < 1-L_t^*$, if currency f is not used in country f , and thus $E_t[\mathcal{M}_{t+1}] < 1-L_t$ for $i_t = i_t^*$. $\square$

A.3. Proof of Proposition 5.1

Proof. [Proposition 5.1] (i) Assume $\phi_t < i_t$. Then $1-L_t \geq E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] = (1+i_t-\phi_t) E_t[\mathcal{M}_{t+1}] > E_t[\mathcal{M}_{t+1}]$. The first inequality holds by (10), the second step holds by (21), the third step follows from $i_t > \phi_t$. Since $1-L_t > E_t[\mathcal{M}_{t+1}]$, local currency h is not used. Given the assumption that at least one currency is used in country h , (10) has to hold with equality, $1-L_t = (1+i_t-\phi_t) E_t[\mathcal{M}_{t+1}]$, and the global currency is used in h . By no arbitrage, a comparison between the return on the global currency and the bond through (7) yields $\frac{1-L_t}{1+i_t-\phi_t} = \frac{1}{1+i_t}$ and thus $L_t = \frac{\phi_t}{1+i_t}$. (ii) Assume $\phi_t = i_t$, then $1-L_t \geq E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] = (1+i_t-\phi_t) E_t[\mathcal{M}_{t+1}] = E_t[\mathcal{M}_{t+1}]$ and since at least one currency has to be in use, we have $1-L_t = E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] = E_t[\mathcal{M}_{t+1}]$, implying that both currencies are used. (iii) Assume $\phi_t > i_t$, then $1-L_t \geq E_t[\mathcal{M}_{t+1}] > (1+i_t-\phi_t) E_t[\mathcal{M}_{t+1}] = E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right]$. Thus, the global currency is not used. But since one currency has to be used, it has to be currency h , $1-L_t = E_t[\mathcal{M}_{t+1}]$. $\square$

A.4. Proof of Proposition 6.1

Proof. [Proposition 6.1] Eq. (30) and its foreign-country counterpart together with the complete markets assumption deliver

$$L_t a_{2,t} = 1 - E_t\left[\mathcal{M}_{t+1} \frac{Q_{t+1}}{Q_t}\right] = 1 - E_t\left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*}\right] = L_t^* a_{2,t}^*$$

and thus the second claim. Use (29) as well as $1-E_t[\mathcal{M}_{t+1}] = i_t/(1+i_t)$ together with its foreign-country counterparts to see that

$$\frac{i_t}{1+i_t} \frac{a_{2,t}}{a_{1,t}} = L_t a_{2,t} = L_t^* a_{2,t}^* = \frac{i_t^*}{1+i_t^*} \frac{a_{2,t}^*}{a_{1,t}^*}$$

and thus (34). $\square$

A.5. Proof of Lemma 6.1

Proof. [Lemma 6.1] Concavity and constant returns to scale imply¹³ that

$$a_1(\bar{m}, 0) \leq a_1(m, g) \leq a_1(0, \bar{g}) \text{ and } a_2(0, \bar{g}) \leq a_2(m, g) \leq a_2(\bar{m}, 0)$$

for all $0 \leq m \leq \bar{m}$ and $0 \leq g \leq \bar{g}$. This implies (36). $\square$

A.6. Proof of Proposition 6.2

¹³ For example, note that $a_1(m, g) = a_1((\bar{g}/g)m, (\bar{g}/g)g) \leq a_1(0, \bar{g})$.

¹⁴ It stands to reason that $m_t = 0$, but we would have to prove that this is so, if we were to use that. Instead, note e.g. that $a(m, g) = \phi(m/g)g$ for some concave function ϕ . Calculate $a_{12}(m, g) = -\phi''(m/g)m/g^2 \geq 0$.

Proof. [Proposition 6.2] Eqs. (31) and (32) holding with equality imply

$$1 = \frac{i_t^*}{1 + i_t^*} \frac{a_{2,t}^*}{a_{1,t}^*} + E_t \left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*} \right] \quad (83)$$

where we have used $E_t[\mathcal{M}_{t+1}^*] = 1/(1 + i_t^*)$. The inequality (39) implies

$$1 - E_t[\mathcal{M}_{t+1}^*] = \frac{i_t}{1 + i_t} > \frac{i_t^*}{1 + i_t^*} \frac{a_{2,t}^*}{a_{1,t}^*} \frac{a_1(0, g_t)}{a_2(0, g_t)} = \left(1 - E_t \left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*} \right] \right) \frac{a_1(0, g_t)}{a_2(0, g_t)} = \left(1 - E_t \left[\mathcal{M}_{t+1}^* \frac{Q_{t+1}^*}{Q_t^*} \right] \right) \frac{a_1(0, g_t)}{a_2(0, g_t)} \geq L_t a_{2,t} \frac{a_1(0, g_t)}{a_2(0, g_t)} \geq L_t a_{1,t}$$

where we have used the complete-market assumption in the first equality on the second line and where we have used¹⁴ $a_{2,t} = a_2(m_t, g_t) \geq a_2(0, g_t)$ as well as $a_1(0, g_t) \geq a_1(m_t, g_t) = a_{1,t}$. Thus, the home currency is not used. $\square$

A.7. Proof of Corollary 6.2

Proof. [Corollary 6.2] This is a straightforward generalization of (34). The proof there applies verbatim here, when $a_{1,t}^*$ and $a_{2,t}^*$ denote the partial derivatives $a_1^*(m_t^*, g_t^*)$ and $a_2^*(m_t^*, g_t^*)$ of a^* rather than a with respect to the first respectively second argument and evaluated at m_t^* and g_t^* . $\square$

A.8. Proof of Proposition 6.3

Proof. [Proposition 6.3] Consider first Eq. (10) and write it as

$$1 = L_t + E_t \left[\frac{Q_{t+1}}{Q_t} \mathcal{M}_{t+1} \right] = L_t + \frac{1}{1 + i_t} E_t \left[\frac{Q_{t+1}}{Q_t} \right] + \text{cov}_t \left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1} \right). \quad (84)$$

in which, in the second line, we have used covariance properties and Assumption 6.1. As well, we can write (13) as

$$1 = L_t^* + E_t \left[\frac{Q_{t+1}}{Q_t} \frac{S_t}{S_{t+1}} \mathcal{M}_{t+1}^* \right],$$

having used $Q_t = S_t Q_t^*$. We can manipulate the above equation, using again covariance properties and Assumption 6.1 to get

$$1 = L_t^* + E_t \left[\frac{Q_{t+1}}{Q_t} \right] E_t \left[\mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} \right] + \text{cov}_t \left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} \right) = L_t^* + \frac{1}{1 + i_t} E_t \left[\frac{Q_{t+1}}{Q_t} \right] + \text{cov}_t \left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} \right). \quad (85)$$

Combining (84) and (85), we obtain

$$L_t = L_t^* + \text{cov}_t \left(\frac{Q_{t+1}}{Q_t}, \mathcal{M}_{t+1}^* \frac{S_t}{S_{t+1}} - \mathcal{M}_{t+1} \right).$$

Using (9) and (12), we obtain Eq. (48). $\square$

Appendix B. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.jinteco.2022.103601>.

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