

628 **Supplementary Material**

## 629 Detailed Methods

### 630 Modeling framework

631 As outlined in the main text, our statistical framework is composed of three fundamental steps. Each of the  
632 steps could be carried out in a number of ways. We present the model in its full generality highlighting the  
633 model presented in the main text as the simplest version of the full model.

#### 634 a) From tree topology to interactions

635 We represent the topology of a binary phylogenetic tree with  $n$  leaves (i.e., the species in the pool) as a binary  
636 matrix  $V$  of size  $(2n - 1) \times n$ . The rows of the matrix represent either the extant species or their ancestors  
637 (including the common ancestor to all species, i.e., the root of the tree), while the columns represent the  
638 extant species. A coefficient  $V_{ij} = 1$  if  $i$  is an ancestor of  $j$  (or  $j$  itself), and is zero otherwise. This matrix  
639 is called the “basis matrix” of the tree in the literature (Bravo *et al.* 2009), and is closely related to the  
640 correlation structure induced by shared evolutionary history (Hansen & Martins 1996): given a vector of  
641  $2n - 1$  branch lengths  $\alpha$ , then  $V^T D(\alpha) V$  is the variance-covariance matrix of the tree.

642 Inspired by classic consumer-resource models, we parameterize the  $n \times n$  matrix of interactions between the  
643 species as:

$$A = D(\gamma) V^T D(\lambda) V D(\theta) \quad , \quad (1)$$

644 where  $\gamma$  and  $\theta$  are positive vectors of length  $n$  with entries summing to one (thus representing  $n - 1$  free  
645 parameters each),  $\lambda$  is a positive vector of length  $2n - 1$ ,  $D(\zeta)$  is a diagonal matrix with the elements of  $\zeta$  on  
646 the diagonal, and  $V^T$  denotes the transpose of matrix  $V$ . We therefore have  $4n - 3$  free parameters in total.  
647 This is the full, most complex model we consider, referred to as model 4. The model presented in the main  
648 text (model 1) has the same formulation except that in its simplest version both  $D(\gamma)$  and  $D(\theta)$  are taken  
649 to be  $\frac{1}{n} I$ , i.e., a scaled version of the identity matrix, which reduces the number of parameters to  $2n - 1$ .  
650 We also consider models with intermediate complexity in which either  $D(\gamma)$  (model 2) or  $D(\theta)$  (model 3) are  
651 taken as the scaled identity matrix, resulting in  $3n - 2$  parameters on each of these alternative versions. For  
652 every tree with  $n$  species that we are fitting, regardless of the model, we fit  $2n - 1$  branch length parameters,  
653 which include the branches related to the  $n$  tips, representing the independent evolutionary history of each  
654 species, and all  $n - 1$  internal branches. Eq.1 expresses overlap in resource use between species, with more  
655 closely related species sharing more similar resource requirements, and competing more strongly as a result.  
656 Further details on these parameterizations and their derivation from consumer-resource models are reported  
657 in the section “Derivation of the model from consumer-resource dynamics”.

658 Provided with a tree topology describing the evolutionary history of the  $n$  species in the pool (defining the  
659 associated matrix  $V$ ), and empirical abundances for a pool of species grown in different combinations, we  
660 aim to find the maximum likelihood estimates of the parameters  $\gamma$ ,  $\lambda$ , and  $\theta$ , keeping in mind that for the  
661 simplest model formulation in the main text we are only estimating  $\lambda$  and for model 2 we also estimate  $\gamma$ ,  
662 for model 3 we also estimate  $\theta$  and for the full model we estimate all parameters. To achieve this goal, we  
663 first relate interactions to predicted abundances, and then predicted abundances to the experimental data.

#### 664 b) From interactions to predictions

665 We want to relate species interactions, encoded in the phylogenetically-structured matrix  $A$  (Eq. 1) with  
666 the abundances species would attain in different assemblages. Take  $k$  to be the set of species in a given  
667 assemblage. We assume that the abundance of species  $i$  in assemblage  $k$ , denoted  $x_i^{(k)}$ , is linearly related  
668 to the abundance of the other species in the assemblage, with each effect mediated by the relevant pairwise  
669 interaction strength:

$$x_i^{(k)} = \frac{1}{A_{ii}} \left( 1 - \sum_{j \in k; j \neq i} A_{ij} x_j^{(k)} \right) \quad .$$

670 Thus, species  $i$  grown alone would reach  $1/A_{ii}$  (its carrying capacity), while growth together with  $j$  would  
 671 yield a lower value whenever  $A_{ij} > 0$ , i.e., when species  $i$  and  $j$  are competitors.

672 Writing  $A^{(k)}$  for the sub-matrix of  $A$  obtained by retaining only the columns and rows of species in assemblage  
 673  $k$ , we can write this system of equations in more compact form as:

$$A^{(k)}x^{(k)} = \mathbf{1}^{(k)} \quad ,$$

674 where  $\mathbf{1}^{(k)}$  is a vector of ones with as many elements as there are species in  $k$ . Thus, provided with a matrix  
 675  $A$  we can compute the value of  $x^{(k)}$ , for any  $k$ :

$$x^{(k)} = (A^{(k)})^{-1} \mathbf{1}^{(k)} \quad . \quad (2)$$

676 There are two possible outcomes: a) all the elements of  $x^{(k)}$  are positive, which we interpret as predicted  
 677 coexistence of the species in assemblage  $k$ , with expected abundances specified by the vector  $x^{(k)}$ ; or b) one  
 678 or more of the elements are negative, which we interpret as the impossibility of coexistence for this set of  
 679 species. Versions of this basic framework have been proposed numerous times in the ecological literature  
 680 (Ansari *et al.* 2021; Fort 2018; Maynard *et al.* 2020; Xiao *et al.* 2017), and here we closely follow the  
 681 approach of Maynard *et al.* (2020) and its extension in Skwara *et al.* (2023).

682 Provided with a matrix  $A$  defined in Eq. 1, we can predict the coexistence and expected abundances of  
 683 species in all possible assemblages using Eq. 2. We then compare these predictions to the empirical data.

### 684 c) From predictions to likelihoods

685 Each data set comprises a set of measurements  $\tilde{x}_i^{(k,r)}$ , specifying the biomass of species  $i$  when growing in  
 686 assemblage  $k$  (i.e., defined by the extant species in the plot) and replicate  $r$ . The data sets contain a large  
 687 number of assemblages, possibly with replicated experiments (i.e., distinct plots in which the same final  
 688 assemblage is observed). We take these measurements to be noisy estimates of the “true”, expected biomass  
 689 of species  $i$  in assemblage  $k$ :

$$\tilde{x}_i^{(k,r)} \stackrel{iid}{\sim} \text{Gamma} \left( \alpha, \frac{\alpha}{x_i^{(k)}} \right) \quad , \quad (3)$$

690 where we assume that the observations have been sampled independently from a Gamma distribution with  
 691 parameters  $\alpha$  (scale) and  $\alpha/x_i^{(k)}$  (rate), such that the expected value is  $\mathbb{E}(\tilde{x}_i^{(k,r)}) = x_i^{(k)}$  and the variance is  
 692  $\mathbb{V}(\tilde{x}_i^{(k,r)}) = \frac{1}{\alpha} (x_i^{(k)})^2$ . The parameter  $\alpha$  is assumed to be specific to the data set. Thus, for a given data set  
 693 all measurements are taken from distributions with a constant coefficient of variation,  $\frac{1}{\sqrt{\alpha}}$ . Whenever  $\alpha > 1$ ,  
 694 the mode of the distribution is larger than zero, and the distribution displays a central tendency.

695 The choice of this particular Gamma distribution is convenient (e.g., it has support on the positive real  
 696 line, a constant coefficient of variation, and adds a single free parameter); alternatively, one could assume a  
 697 Log-Normal distribution, or any other appropriate alternative. We do not expect the choice of a particular  
 698 distribution to affect our qualitative conclusions.

### 699 Numerical search for maximum likelihood estimates

700 In summary, provided with the phylogenetic tree for a species pool, the parameters of the model (the vectors  
 701  $\gamma$ ,  $\theta$  and  $\lambda$ , as well as the parameter  $\alpha$  controlling the shape of the distribution), and the empirical data,  
 702 comprising measurements of the biomass of the species across different (possibly replicated) assemblages, we  
 703 can: a) use the parameters and the tree to build a matrix of interactions (Eq. 1), b) compute the predicted  
 704 abundances for all assemblages (Eq. 2), and c) compute a likelihood by multiplying the probability of  
 705 observing each measurement under the fitted model Eq. 3.

706 This bridge from parameters to likelihoods allows us to search numerically for the maximum likelihood esti-  
707 mates of the parameters. Briefly, a) we initialize the parameters such that  $A$  is the sum of the identity matrix  
708 and a random matrix with small norm (practically, ensuring coexistence in all possible assemblages); b) search  
709 for maximum likelihood parameters via a heuristic optimization routine that combines simulated annealing,  
710 hill-climbing (where we slightly alter parameters and accept the move if the likelihood is increased), and nu-  
711 merical optimization via the Nelder-Mead and BFGS algorithms implemented in the *optim* function in *R* (R  
712 Core Team 2021); c) each step in b) is repeated 500 times until (presumptive) convergence to the maximum  
713 likelihood estimates. Parameterizations that predict a lack of coexistence for assemblages that were observed  
714 to coexist experimentally are discarded. Parameterizations that yield a likelihood lower than found for the  
715 corresponding star tree are also discarded. Finding optimal parameters is computationally very difficult  
716 (there can be many local optima in the parameter space), and very expensive (because each prediction re-  
717 quires the inversion of a matrix, following Eq. 2). We implemented the approach using a combination of *Stan*  
718 (Stan Development Team 2023) and *R* (R Core Team 2021) code, started each parameter search five times  
719 with a random initialization, and retained the best likelihood for each data set/model combination. The code,  
720 raw and organized data, and results are available at [github.com/StefanoAllesina/lemos-costa-2023](https://github.com/StefanoAllesina/lemos-costa-2023).

## 721 Testing for phylogenetic structure

722 In the preceding sections, we showed that, given empirical data and a matrix  $V$  corresponding to a phyloge-  
723 netic tree, we can find the maximum likelihood estimates of the parameters in Eq. 1, and thus the maximum  
724 likelihood associated with the tree,  $\mathcal{L}_V$ . To test whether phylogeny can explain species interactions, and  
725 consequently the observed abundances in different assemblages, we repeat the same fitting procedure for a  
726 random tree  $V'$ , yielding  $\mathcal{L}_{V'}$ . By repeating this procedure many times, we can estimate the probability  
727 that a random tree yields a higher likelihood than the “true” tree associated with  $V$ . As such we take  
728  $p \approx \frac{1}{m} \sum_i^m \mathcal{H}(\mathcal{L}_V \leq \mathcal{L}_{V'_i})$ , where  $m$  is the number of random trees,  $\mathcal{H}(\cdot)$  the Heaviside step function and  
729  $V'_i$  is the matrix associated with the  $i^{\text{th}}$  random tree.

730 Finally, we need to define what we mean by a random tree. We consider two possibilities: a) a random tree  
731 with the same number of leaves as the original constructed according to the Yule model, a classic speciation  
732 model in which every branch has the same probability of speciating at every time; b) a tree with the same  
733 topology as the original, but where we shuffle species’ identities. Therefore, for each data set we present  
734 randomizations for four nested models (all variations on Eq. 1, with the simplest model detailed in the main  
735 text) and two distinct ways of constructing the random trees. For each randomization method, we sample  
736 tree topologies until we have found one thousand distinct trees; whenever duplicate trees are encountered in  
737 this process, we fit both and retain the best likelihood.

## 738 Data and data organization

739 The methods of Maynard *et al.* (2020) were devised to analyze experiments carried out in controlled condi-  
740 tions with a small species pool, for which a substantial proportion of all possible combinations of species  
741 were co-cultured. We analyzed data sets from biodiversity and ecosystem functioning experiments which  
742 are often conducted in experimental plots, using a pool of a dozen or more species. Because the number of  
743 possible assemblages one can form with  $n$  species is  $2^n$ , and only dozens or hundreds of experimental plots  
744 are typically feasible, the number of sampled assemblages in these experiments is necessarily small compared  
745 to the theoretical limit (e.g.  $2^{10}$  is already more than a thousand distinct assemblages for  $n = 10$ ). We  
746 therefore attempted to select data sets in which a) only species that appear in multiple plots are considered  
747 to be part of the pool; b) unidentified biomass or non-target species do not dominate the plots; c) we have  
748 sufficient replication or diversity of assemblages to confidently fit the parameters of the model.

749 To this end, we consider data collected as part of the Biodiversity II experiment (Tilman *et al.* (2001),  
750 data from 2001 to 2018, inclusive, downloaded from the Cedar Creek website), the Wageningen diversity  
751 experiment (Van Ruijven & Berendse (2010), provided by Dr. Jasper van Ruijven), and an experiment  
752 carried out at the Toronto’s Koffler Scientific Reserve by Marc W. Cadotte (data accompanying Cadotte  
753 (2013)).

754 The data from Cadotte (2013) contains plots in which a subset of 14 species were planted. Some did not

755 grow and went extinct during the experiment. We consider a species that did not reach 2.5% of its maximum  
 756 observed biomass to be extinct in the plot. We then considered species that appeared in at least 5 distinct  
 757 assemblages; if a plot contained species that did not meet this requirement, the whole plot was discarded; the  
 758 procedure was then repeated until we obtained a subset of the original data in which all species appeared in  
 759 at least 5 distinct assemblages. This left us with 8 species, forming 27 distinct assemblages, for a total of 87  
 760 measurements (including replicated assemblages). Code to implement this procedure, along with the raw and  
 761 elaborated data are in the aforementioned repository ([github.com/StefanoAllesina/lemons-costa-2023](https://github.com/StefanoAllesina/lemons-costa-2023)).

762 The same general procedure was applied to the data from Van Ruijven & Berendse (2010), with each species  
 763 also required to be present in 5 distinct assemblages. After the selection procedure, all eight species were  
 764 retained, and we obtained nine separate data sets, one for each yearly sampling from 2001 to 2009, inclusive.

765 The data from Tilman *et al.* (2001) are the most difficult to process, because aside from the original target  
 766 pool of eighteen species, many other species are found in the plots, along with a substantial amount of litter  
 767 or unidentified biomass. We therefore included in the “species pool” a larger number of species, excluded  
 768 plots in which the total biomass for species not in the pool surpassed 10% of the total biomass, and then  
 769 applied the procedure used for the other data sets. In this way, we were able to extract nine data sets (for  
 770 distinct years) containing between 13 and 20 species and a substantial number of assemblages.

771 Summary statistics for each data set, including number of species, number of unique assemblages and number  
 772 of measurements are reported in Table 2. The name of the species in each data set across all years (when  
 773 applicable) are in Table 1.

774 To obtain a phylogeny for each species pool, we normalized species names using the World Flora Database  
 775 (<http://www.worldfloraonline.org/>) and then constructed the phylogenetic tree associated with each set of  
 776 species using the *V.PhyloMaker* package in *R* (Jin & Qian 2019).

Table 1: Species names and family for each data set

source	species	family
Cadotte	<i>Andropogon gerardii</i>	Poaceae
Cadotte	<i>Desmodium canadense</i>	Fabaceae
Cadotte	<i>Elymus canadensis</i>	Poaceae
Cadotte	<i>Elymus trachycaulus</i>	Poaceae
Cadotte	<i>Monarda fistulosa</i>	Lamiaceae
Cadotte	<i>Rudbeckia hirta</i>	Asteraceae
Cadotte	<i>Schizachyrium scoparium</i>	Poaceae
Cadotte	<i>Solidago altissima</i>	Asteraceae
Biodiversity II	<i>Achillea millefolium</i>	Asteraceae
Biodiversity II	<i>Agrostis rudis</i>	Poaceae
Biodiversity II	<i>Amorpha canescens</i>	Fabaceae
Biodiversity II	<i>Andropogon gerardi</i>	Poaceae
Biodiversity II	<i>Asclepias tuberosa</i>	Apocynaceae
Biodiversity II	<i>Bouteloua aristidoides</i>	Poaceae
Biodiversity II	<i>Elymus repens</i>	Poaceae
Biodiversity II	<i>Koeleria pyramidata</i>	Poaceae
Biodiversity II	<i>Lespedeza capitata</i>	Fabaceae

source	species	family
Biodiversity II	<i>Liatris aspera</i>	Asteraceae
Biodiversity II	<i>Lupinus perennis</i>	Fabaceae
Biodiversity II	<i>Monarda fistulosa</i>	Lamiaceae
Biodiversity II	<i>Panicum oligosanthos</i>	Poaceae
Biodiversity II	<i>Panicum sumatrense</i>	Poaceae
Biodiversity II	<i>Petalostemum villosum</i>	Fabaceae
Biodiversity II	<i>Poa pratensis</i>	Poaceae
Biodiversity II	<i>Rumex acetosella</i>	Polygonaceae
Biodiversity II	<i>Schizachyrium scoparium</i>	Poaceae
Biodiversity II	<i>Solidago nemoralis</i>	Asteraceae
Biodiversity II	<i>Sorghastrum nutans</i>	Poaceae
Biodiversity II	<i>Sporobolus cryptandrus</i>	Poaceae
Wageningen	<i>Agrostis capillaris</i>	Poaceae
Wageningen	<i>Anthoxanthum odoratum</i>	Poaceae
Wageningen	<i>Centaurea jacea</i>	Asteraceae
Wageningen	<i>Festuca rubra</i>	Poaceae
Wageningen	<i>Holcus lanatus</i>	Poaceae
Wageningen	<i>Leucanthemum vulgare</i>	Asteraceae
Wageningen	<i>Plantago lanceolata</i>	Plantaginaceae
Wageningen	<i>Rumex acetosa</i>	Polygonaceae

777 **Derivation of the model from consumer-resource dynamics**

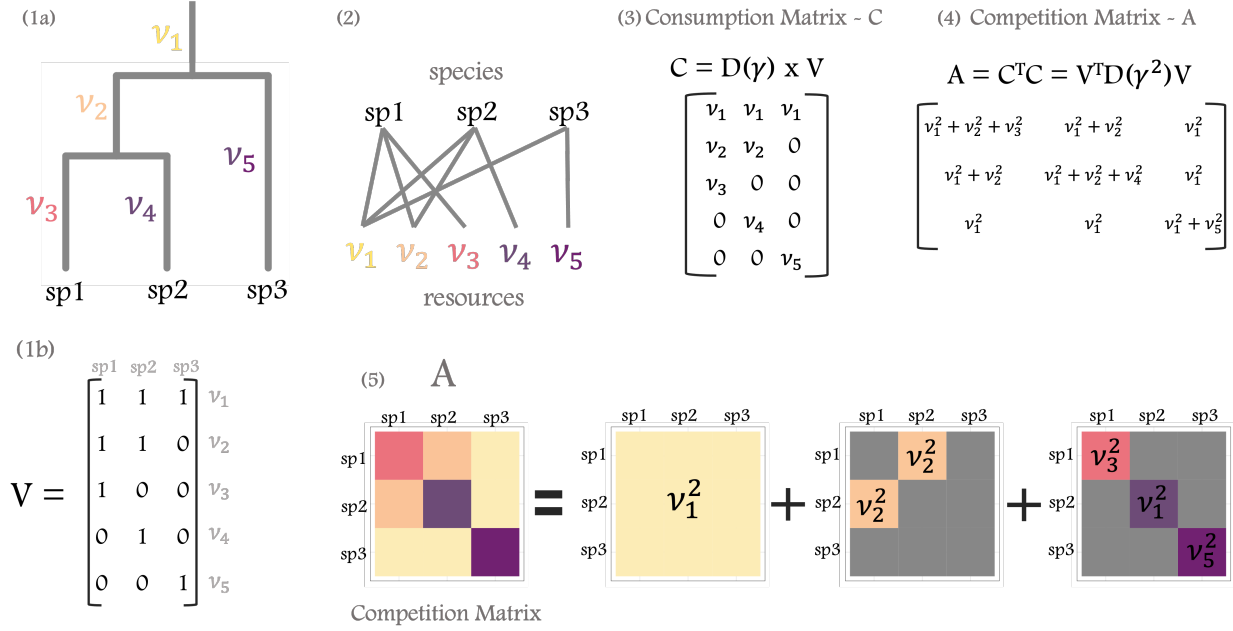


Figure 5: Consumer-resource framework for the model presented in the main text. 1) Each clade (including all the descendent species of a common ancestor) has access to a “private” resource, as encoded in matrix  $V$  (the rows are the resources, the columns the species, and a coefficient is one if the species can access the resource). 2) Network representation of the species (nodes  $sp_i$ ) and the resources (nodes  $\nu_i$ ) they consume (links) 3) Each resource has a value, stored in vector  $\nu$ ; in this case the consumption matrix is simply  $C = D(\nu)V$ . 4) The competition matrix  $A$  is obtained through the consumption matrix and is related to resources’ values and species’ shared evolutionary history encoded in the matrix  $V$ . The resulting matrix has a nested block structure, with a block per clade. 5) An additional interpretation of the competition matrix can be derived by considering the  $A$  matrix as the sum of the competition coefficients ( $\nu_j^2$ ) for each clade a species belongs to

778 We consider  $n$  consumer species with a specified phylogeny. We imagine a situation in which each clade in  
779 the tree has access to a clade-specific resource. Clade-specific resources are an idealization of the resources  
780 needed by the clade to support themselves and can be considered as the pool of all resources used by the  
781 species in the clade (including “private” resources which are the requirements of individual species. Thus we  
782 can build a matrix  $V$  with  $2n - 1$  rows (the resources, one per clade, which also includes a resource accessible  
783 to all species) and  $n$  columns (the consumers). The matrix has a coefficient of  $V_{ij} = 1$  whenever consumer  $j$   
784 has access to resource  $i$ , and zero elsewhere. Next, we model consumption, by assuming that each resource  
785 has a certain value (taken to be the same irrespective of the consumer), and that each consumer has a given  
786 uptake rate (taken to be the same for each resource):

$$C = D(v)VD(\alpha) = v\alpha^T \circ V \quad ,$$

787 where  $D(v)$  is a diagonal matrix with the value of each resource on the diagonal,  $D(\alpha)$  a diagonal matrix of  
788 uptake rates and  $\circ$  is the Hadamard product. We obtain a system of  $2n - 1 + n$  differential equations, which  
789 follow the Generalized Lotka-Volterra model (MacArthur consumer-resource model MacArthur (1970)):

$$\begin{cases} \frac{dx_i}{dt} = x_i \left( -\delta_i + \sum_{j=1}^{2n-1} C_{ji} y_j \right) \\ \frac{dy_j}{dt} = y_j \left( \rho_j - \kappa_j y_j - \sum_{i=1}^n C_{ji} x_i \right) \end{cases} \quad ,$$

790 in which  $x_i = x_i(t)$  is the density of consumer  $i$ ,  $y_j = y_j(t)$  is the density of resource  $j$ , and all parameters  
 791 are positive.  $\delta_i$  is the intrinsic death rate of consumer  $i$ ,  $\rho_j$  is the growth rate of resource  $j$  and  $\kappa_j$  is its self-  
 792 limitation. If we assume that resource dynamics quickly equilibrate for any consumer densities (practically,  
 793 if  $\rho_j \gg \sum_{i=1}^n C_{ji}x_i$ ), we can perform a “separation of time-scales” as in MacArthur (1970), and solve the  
 794 equation for the equilibrium of  $y_j$ :

$$y_j^* = \frac{1}{\kappa_j} \left( \rho_j - \sum_{i=1}^n C_{ji}x_i \right) .$$

795 Plugging these values into the equations for the consumers yields:

$$\begin{aligned} \frac{dx_i}{dt} &= x_i \left( -\delta_i + \sum_j C_{ij} \frac{1}{\kappa_j} \left( \rho_j - \sum_i C_{ji}x_i \right) \right) \\ &= x_i \left( -\delta_i + \sum_j C_{ij} \frac{\rho_j}{\kappa_j} - \sum_j \sum_k C_{ji} \frac{1}{\kappa_j} C_{jk}x_k \right) , \\ &= x_i \left( \zeta_i - \sum_k B_{ik}x_k \right) \end{aligned}$$

796 where we have defined  $\zeta_i = (\sum_j C_{ij}\rho_j/\kappa_j) - \delta_i$  and  $B = C^T D(\kappa)^{-1}C$ . Finally, we factor  $\zeta_i$  outside the  
 797 parenthesis, obtaining:

$$\frac{dx_i}{dt} = x_i \zeta_i \left( 1 - \sum_k \frac{1}{\zeta_i} B_{ik}x_k \right) .$$

798 The matrix of species’ interactions is therefore:

$$\begin{aligned} A &= D(\zeta)^{-1}B = D(\zeta)^{-1}C^T D(\kappa)^{-1}C \\ &= D(\zeta)^{-1}D(\alpha)V^T D(\nu)D(\kappa)^{-1}D(\nu)VD(\alpha) \\ &= D(\gamma)V^T D(\lambda)VD(\theta) , \end{aligned}$$

799 where  $\theta = \alpha$ ,  $\gamma = \frac{\alpha}{\zeta}$  and  $\lambda = \frac{\nu^2}{\kappa}$ . This is exactly the Eq. 1 in the main text, which we use for model 4.  
 800 Further assuming that  $\zeta = 1/\alpha$  we obtain model 2; choosing  $\alpha = 1$  yields model 3 and, finally, using both  
 801 simplifications we obtain model 1. Figure 5 illustrates the parameterization for the case of the simplest model:  
 802  $A = V^T D(\lambda)V$ . We note that the variance-covariance matrix of a tree with branch lengths  $\lambda$  would take  
 803 same form; as such, an alternative parameterization is thus to take competition coefficients to be the result  
 804 of evolution via Brownian motion of many traits (Ives & Helmus 2011; Serván *et al.* 2023). Additionally the  
 805 matrix  $A$  is proportional to the expected variance-covariance matrix of the residual error in a phylogenetic  
 806 generalized least squares regression model (Revell 2010).

## 807 **Tree distances and likelihoods**

808 To better understand the significantly good fit we observe for the true phylogenetic tree topology for most  
809 data sets, we investigated whether randomized trees that were more similar to the true tree also had higher  
810 likelihoods on average. To quantify the similarity between randomized trees and the true topology for each  
811 data set, we calculated the distance between them using an information-based generalized Robinson-Foulds  
812 metric, which we implemented using the TreeDist package in R (Smith 2020). This metric measures the  
813 similarity between two tree topologies by quantifying how much information the splits in the two trees hold  
814 in common. We also considered several alternative tree distance metrics, all of which produced similar results  
815 (not shown).

816 We then calculated the Pearson correlation between log-likelihood and distance (from the original tree) in  
817 each set of randomized trees (across all 19 data sets and 2 randomization methods). The original tree was  
818 always excluded from this analysis. The correlations are shown in Figure 6, plotted against the p-value found  
819 for the true tree against the corresponding randomization ensemble. We also regressed log-likelihood against  
820 distance in a linear model, to check whether there was a significant effect of distance.

821 Because many of the distributions of tree distances contained high leverage points, we used bootstrap re-  
822 sampling to calculate confidence intervals for the correlation coefficients and counted the fraction of bootstrap  
823 samples where distance was a significant predictor of log-likelihood (at the  $\alpha = 0.05$  level).

824 Overall, we found consistent negative relationships between the distance of each randomized tree from the  
825 true topology and its log-likelihood. These relationships were generally weak but consistently significant for  
826 17 out of 18 cases for the Biodiversity II data sets and 13 out of 18 cases for the Wageningen data sets.  
827 For the remaining data sets, including the Cadotte data, we found no evidence for a relationship between  
828 distance and log-likelihood. The strongest negative correlations coincided with the data sets where the true  
829 tree topology performed best (smallest p-values). However, we also found significant slopes for several data  
830 sets where the randomization test did not yield significant evidence for phylogenetic structure. In these  
831 cases, we hypothesize that the ability of trees to fit the data does not fall off smoothly with distance to the  
832 true phylogeny, but depends on specific topological features, such as the key splits we identify in Figure 4.  
833 Thus, because many (i.e. more than 1 in 20) random trees might have these key features, they can provide  
834 an equal or better fit compared to the true topology, despite differing from the true topology in other splits  
835 (which matter less for structuring interactions).

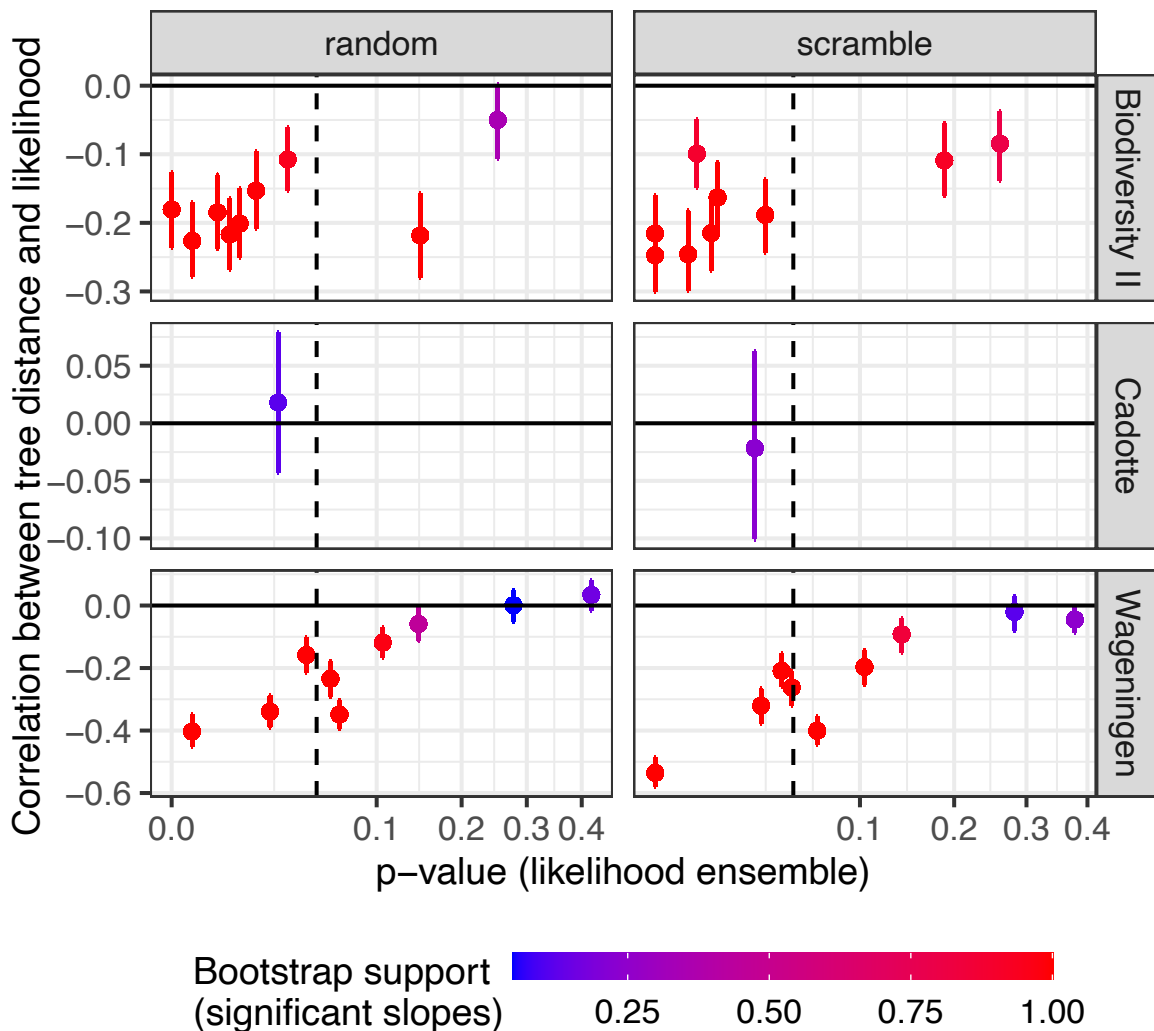


Figure 6: **Relationships between distance from the true tree and log-likelihood for randomized trees.** For each experiment (rows) and randomization method (columns), we plot the correlation between the distance from the true tree and the log-likelihood found in the ensemble of randomized trees (y-axis). For comparison, the p-value for the corresponding true phylogeny is plotted on the x-axis. Each point represents the set of randomizations corresponding to a specific data set (experiment/year combination). Bootstrap 95% confidence intervals are shown, and color indicates the fraction of bootstrap samples in which the slope of log-likelihood vs. distance was significantly different from zero. We find that almost all correlations are less than zero (solid horizontal line), and many data sets have consistently significant relationships between distance and log-likelihood. This is especially true for data sets where the randomization test p-value is less than 0.05 (vertical dashed line). Note that p-values (x-axis) are shown square-root transformed for better visualization.

## 836 Parameterizations based on molecular branch lengths

837 In our framework we fit models of species interactions based on population dynamics and constrained by  
838 species shared evolutionary history. Ultimately, our model uses phylogenetic tree structure to find the  
839 maximum likelihood estimates of branch lengths which are directly associated with interspecific competition  
840 based on data of species' biomasses when grown in different combinations. As highlighted in the main text,  
841 we make no assumption on the linearity or shape of the relationship between shared evolutionary history  
842 and competition strength. Instead we let the data (ecology) guide the fit, finding the distribution of branch  
843 lengths that maximizes the likelihood of the parameters given the data and model parameters while also  
844 minimizing predicted biomasses derived from model prediction versus observed biomasses in the experimental  
845 communities. It is also reasonable to imagine that the information encoded in the branch lengths of molecular  
846 phylogenies could still provide insights into the structure of these experimental ecological communities. If  
847 these branch lengths are reflective of trait evolution and most importantly, evolution of traits that are  
848 directly related to competitive interactions we would observe a good fit between predictions made by using  
849 the molecular phylogeny as the input of the interaction matrix in our modeling framework. To test this,  
850 we parameterize our model for species interactions with the molecular phylogeny, i.e, instead of fitting the  
851 branch lengths we used the distribution of branch lengths from the molecular phylogeny to get estimates of  
852 predicted abundances of species in the experimental communities. We then compared these predictions with  
853 the observed abundances. It is worth noticing that we are interested in the correlation between predicted and  
854 observed abundances and not necessarily in the absolute values of predicted abundances, as all abundances  
855 can be rescaled if we fitted the root. Fitting the root would only rescale the biomasses without changing the  
856 observed correlations. Additionally, because the phylogenetic trees used in our analyses were ultrametric, all  
857 species are predicted to achieve the same biomass when grown in monoculture, which is already a biologically  
858 unrealistic expectation. All data sets showed a poor correlation between the log of predicted and the log of  
859 observed biomasses (top panel in Figures 7-24).

860 Additionally, we compared the fitted branch lengths from our modeling framework with the molecular branch  
861 lengths from the phylogenies, showing that also in this case, the correspondence between estimated branch  
862 lengths show very little agreement (bottom panels in Figures 7-24). In this comparison we are also interested  
863 in the shape of the relationship and not in correspondence between the units, as the units of measurement  
864 of the molecular phylogeny are not comparable with the units of measure of the fitted branch lengths from  
865 our modeling framework. However, the comparison of the fitted branch length is made with the transformed  
866 square root of the molecular branch length as functional dissimilarity has been shown to be related to  
867 the square root of molecular distances (Letten & Cornwell 2015) and is an appropriate transformation for  
868 molecular branch lengths, but the same result applies to the un-transformed branch lengths.

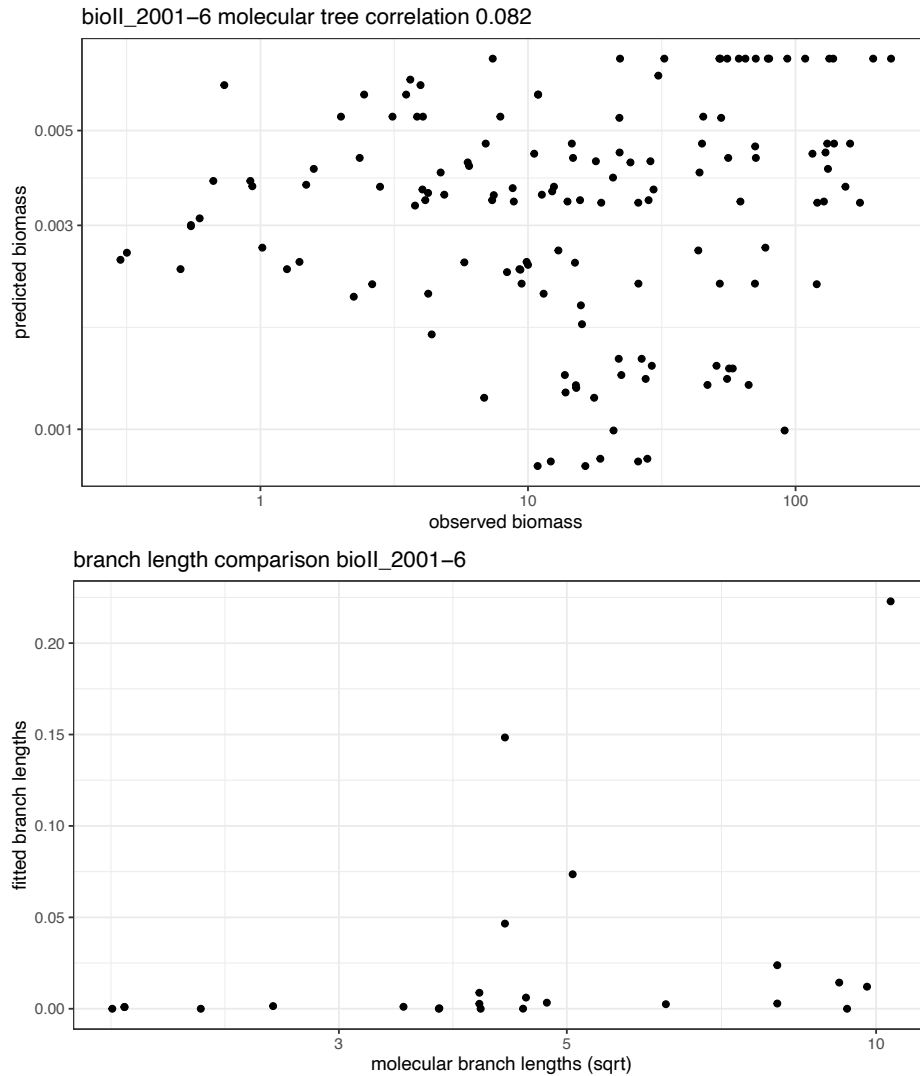


Figure 7: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

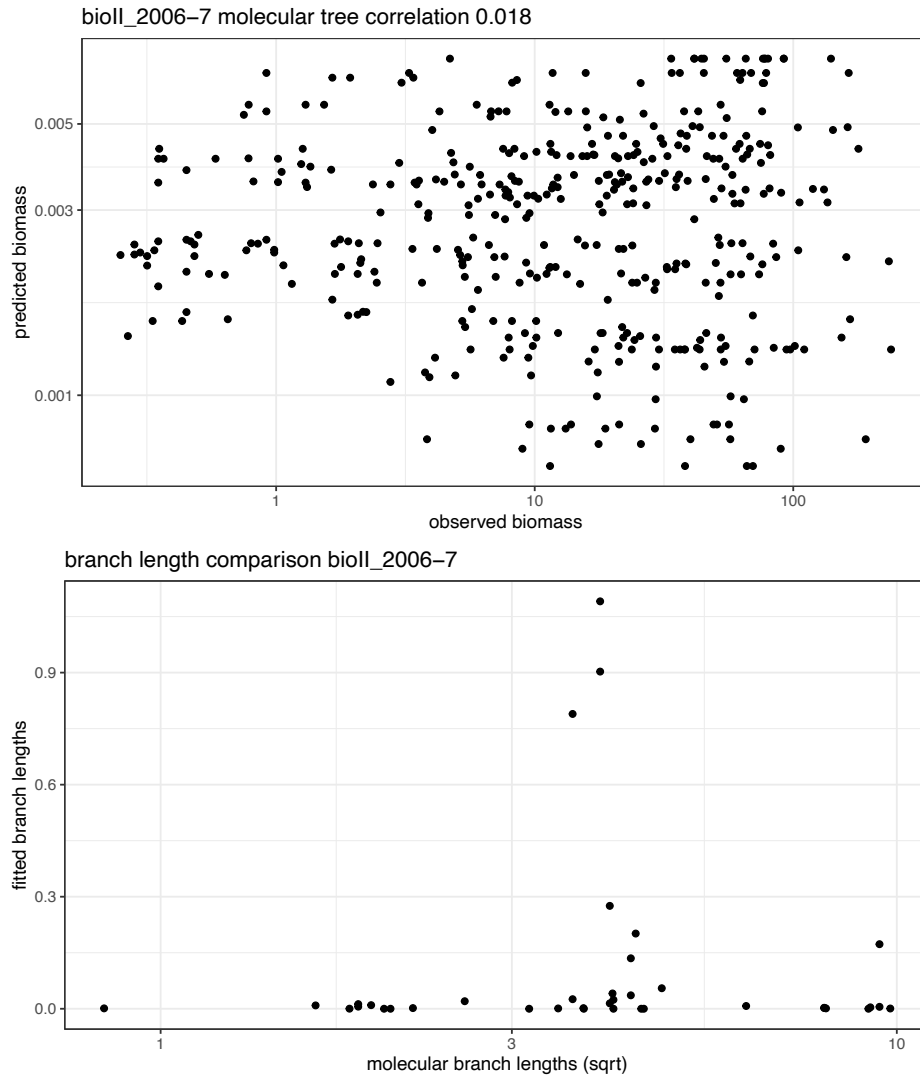


Figure 8: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

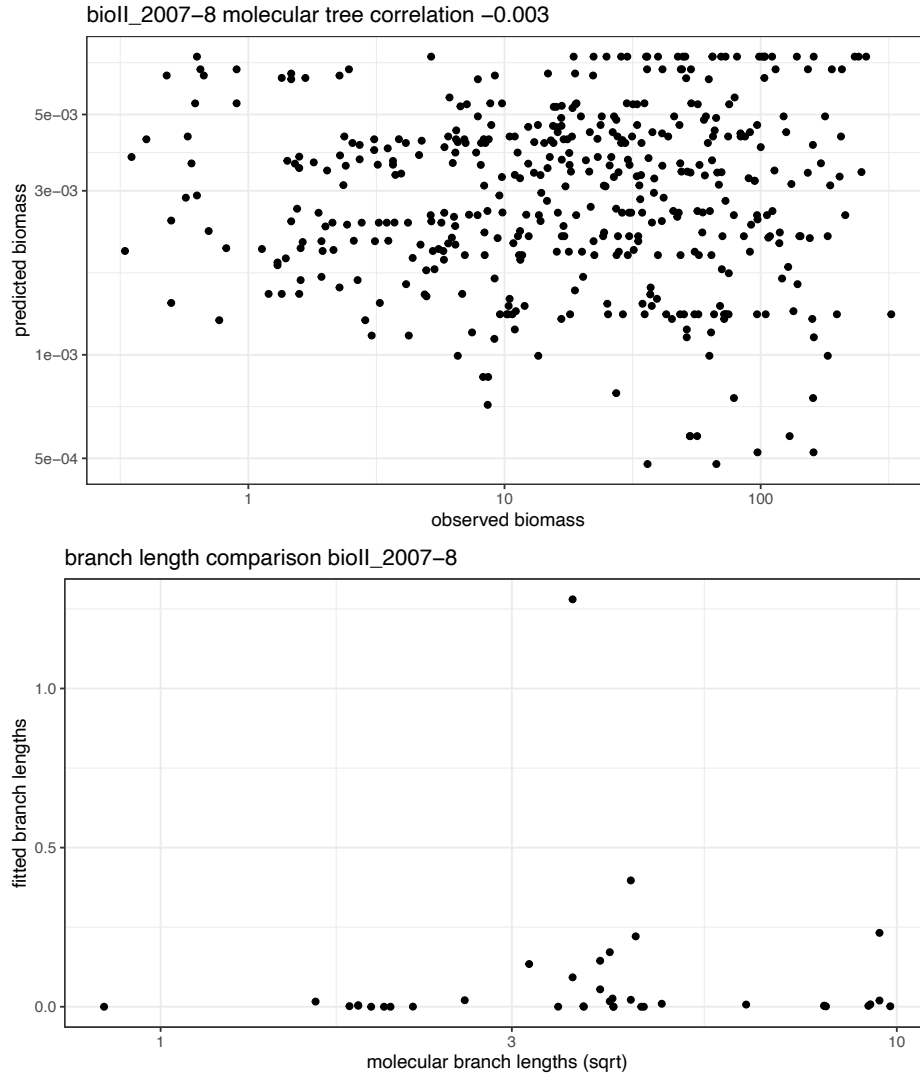


Figure 9: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

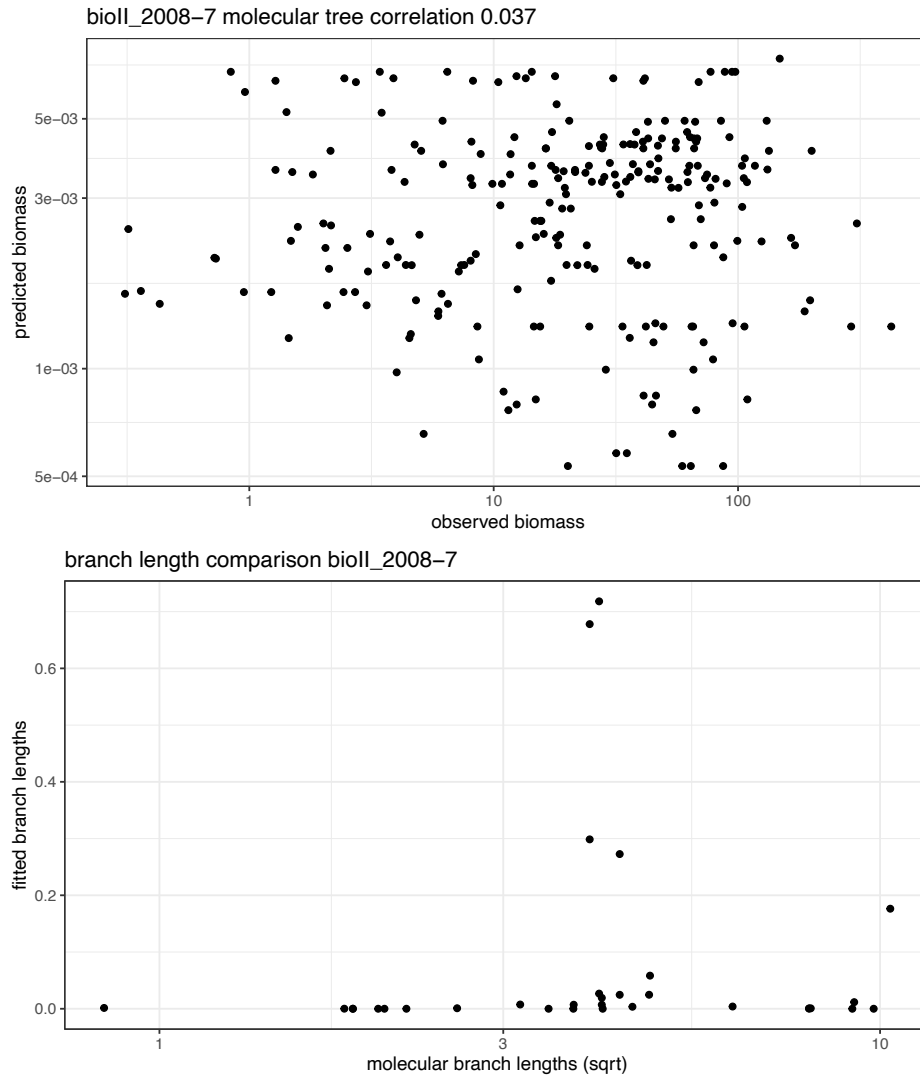


Figure 10: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

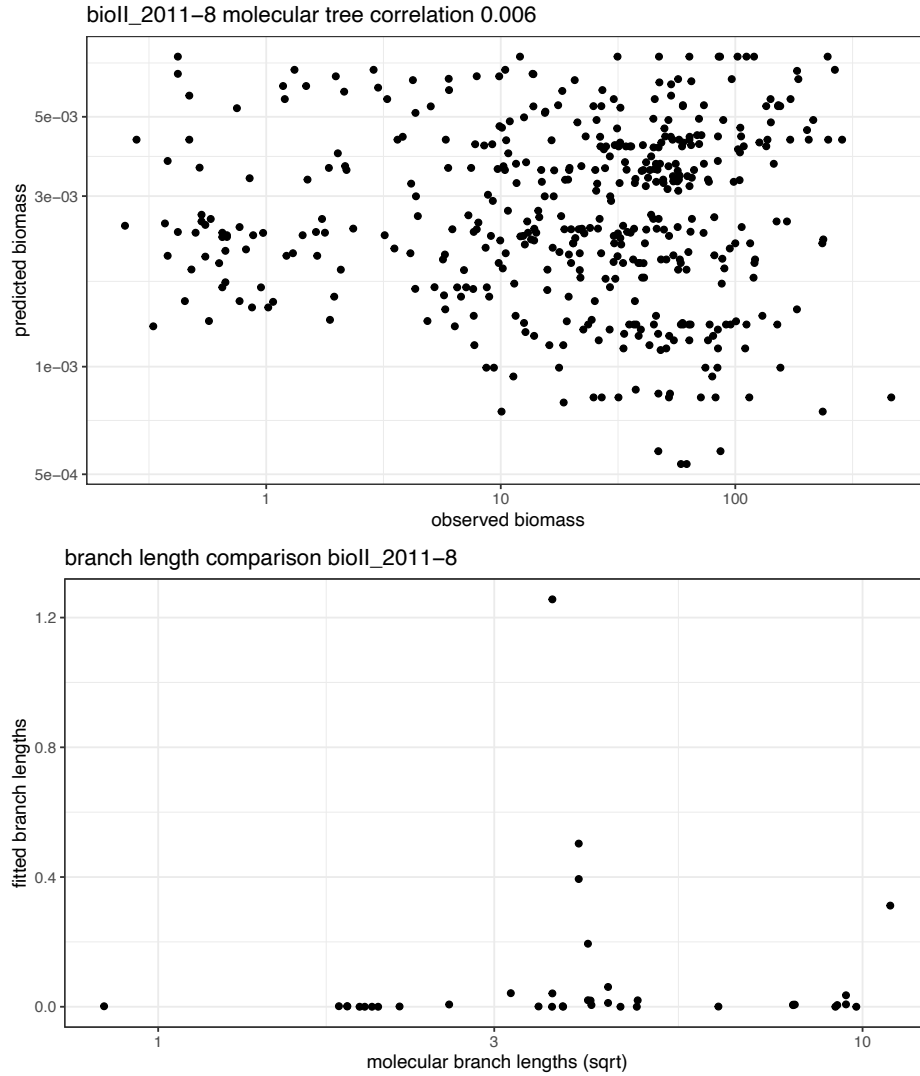


Figure 11: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

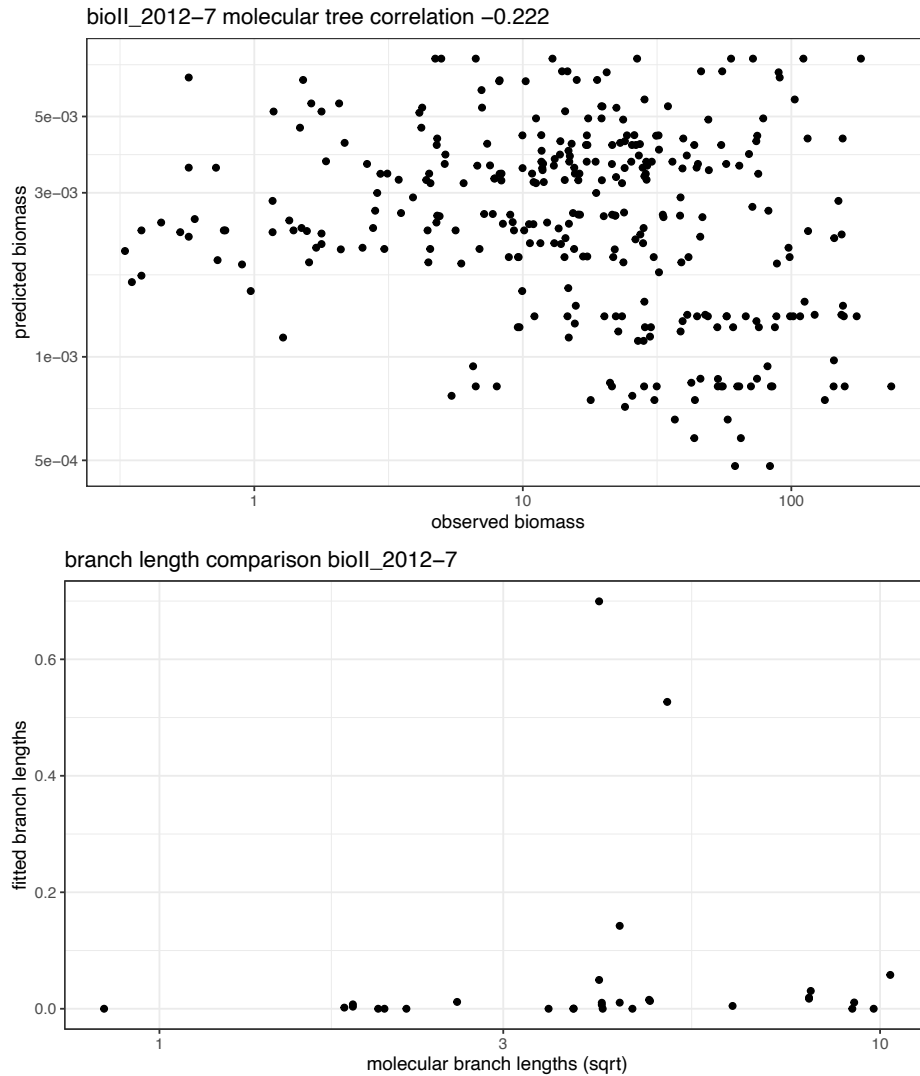


Figure 12: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

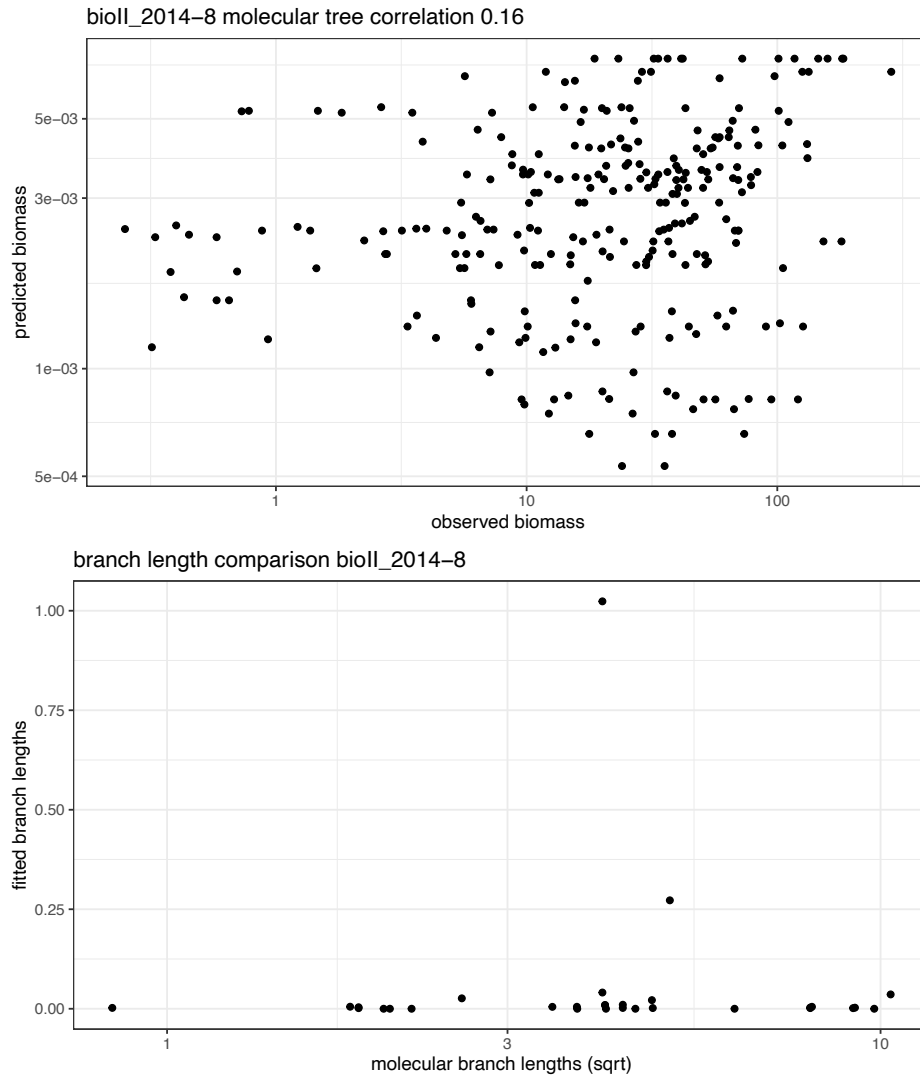


Figure 13: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

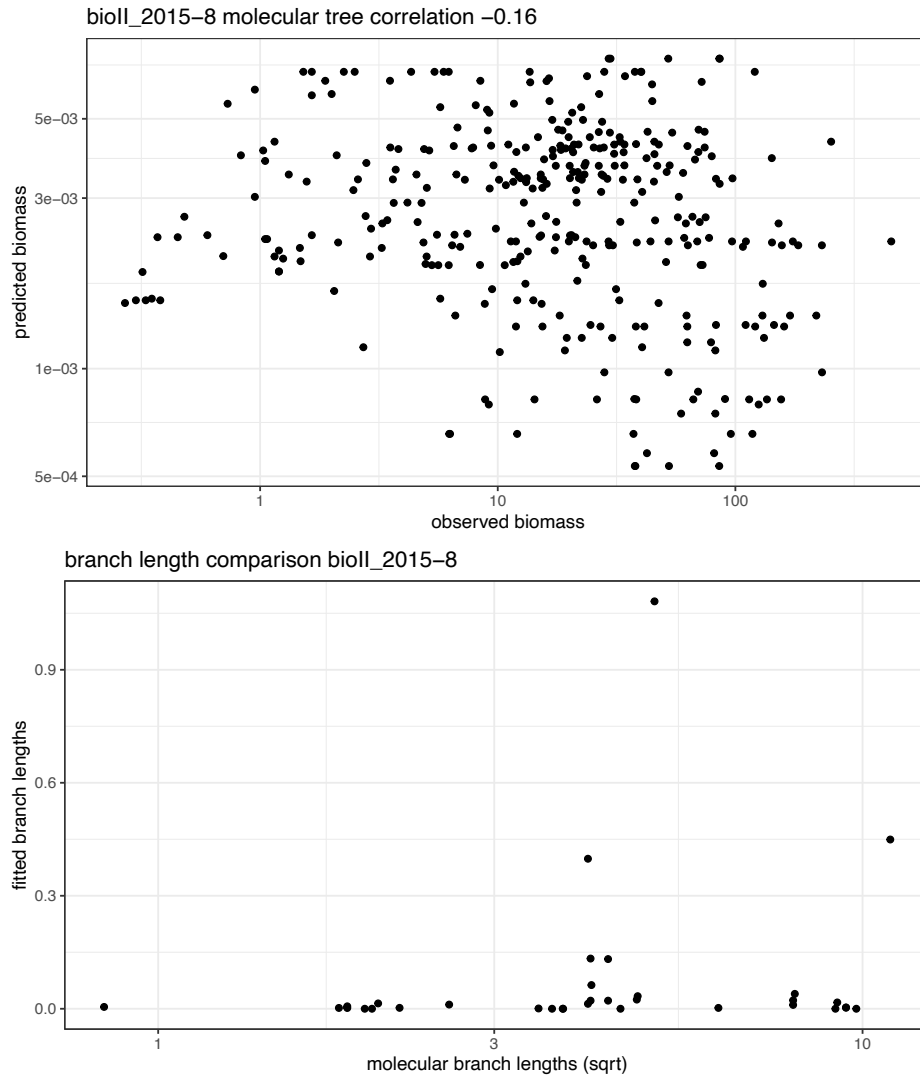


Figure 14: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

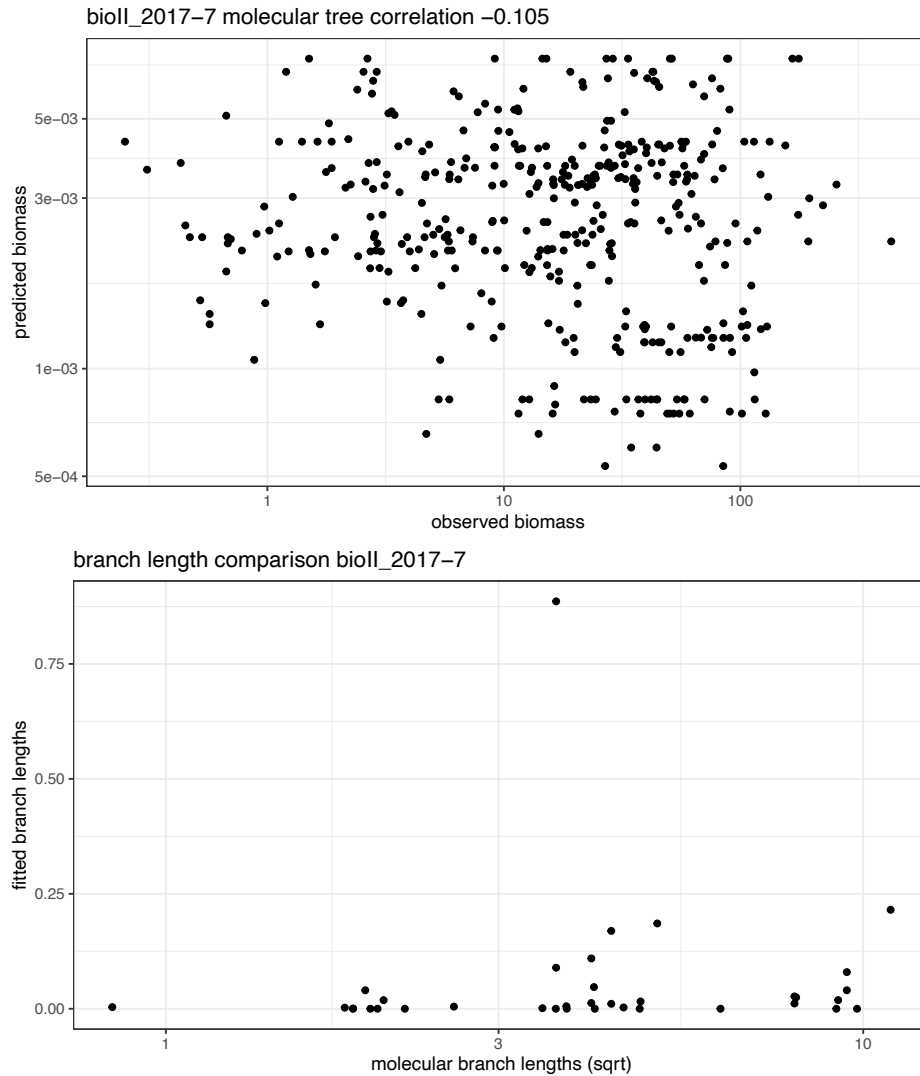


Figure 15: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

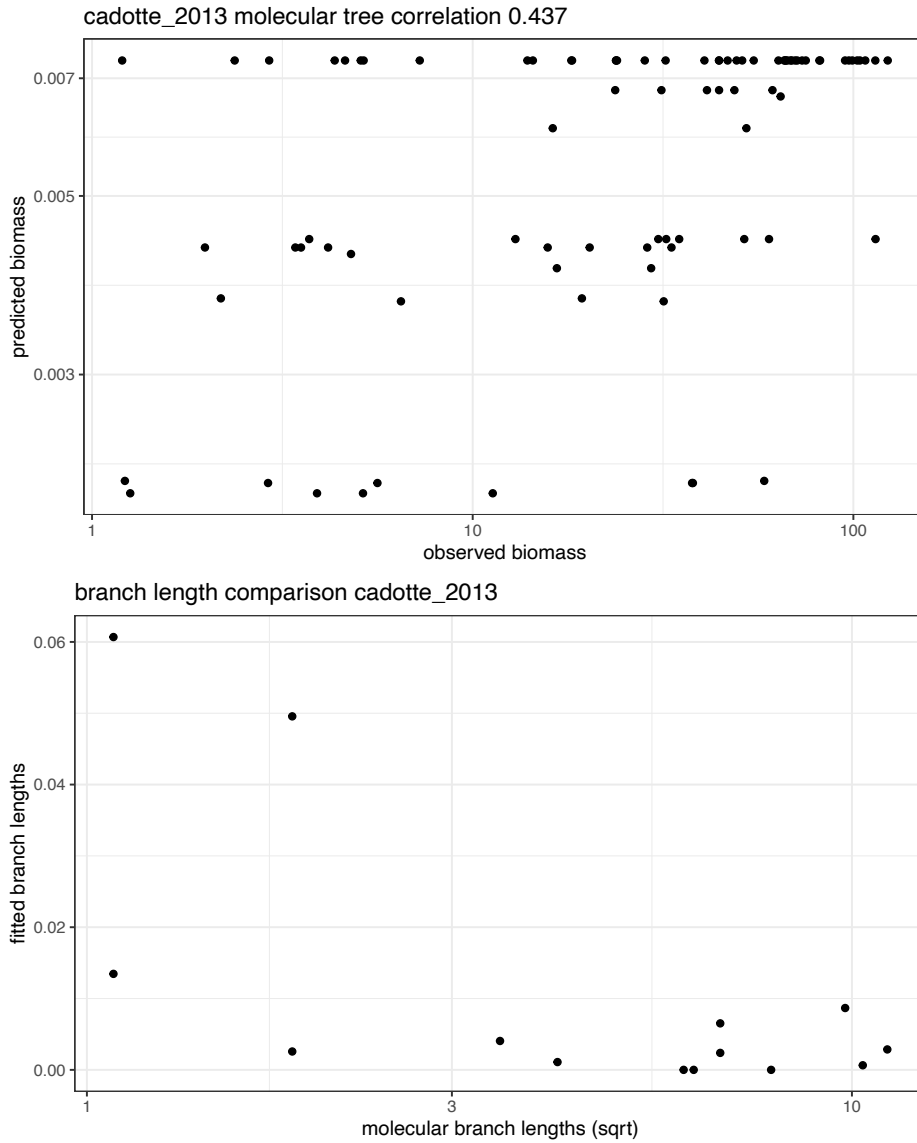


Figure 16: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

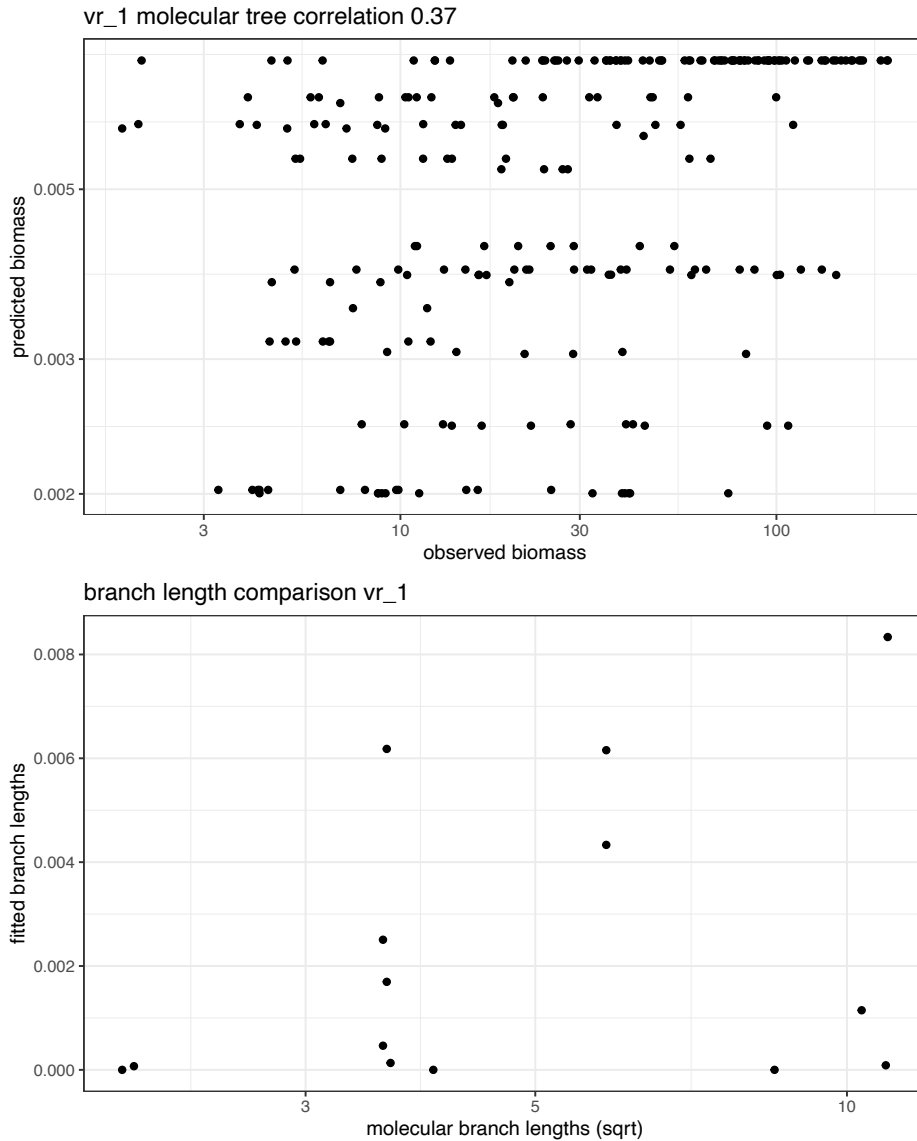


Figure 17: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

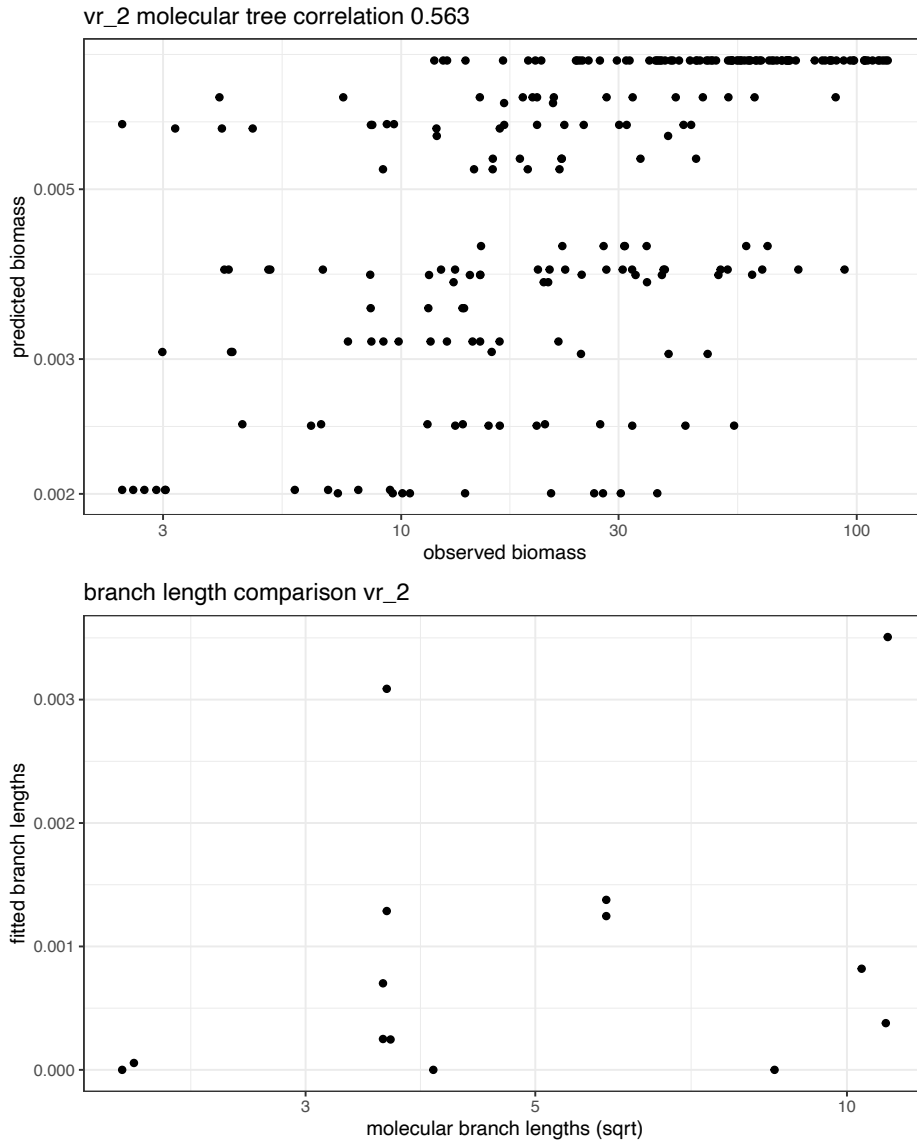


Figure 18: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

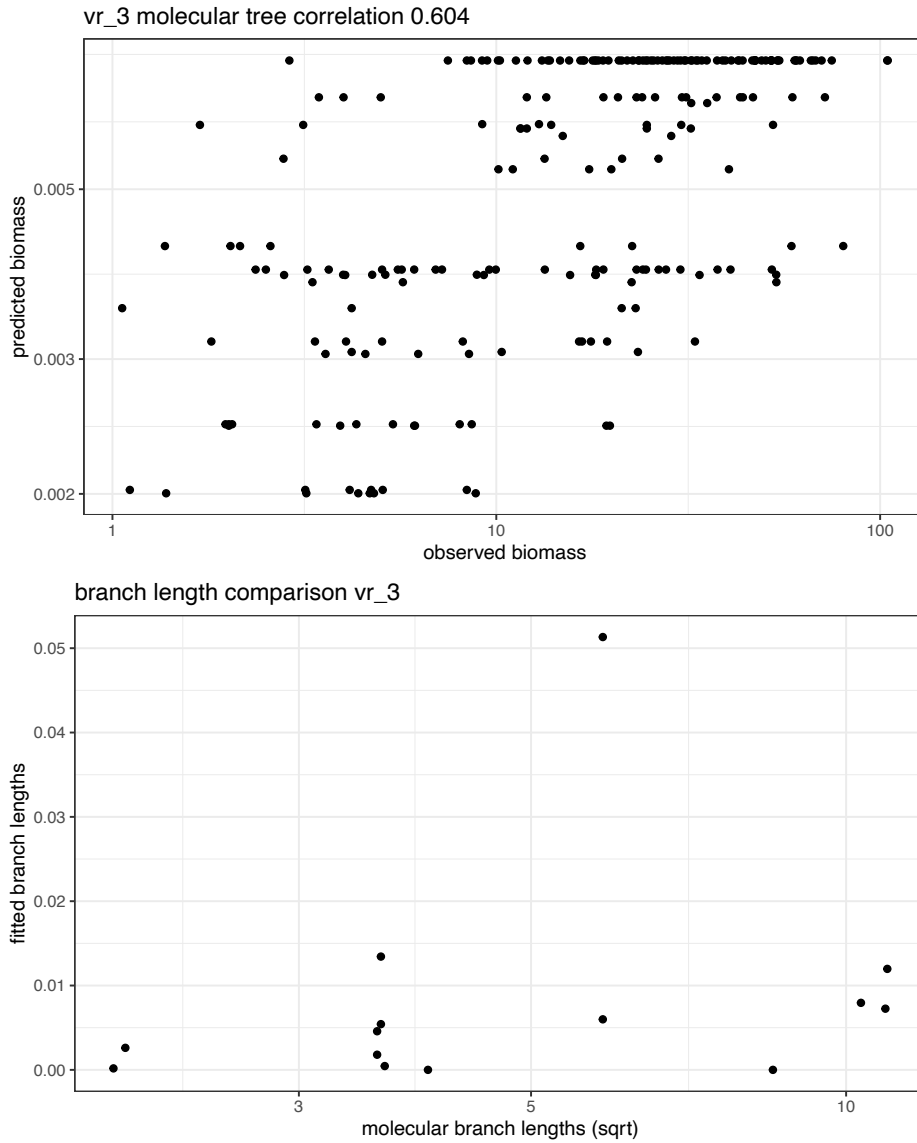


Figure 19: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

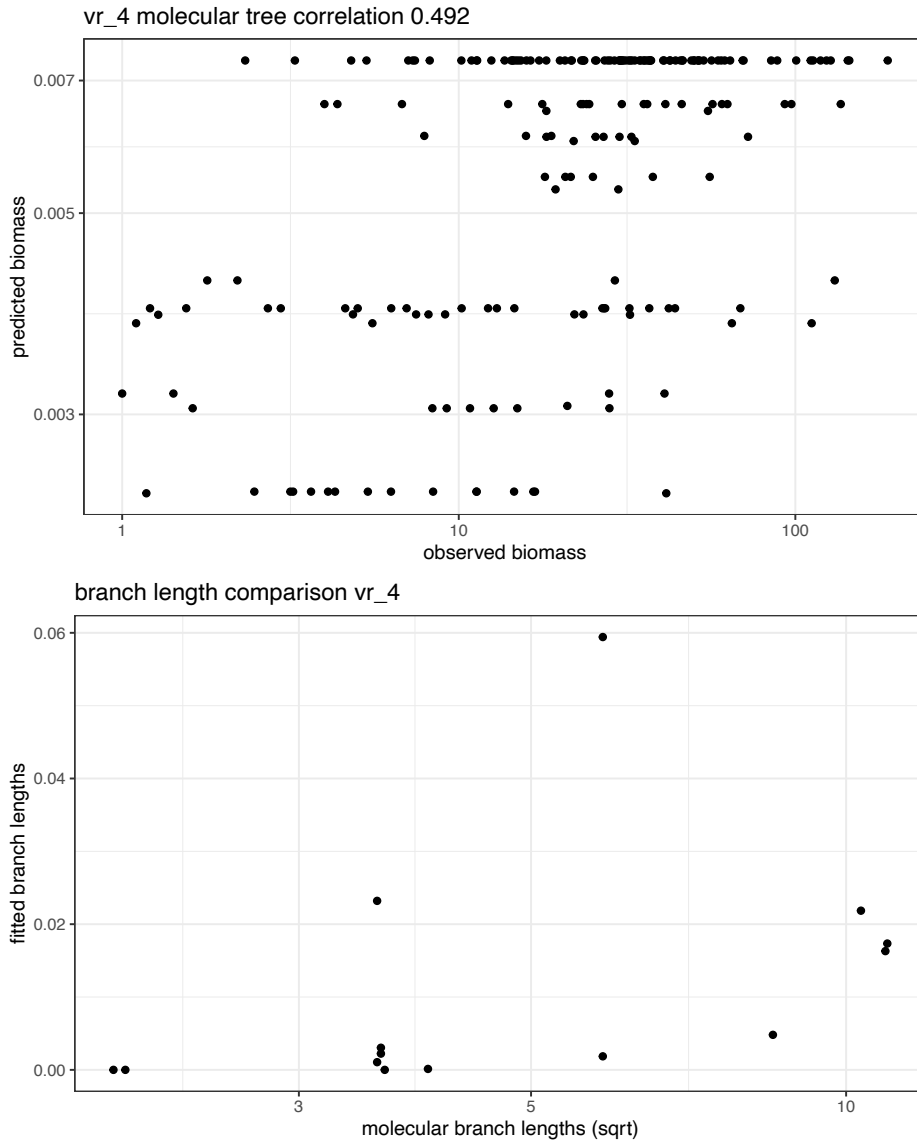


Figure 20: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

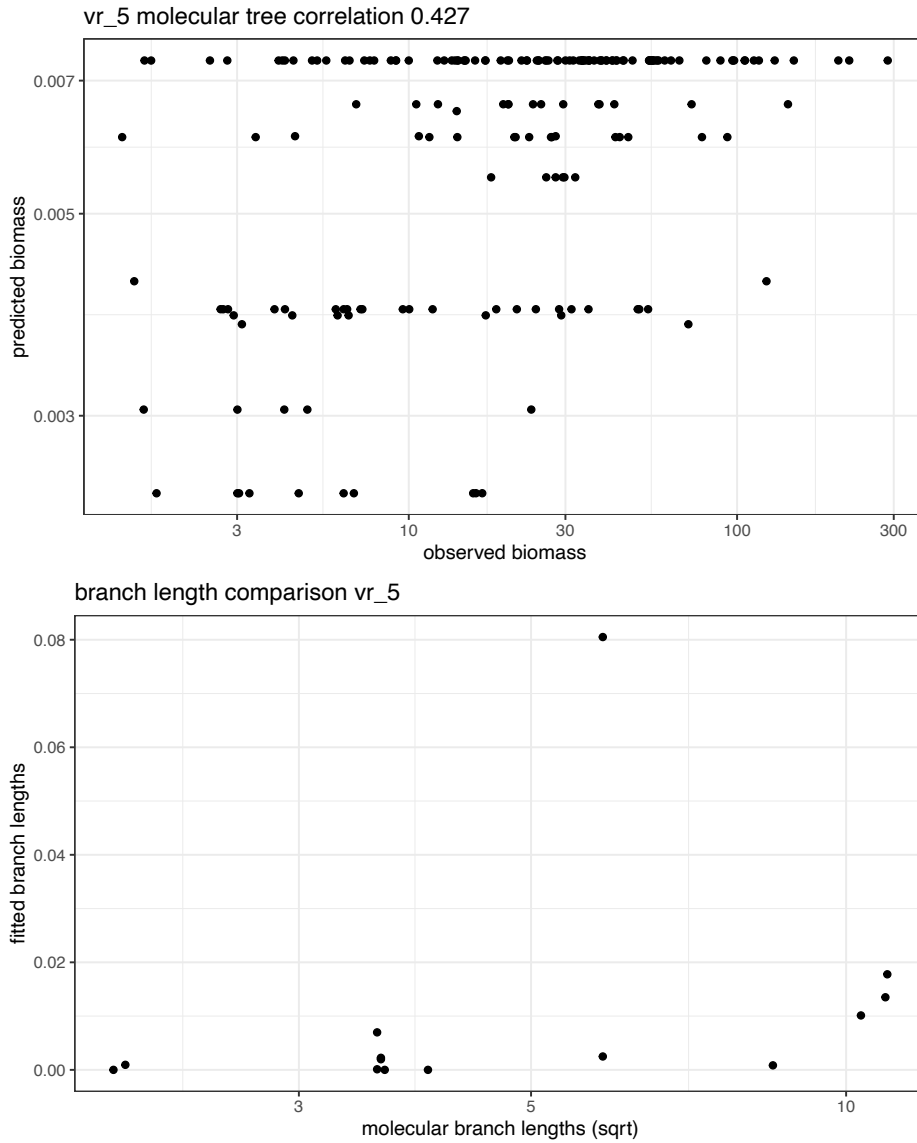


Figure 21: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

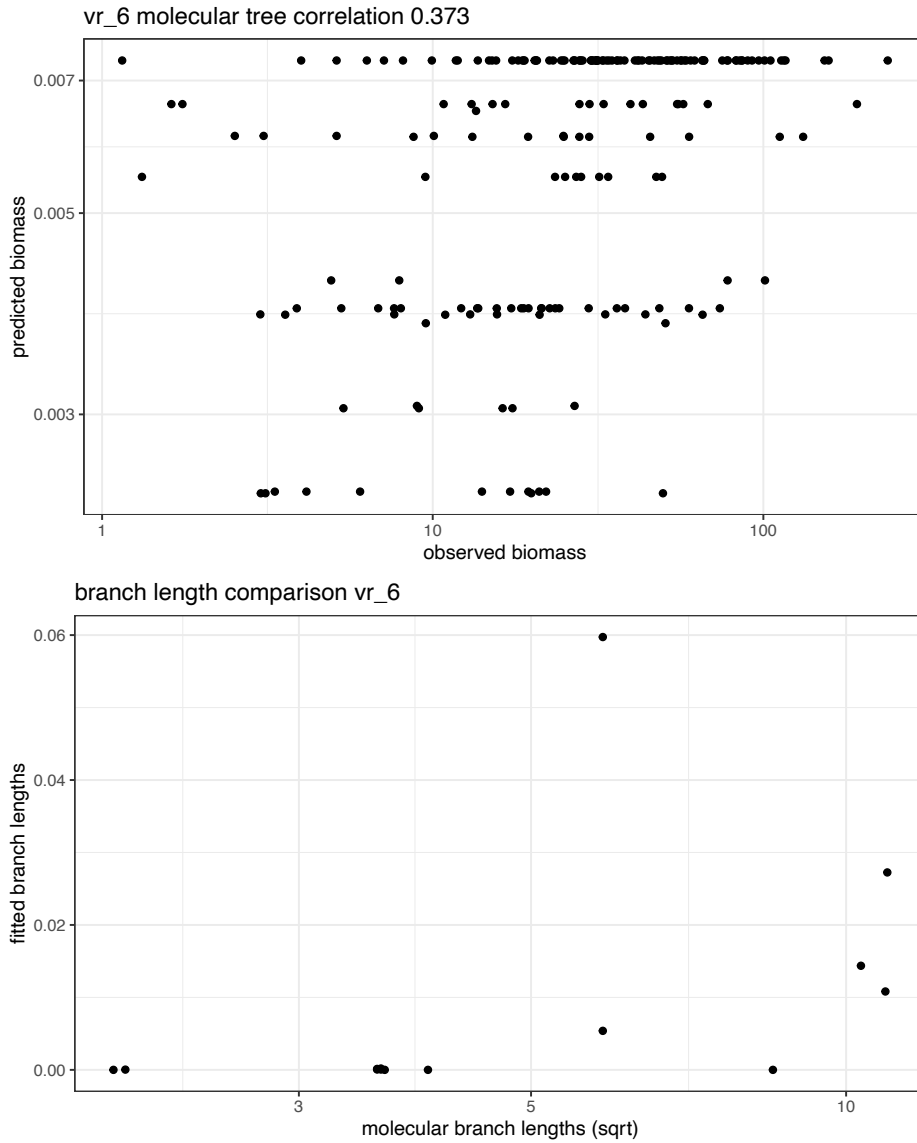


Figure 22: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

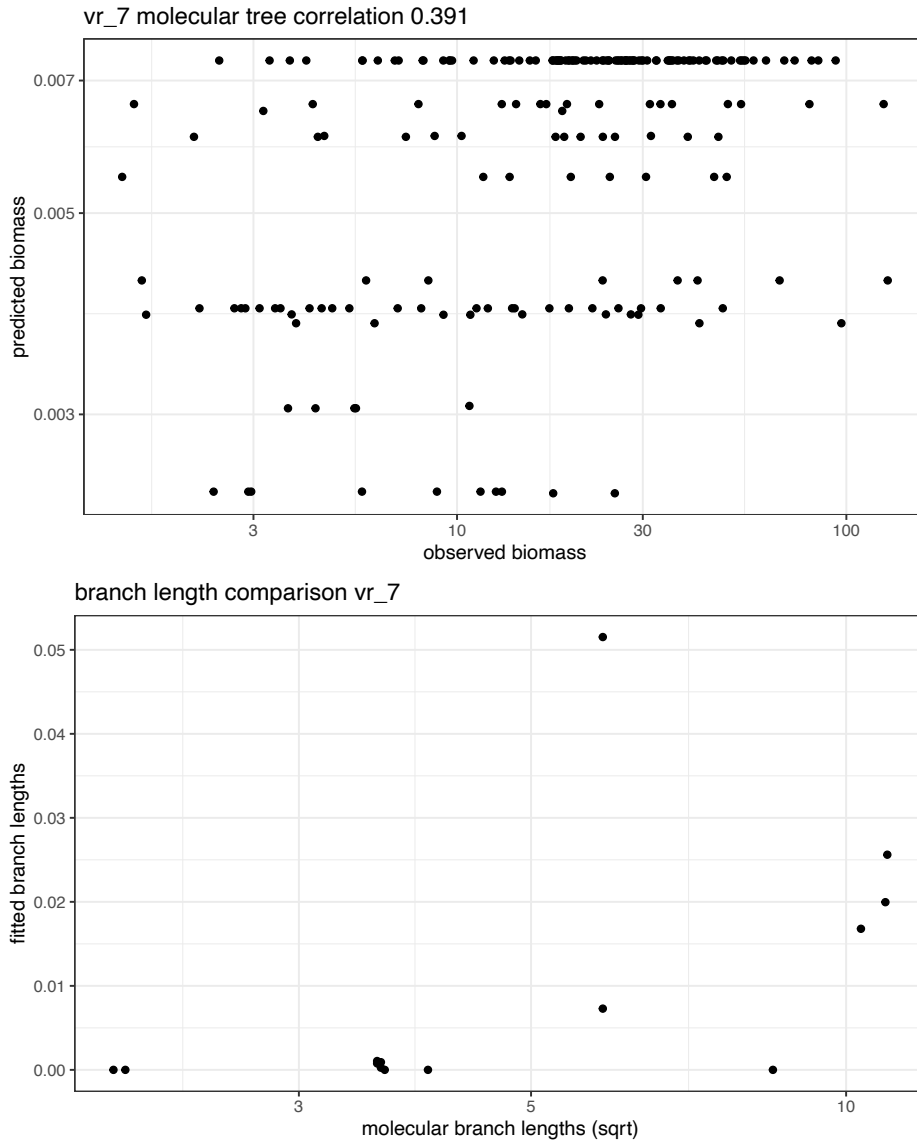


Figure 23: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

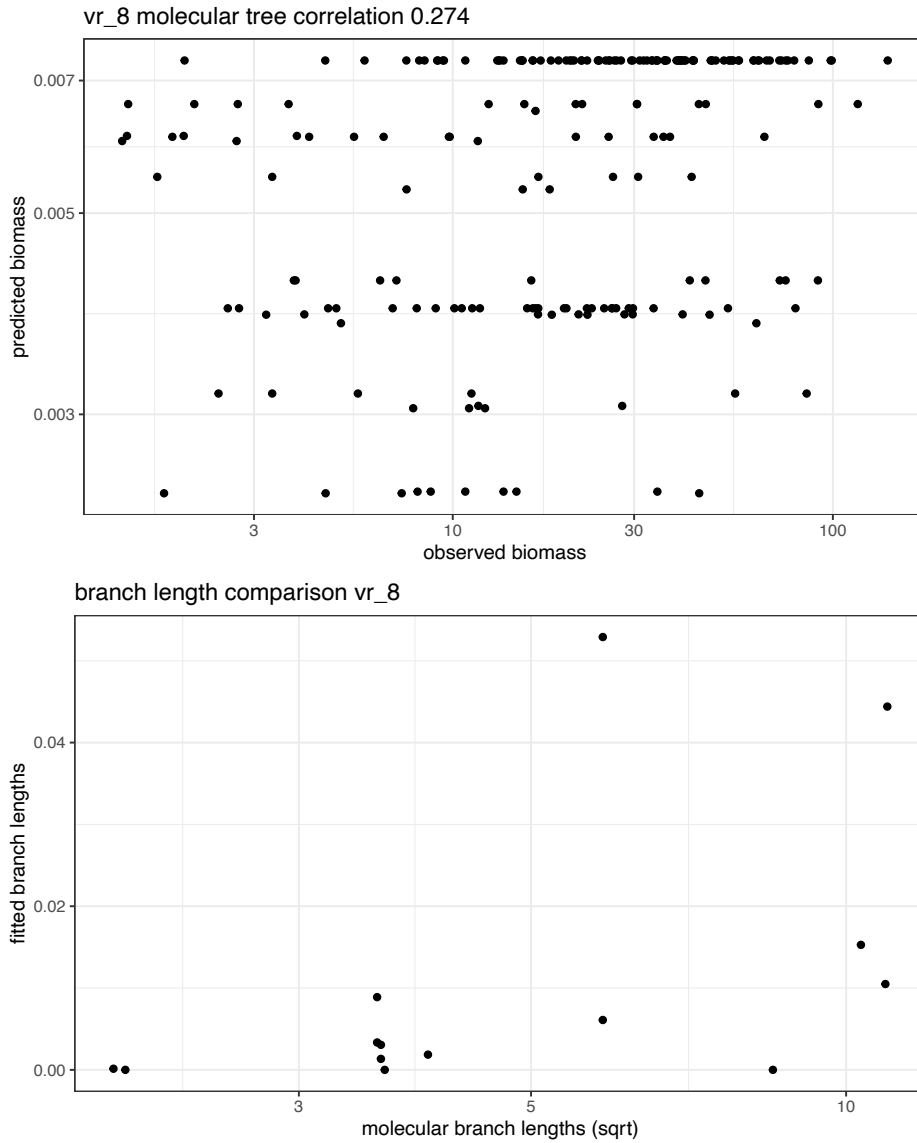


Figure 24: **Model predictions based on molecular branch lengths and comparison between fitted and molecular branch lengths.** Top panel shows predicted biomasses generated by parameterizing the model with the branch lengths from the molecular phylogeny of each data set as a function of the observed biomasses in experimental plots. BOx axes are in log scale and the correlation is estimate between the log of biomasses. The bottom panel shows the relationship between the branch lengths fitted according to our modeling approach as a function of the molecular branch lengths.

## 869 Analysis of previous approaches

870 Previous analysis of BEF data incorporating phylogenetic information to determine the role of phylogeny  
 871 in structuring such experimental communities share two overarching features: a) they typically consider a  
 872 single measurement for the function of each community (e.g., total biomass for each experimental plot, or  
 873 the log-ratio of species abundances in multispecies communities to their abundances in monoculture), and b)  
 874 they employ a statistical approach based on regressing these measurements against phylogenetic diversity or  
 875 dissimilarity (Cadotte *et al.* 2008; Flynn *et al.* 2011; Venail *et al.* 2015). Here we show that by abandoning  
 876 these two features we can perform a strong and principled test for phylogenetic structure in these data,  
 877 and we find that indeed phylogeny structures species’ interactions and thus patterns of coexistence and  
 878 abundance.

879 Traditional approaches used to fit data from Biodiversity-Ecosystem Functioning experiments rely on re-  
 880 gression models that consider the effects of biodiversity, in terms of species richness and composition, and  
 881 some measurement of ecosystem function, such as biomass, carbon fixation, and litter decomposition. These  
 882 models usually consider total biomass of each plot as the response variable, and regress it against the num-  
 883 ber of species or other properties of the plots; for example, they consider a design matrix of zeros and  
 884 ones detailing the presence/absence of each species in a given plot. These models can be supplemented by  
 885 measures of phylogenetic distance between the species, species’ functional groups, species-specific effects,  
 886 pairwise interactions, etc. Because of their underlying structure, these models do not take full advantage of  
 887 the data, which usually report individual biomasses for each species in each plot—these data are aggregated  
 888 when computing the total biomass per plot. These models suffer from three main limitations: (i) the use of  
 889 aggregate data to fit the models when measurements are made at the species-level; (ii) lack of consistency  
 890 with population dynamical models (but see Parain *et al.* 2019); and (iii) underlying assumptions regarding  
 891 the error structure of the statistical models, which are not in accordance with the structure of the data or  
 892 the assumptions of the model. Following the formulation by Connolly *et al.* (2011), a typical regression  
 893 model might have the following structure:

$$y_i = \beta_0 + \sum_{j=1}^S \beta_j P_{ij} + \delta_{AV} \sum_{j < k}^S P_{ij} P_{ik} + \kappa C_{D_i} + \epsilon_i \quad (4)$$

894 where  $y_i$  is a measurement of ecosystem function for plot  $i$  (e.g., total biomass),  $S$  is the total number of  
 895 species considered in the experiment (total species richness),  $\beta_0$  is an intercept,  $\beta_j$  is the effect of species  
 896  $j$  on function in monoculture,  $P_{ij}$  is an indicator variable for the presence (or absence) of species  $j$  in plot  
 897  $i$ ,  $\delta_{AV}$  is the average interaction effect,  $C_{D_i}$  is the phylogenetic diversity in plot  $i$ , computed as  $C_{D_i} =$   
 898  $\sum_{j < k}^S (D_{jk} - \bar{D}) P_j P_k$ , where  $D_{jk}$  is the phylogenetic distance between species  $j$  and  $k$  (accounted as the sum  
 899 of branch lengths between the two species) and  $\bar{D}$  is the average distance of all species in the pool), and  
 900 finally  $\epsilon_i$  is the error term.

901 The amount of data needed to fit such a model can be very large. To examine the performance of this  
 902 kind of regression model, we therefore use simulations where data is generated in agreement with basic  
 903 biological assumptions and test the model with the simulated data. Here we simulate ecological communities  
 904 of competing species following the Generalized Lotka-Volterra dynamics, with the matrix of interactions  
 905 given by the variance-covariance matrix corresponding to a phylogenetic tree. This should be an ideal  
 906 situation for fitting the model, as interactions are constant and strictly pairwise, with a clear phylogenetic  
 907 structure. Starting from a pool of  $n = 10$  species, we assume all species have the same intrinsic growth  
 908 rates, so that dynamics are determined solely by phylogenetic relations. We draw a random tree, construct  
 909 its variance-covariance matrix, assemble all  $2^n - 1 = 1023$  communities that can be formed from the species  
 910 pool and record each species’ biomass in each community. The structure of the matrix of interactions  
 911 can be thought of as emerging from models of trait evolution; for example, if we follow the evolution  
 912 of many trait values, each changing under Brownian motion, this process gives rise to the trait variance-  
 913 covariance matrix which we associated with competition coefficients. In this way, differences in trait values  
 914 are proportional to evolutionary distances (Hansen & Martins 1996; Ives & Helmus 2011). One key aspect

915 of this parameterization is that all sub-communities that can be formed with a subset of species are feasible  
 916 and dynamically stable (see Serván *et al.* 2023 for details).

917 Having produced a large synthetic data set containing more than a thousand “plots”, we can assess the  
 918 quality of fit using a variety of regression models of varying complexity. Model  $M0 : y \sim P$  regresses total  
 919 biomass against the presence/absence of each species ( $P$ ); model  $M1 : y \sim P + C_D$  regresses the total  
 920 biomass against presence/absence of species ( $P$ ) and the phylogenetic distance of species in the plot ( $C_D$ );  
 921  $M2 : y \sim P + C_D + P : C_D$  is the same as  $M1$  but also considers the interaction between presence and  
 922 phylogenetic distance;  $M3 : y \sim P + \sum P_i P_j$  considers the presence absence of each species and their pairwise  
 923 interaction;  $M4 : y \sim P + \sum P_i P_j + C_D$  is the same as  $M3$  adding the phylogenetic distance of each plot; and  
 924 finally  $M5 : y \sim P + \sum P_i P_j + C_D + P : C_D$  is the same as  $m4$  including the interaction between presence  
 925 and phylogenetic distance. Below we show the plots for each of the models, including the predicted versus  
 926 observed biomasses and diagnostic plots from linear regression.

927 These results show that a) none of the models can fully capture the simulated data (despite the lack of  
 928 noise); b) all of the model fits violate some of the main assumptions of linear regressions: residuals are not  
 929 independent and normally distributed, variances are not constant, and thus Quantile-Quantile plots deviate  
 930 substantially from the 1:1 line. We conclude that these model structures are not adequate to capture models  
 931 for population dynamics—generalizing beyond competition, choosing more complex models for population  
 932 dynamics, or introducing stochasticity and measurement error can only worsen the fit.

933 The inadequacy of regression-based approaches motivates our alternative methodology for inferring phyloge-  
 934 netic structure in these data.

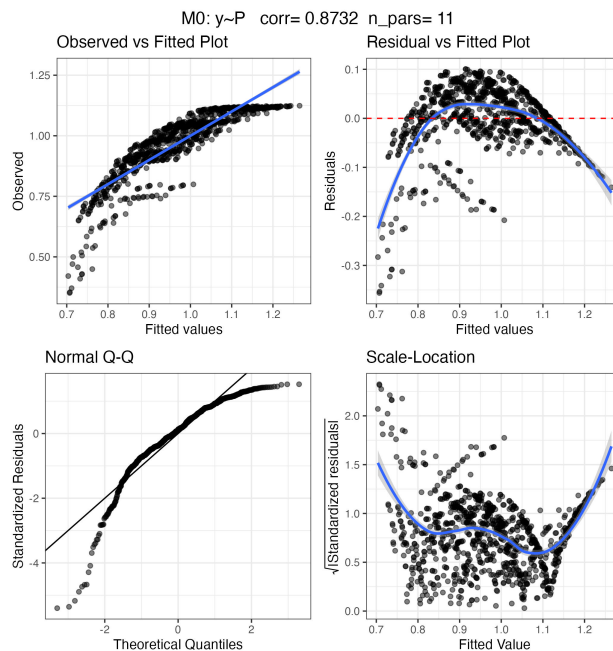


Figure 25: Fitting regression models to simulated data from a phylogenetically-structured Generalized Lotka-Volterra model. Each figure reports the structure of the model (top) as well as scatter-plots showing the relationship between observed and fitted total biomasses per plot; corresponding distribution of standardized residuals (for linear regression, these should be centered at zero and have the same variance irrespective of the fitted values); Quantile-Quantile plots (points should fall on the 1 to 1 line); scale location plots, showing whether residuals change with the input (they should form a horizontal band of points).

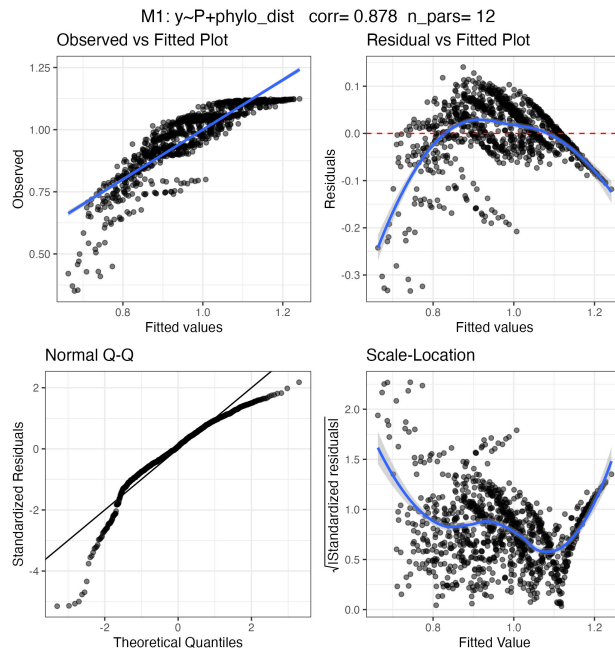


Figure 26: Fitting regression models to simulated data from a phylogenetically-structured Generalized Lotka-Volterra model. Each figure reports the structure of the model (top) as well as scatter-plots showing the relationship between observed and fitted total biomasses per plot; corresponding distribution of standardized residuals (for linear regression, these should be centered at zero and have the same variance irrespective of the fitted values); Quantile-Quantile plots (points should fall on the 1 to 1 line); scale location plots, showing whether residuals change with the input (they should form a horizontal band of points).

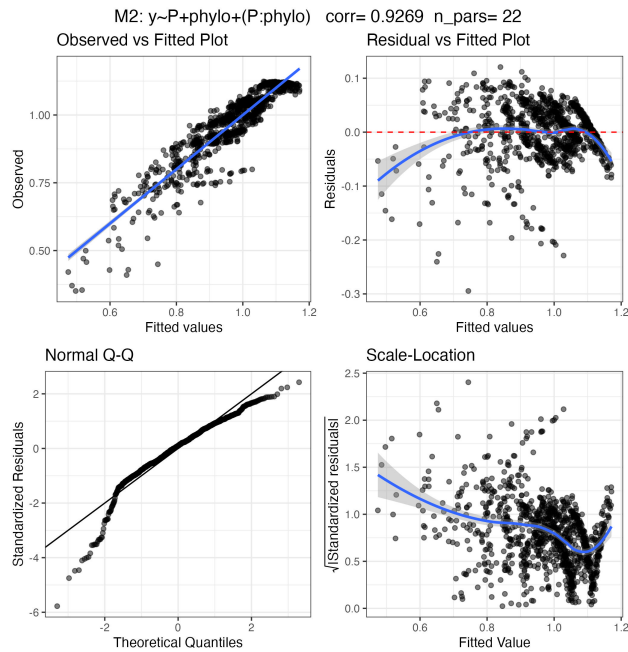


Figure 27: Fitting regression models to simulated data from a phylogenetically-structured Generalized Lotka-Volterra model. Each figure reports the structure of the model (top) as well as scatter-plots showing the relationship between observed and fitted total biomasses per plot; corresponding distribution of standardized residuals (for linear regression, these should be centered at zero and have the same variance irrespective of the fitted values); Quantile-Quantile plots (points should fall on the 1 to 1 line); scale location plots, showing whether residuals change with the input (they should form a horizontal band of points).

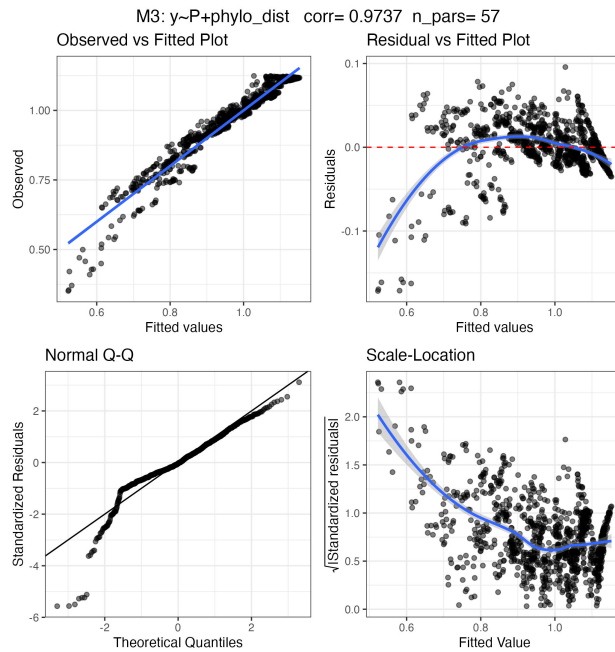


Figure 28: Fitting regression models to simulated data from a phylogenetically-structured Generalized Lotka-Volterra model. Each figure reports the structure of the model (top) as well as scatter-plots showing the relationship between observed and fitted total biomasses per plot; corresponding distribution of standardized residuals (for linear regression, these should be centered at zero and have the same variance irrespective of the fitted values); Quantile-Quantile plots (points should fall on the 1 to 1 line); scale location plots, showing whether residuals change with the input (they should form a horizontal band of points).

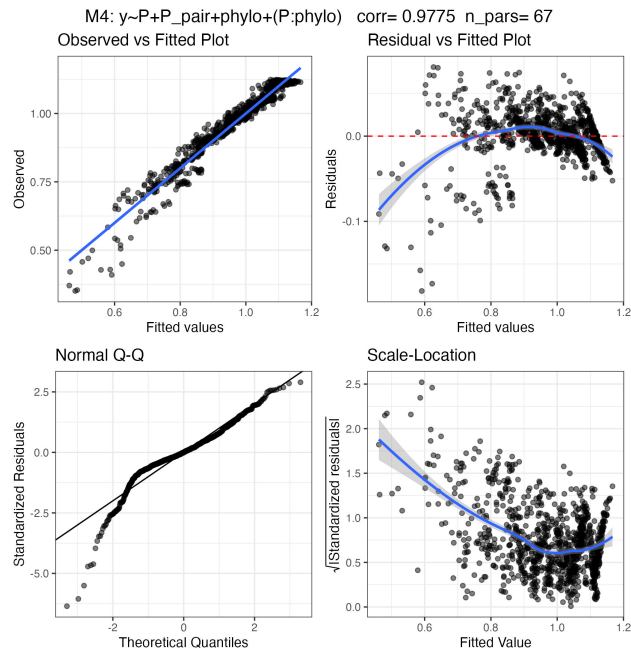


Figure 29: Fitting regression models to simulated data from a phylogenetically-structured Generalized Lotka-Volterra model. Each figure reports the structure of the model (top) as well as scatter-plots showing the relationship between observed and fitted total biomasses per plot; corresponding distribution of standardized residuals (for linear regression, these should be centered at zero and have the same variance irrespective of the fitted values); Quantile-Quantile plots (points should fall on the 1 to 1 line); scale location plots, showing whether residuals change with the input (they should form a horizontal band of points).

935 **Full results**

936 The results for all model formulations and each data set are reported in Table 2. Scatter-plots for the  
 937 data stemming from the Biodiversity II and the Wageningen experiments are reported in Figure 30 and  
 938 Figure 32, respectively. Histograms of the likelihoods for the randomized trees are reported in Figure 31  
 939 and Figure 33. The fitted trees and associated likelihood boxplots for randomizations stratified by selected  
 940 clades are reported in Figure 34 - Figure 41 for the Biodiversity II experiment and Figure 42 - Figure 49 for  
 941 the Wageningen experiment. Finally, the fits for models 2-4 with the associated tree and vectors are also in  
 942 Figures 50-68.

Table 2: For each data set (Bio II, from Tilman et al. (2001); Cadotte, from Cadotte (2013); Wag, from Van Ruijven and Berendse (2010)), we report the number of species ( $n_{sp}$ ); the number of unique assemblages ( $n_{comm}$ ); the total number of measurements ( $n_{meas}$ ); the model used to fit the data; the corresponding log-likelihood (logLik); the total number of parameters ( $n_{par}$ ); the p-values for randomized trees either produced by the Yule model ( $p_{rnd}$ ) or by shuffling the species' identities ( $p_{shuffle}$ ); and the correlation between the logarithms of the observed and predicted biomasses (cor). P-values below 0.05 are bolded.

data set	$n_{sp}$	$n_{comm}$	$n_{meas}$	model	logLik	$n_{par}$	$P_{rnd}$	$P_{shuffle}$	cor
Bio II 6/01	13	28	142	1	-515.125	26	<b>0.011</b>	<b>0.006</b>	0.916
				2	-506.803	38	<b>0.001</b>	<b>0.004</b>	0.924
				3	-510.384	38	0.606	0.612	0.923
				4	-496.525	50	0.153	0.137	0.936
Bio II 7/06	20	63	416	1	-1 562.862	40	<b>0.032</b>	<b>0.034</b>	0.848
				2	-1 543.540	59	<b>0.028</b>	<b>0.032</b>	0.857
				3	-1 548.530	59	<b>0.013</b>	<b>0.028</b>	0.856
				4	-1 528.100	78	<b>0.001</b>	<b>0.007</b>	0.866
Bio II 8/07	20	69	445	1	-1 829.444	40	<b>0.017</b>	<b>0.014</b>	0.829
				2	-1 810.571	59	<b>0.020</b>	<b>0.018</b>	0.842
				3	-1 816.684	59	<b>0.033</b>	0.056	0.840
				4	-1 791.473	78	<b>0.049</b>	<b>0.041</b>	0.852
Bio II 7/08	17	33	247	1	-1 019.927	34	<b>0.008</b>	<b>0.008</b>	0.833
				2	-1 005.384	50	<b>0.045</b>	<b>0.049</b>	0.848
				3	-1 014.225	50	<b>0.030</b>	<b>0.024</b>	0.842
				4	-989.244	66	<b>0.014</b>	<b>0.008</b>	0.854
Bio II 8/11	20	59	451	1	-1 872.468	40	0.147	0.188	0.865
				2	-1 851.060	59	<b>0.037</b>	<b>0.033</b>	0.876
				3	-1 845.121	59	<b>0.002</b>	<b>0.005</b>	0.880
				4	-1 822.608	78	<b>0.000</b>	<b>0.000</b>	0.888
Bio II 7/12	16	40	322	1	-1 265.636	32	0.253	0.261	0.814
				2	-1 257.352	47	0.141	0.118	0.821
				3	-1 256.901	47	0.193	0.216	0.822
				4	-1 239.699	62	<b>0.009</b>	<b>0.009</b>	0.843

data set	n <sub>sp</sub>	n <sub>comm</sub>	n <sub>meas</sub>	model	logLik	n <sub>par</sub>	P <sub>rnd</sub>	P <sub>shuffle</sub>	cor
Bio II 8/14	16	39	271	1	-1 100.731	32	<b>0.000</b>	<b>0.001</b>	0.832
				2	-1 089.324	47	<b>0.027</b>	<b>0.019</b>	0.844
				3	-1 093.747	47	<b>0.006</b>	<b>0.003</b>	0.838
				4	-1 077.425	62	<b>0.012</b>	<b>0.013</b>	0.856
Bio II 8/15	18	43	337	1	-1 344.643	36	<b>0.005</b>	<b>0.012</b>	0.830
				2	-1 335.333	53	<b>0.002</b>	<b>0.004</b>	0.835
				3	-1 333.390	53	<b>0.027</b>	<b>0.028</b>	0.840
				4	-1 315.121	70	<b>0.004</b>	<b>0.009</b>	0.854
Bio II 7/17	19	53	409	1	-1 599.741	38	<b>0.001</b>	<b>0.001</b>	0.841
				2	-1 587.881	56	<b>0.011</b>	<b>0.014</b>	0.850
				3	-1 580.571	56	<b>0.002</b>	<b>0.000</b>	0.851
				4	-1 562.737	74	<b>0.001</b>	<b>0.000</b>	0.863
Cadotte	8	27	87	1	-348.372	16	<b>0.027</b>	<b>0.029</b>	0.878
				2	-344.637	23	0.131	0.132	0.890
				3	-345.628	23	0.512	0.507	0.881
				4	-342.545	30	0.696	0.711	0.891
Wag 00	8	58	235	1	-856.445	16	0.419	0.378	0.948
				2	-850.295	23	0.456	0.435	0.951
				3	-823.108	23	0.246	0.248	0.960
				4	-817.592	30	0.260	0.297	0.962
Wag 01	8	58	231	1	-815.679	16	<b>0.001</b>	<b>0.001</b>	0.933
				2	-811.568	23	0.103	0.115	0.935
				3	-786.491	23	<b>0.000</b>	<b>0.001</b>	0.948
				4	-780.650	30	0.071	0.066	0.950
Wag 02	8	56	222	1	-770.436	16	0.067	0.066	0.858
				2	-756.722	23	<b>0.040</b>	<b>0.024</b>	0.879
				3	-754.152	23	0.068	0.071	0.877
				4	-726.884	30	<b>0.003</b>	<b>0.003</b>	0.908
Wag 03	8	51	196	1	-754.342	16	<b>0.043</b>	<b>0.043</b>	0.849
				2	-737.109	23	<b>0.036</b>	<b>0.018</b>	0.873
				3	-731.931	23	0.076	<b>0.027</b>	0.880
				4	-713.488	30	<b>0.030</b>	<b>0.028</b>	0.903
Wag 04	8	53	184	1	-731.749	16	0.145	0.140	0.796
				2	-721.201	23	0.115	0.088	0.823
				3	-699.034	23	<b>0.005</b>	<b>0.003</b>	0.853

data set	n <sub>sp</sub>	n <sub>comm</sub>	n <sub>meas</sub>	model	logLik	n <sub>par</sub>	P <sub>rnd</sub>	P <sub>shuffle</sub>	cor
				4	-690.901	30	0.214	0.215	0.871
Wag 05	8	53	197	1	-816.254	16	0.060	<b>0.049</b>	0.766
				2	-807.928	23	0.125	0.071	0.786
				3	-804.602	23	<b>0.028</b>	<b>0.020</b>	0.802
				4	-792.838	30	0.380	0.387	0.820
Wag 06	8	54	197	1	-746.003	16	0.106	0.104	0.721
				2	-740.846	23	0.239	0.243	0.741
				3	-720.442	23	<b>0.028</b>	<b>0.028</b>	0.790
				4	-714.023	30	0.166	0.166	0.803
Wag 07	8	55	206	1	-808.122	16	<b>0.023</b>	<b>0.032</b>	0.769
				2	-799.968	23	0.148	0.152	0.788
				3	-791.224	23	<b>0.036</b>	0.075	0.807
				4	-786.148	30	0.080	0.077	0.809
Wag 08	8	54	210	1	-803.785	16	0.278	0.282	0.780
				2	-792.913	23	0.986	0.961	0.797
				3	-794.166	23	0.236	0.271	0.799
				4	-779.235	30	1.000	1.000	0.822

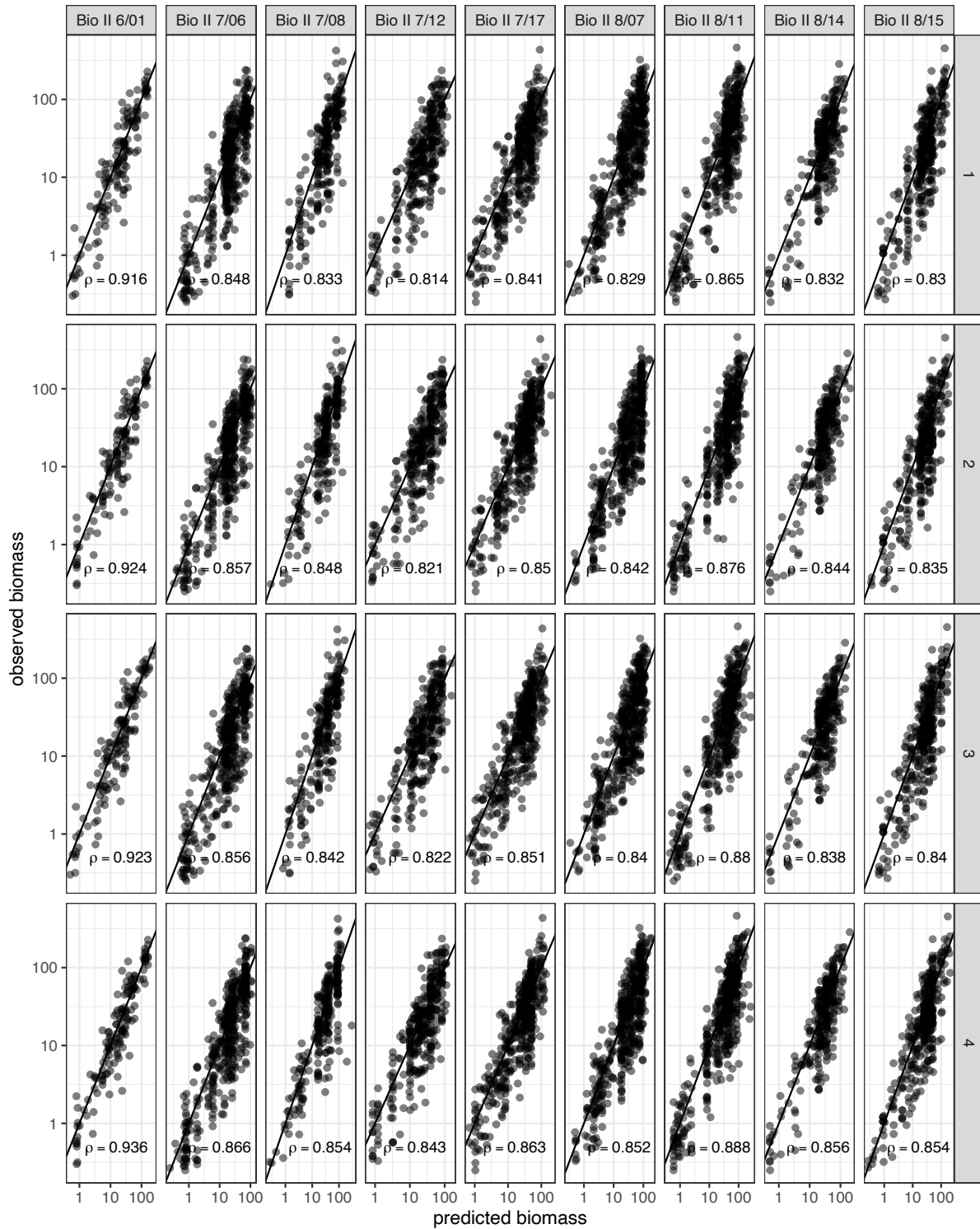


Figure 30: Scatterplot of predicted vs. observed biomass for the Biodiversity II data. Each panel represents a specific sampling date and model. The correlation between the logarithm of the observed biomass and the logarithm of the predicted biomass is reported in each panel.

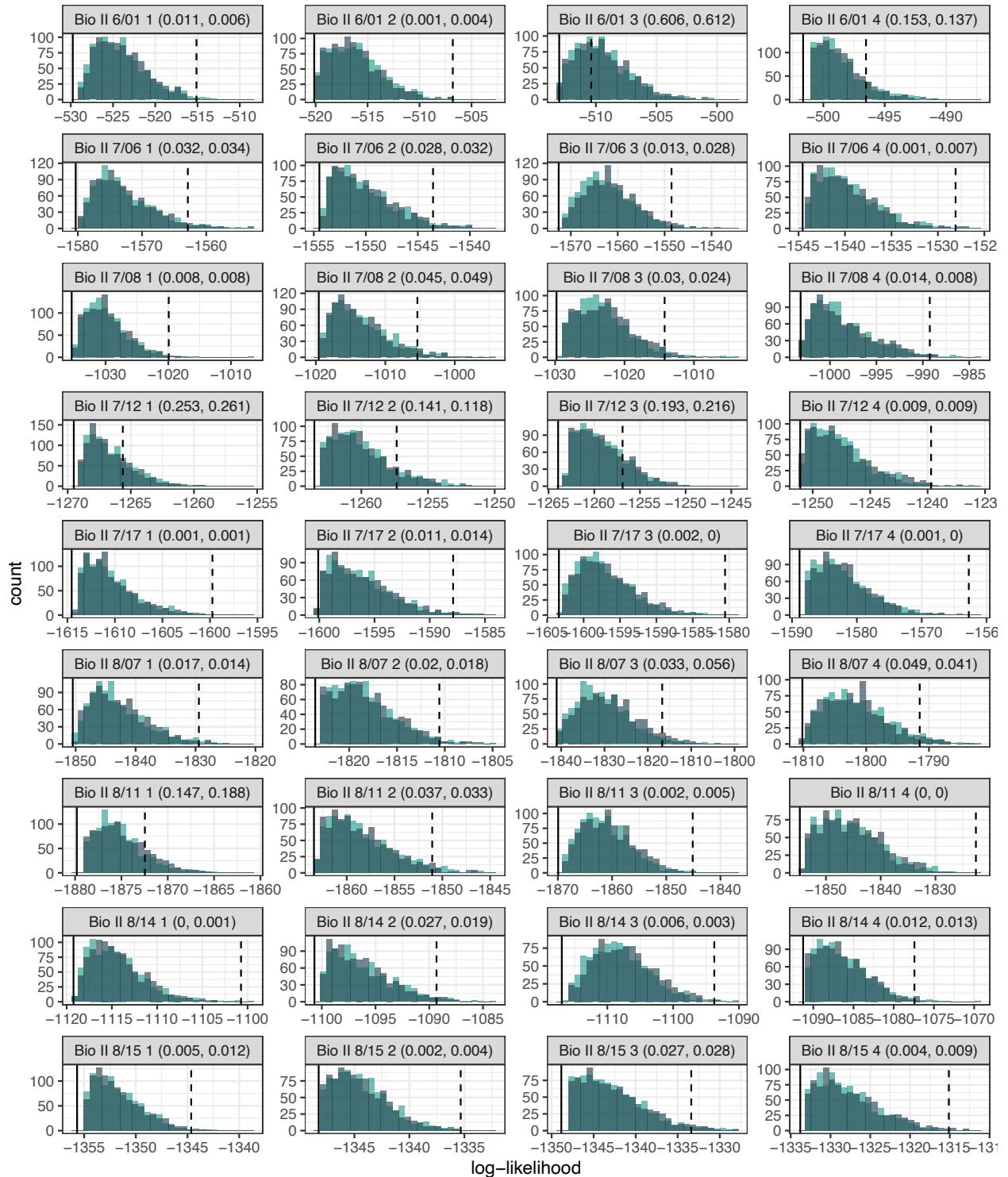


Figure 31: Histograms of the log-likelihoods for models parameterized using random trees and data from the Biodiversity II experiment. The distributions for the random trees generated by the Yule model are in teal, and those for the shuffled trees in grey. Each panel reports the p-values obtained for the Yule and shuffled trees, respectively.



Figure 32: Scatterplot of predicted vs. observed biomass for the Wageningen biodiversity experiment data. Each panel represents a specific sampling date and model. The correlation between the logarithm of the observed biomass and the logarithm of the predicted biomass is reported in each panel.

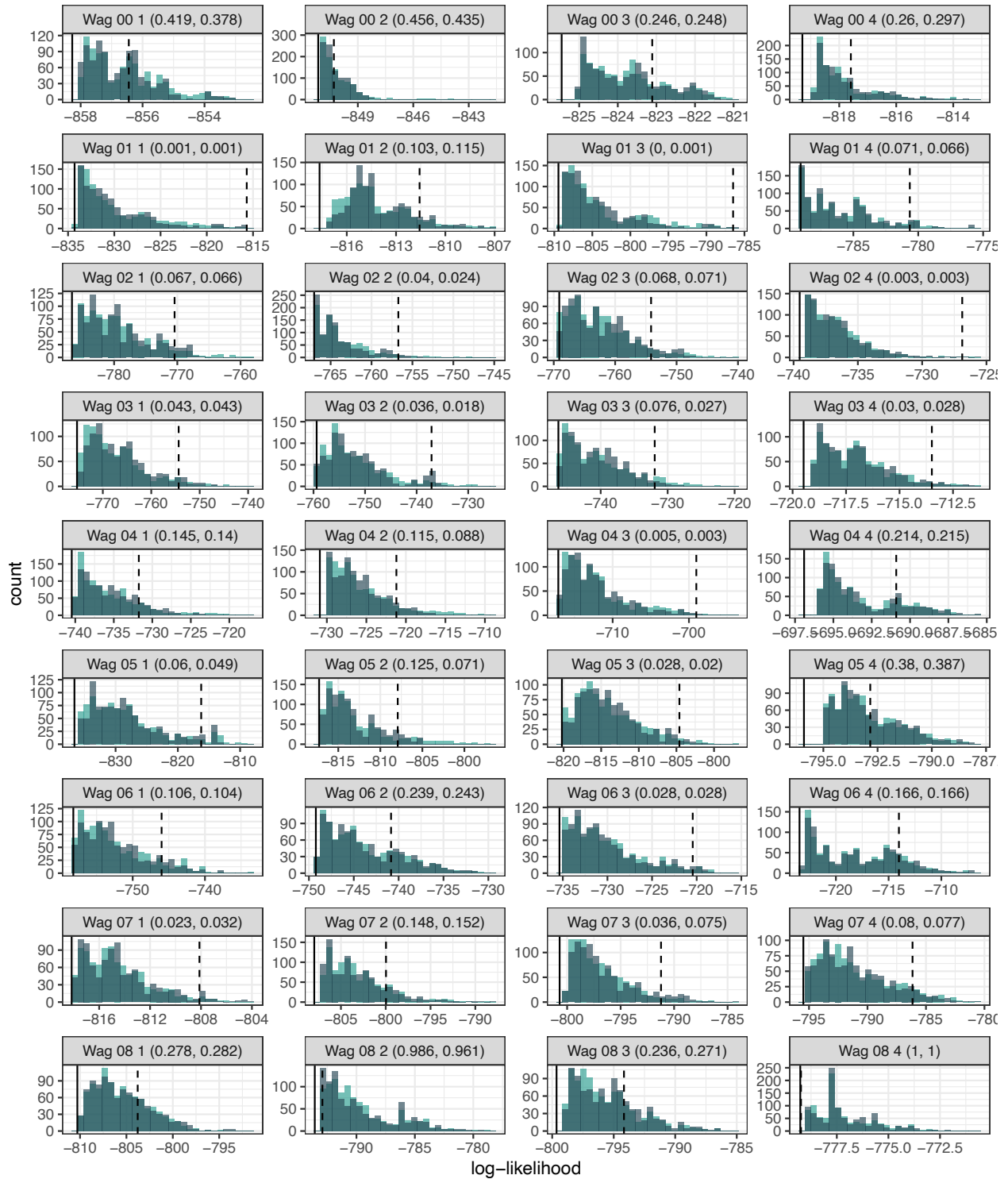


Figure 33: Histograms of the log-likelihoods for models parameterized using random trees and data from the Wageningen diversity experiment. The distributions for the random trees generated by the Yule model are in teal, and those for the shuffled trees in grey. Each panel reports the p-values obtained for the Yule and shuffled trees, respectively.

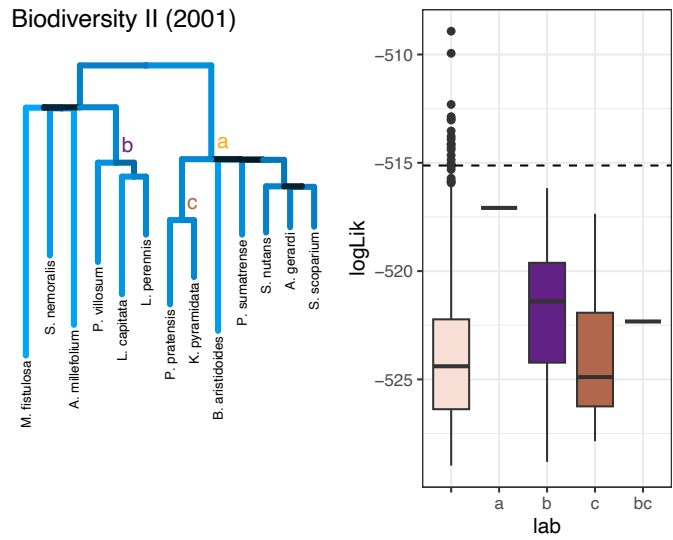


Figure 34: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

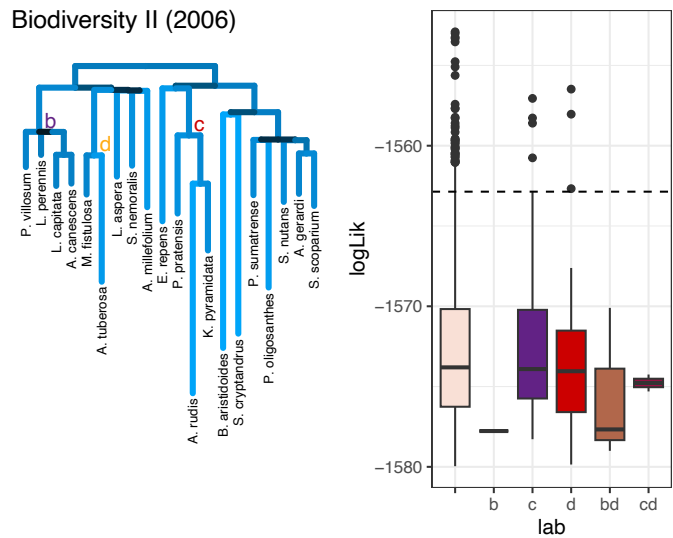


Figure 35: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

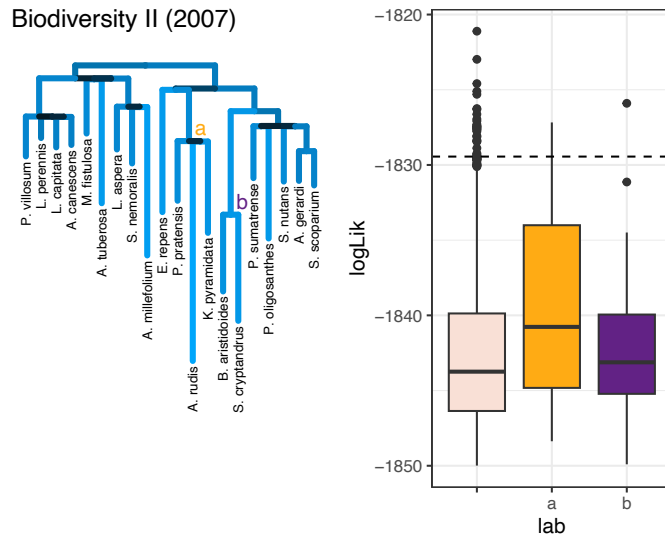


Figure 36: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

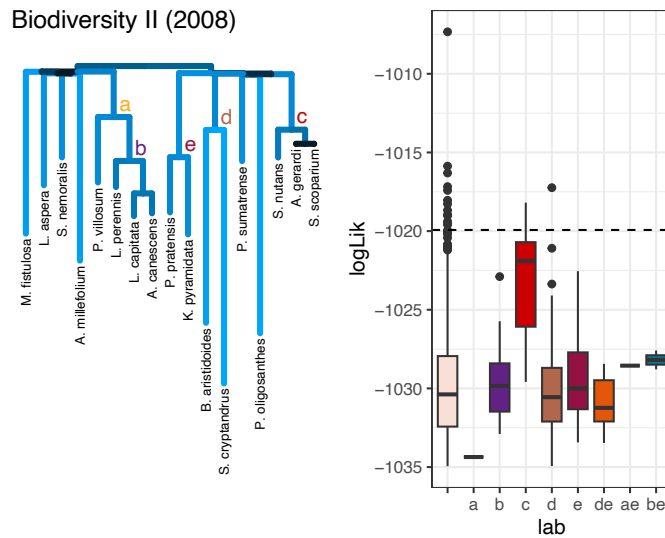


Figure 37: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

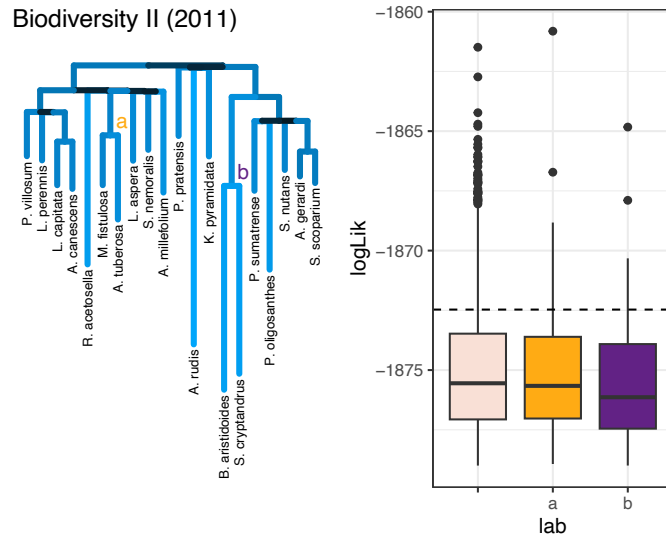


Figure 38: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

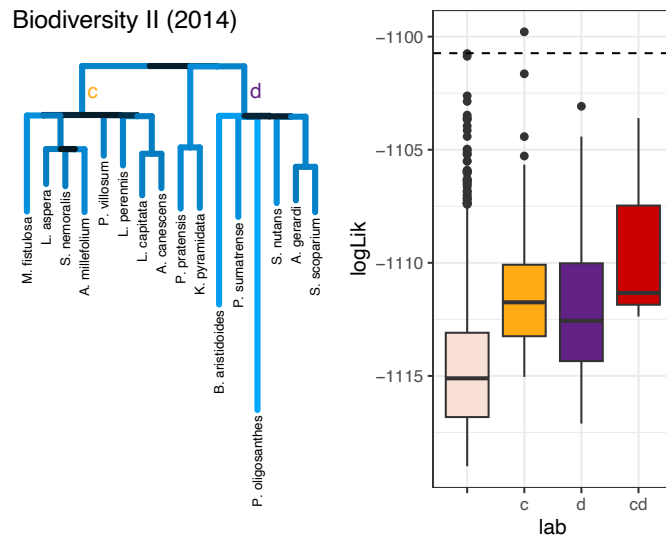


Figure 39: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

Biodiversity II (2015)

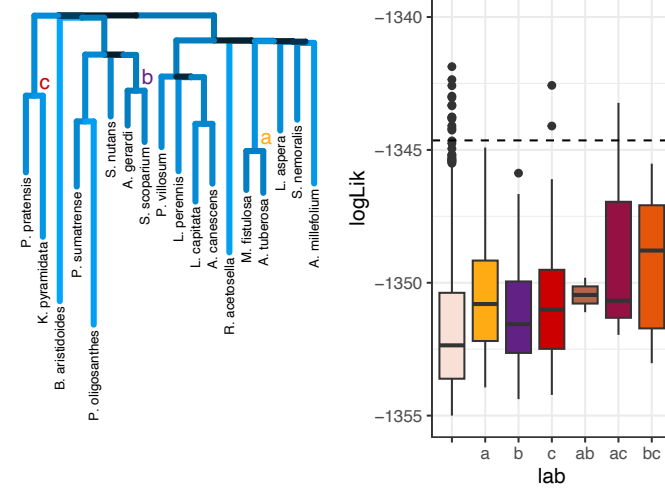


Figure 40: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

Biodiversity II (2017)

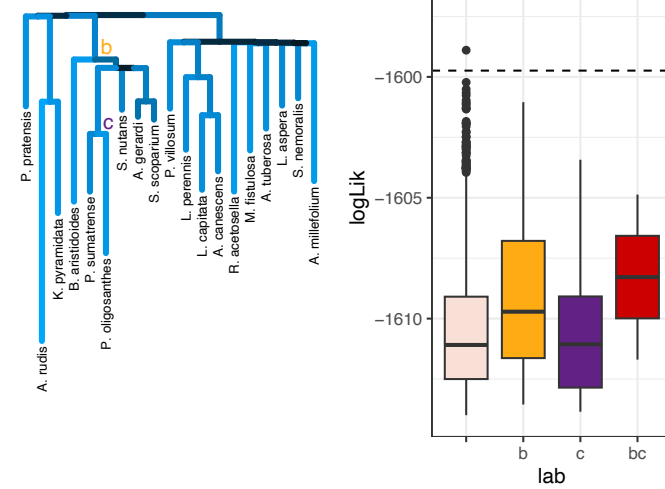


Figure 41: Resulting trees for the Biodiversity II experiments in Cedar Creek, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

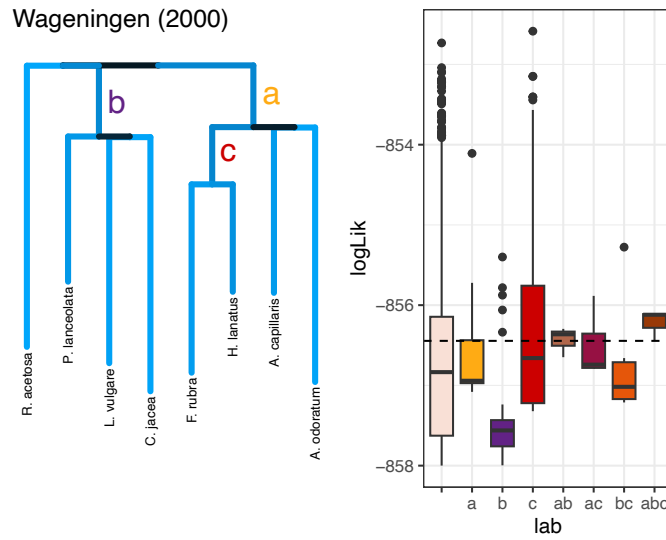


Figure 42: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

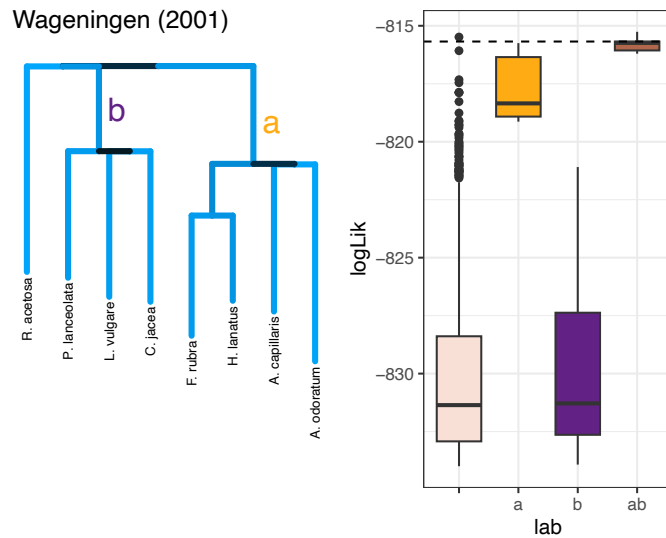


Figure 43: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

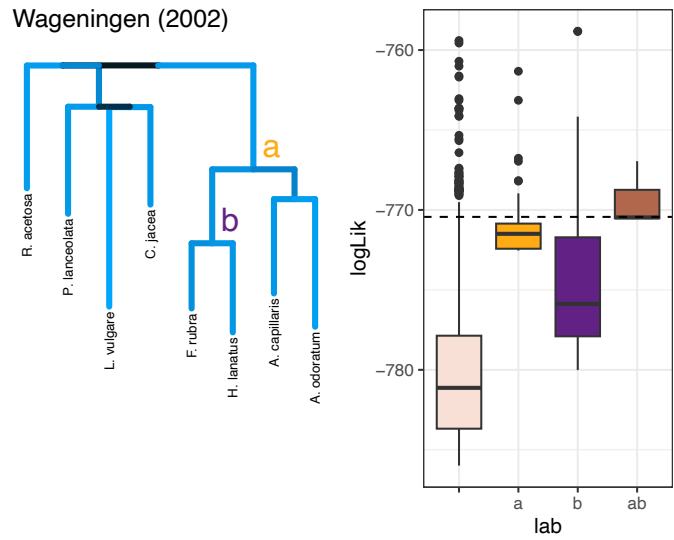


Figure 44: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

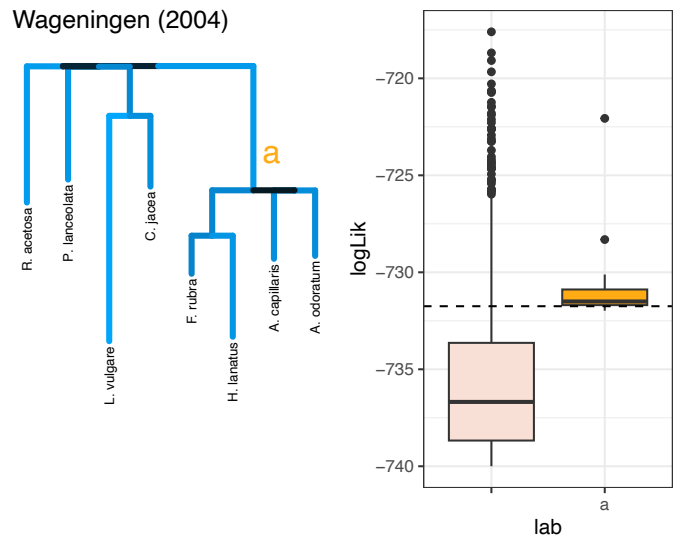


Figure 45: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

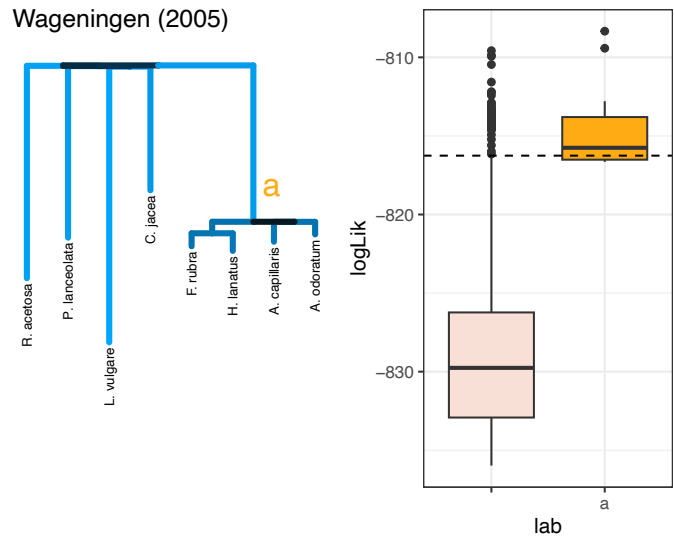


Figure 46: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

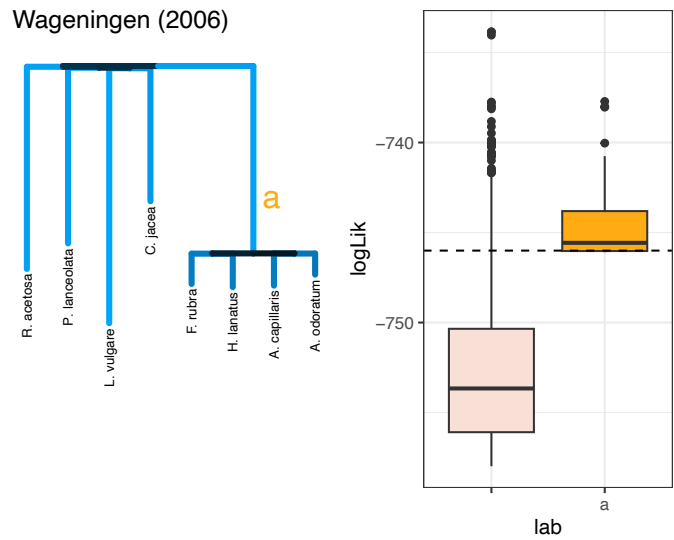


Figure 47: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

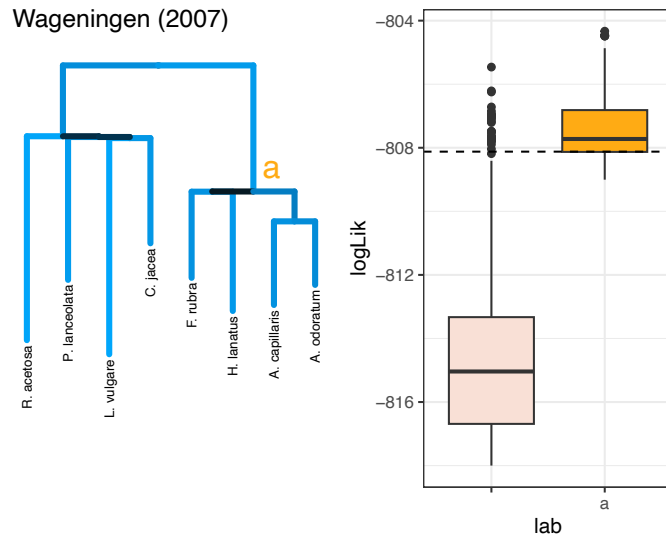


Figure 48: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

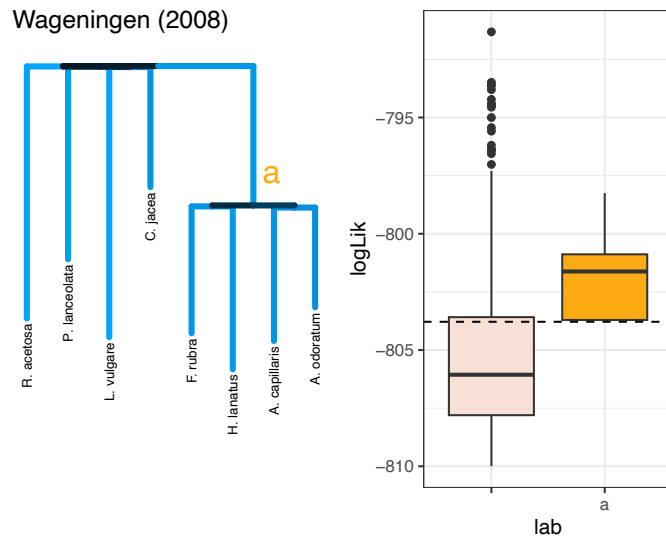
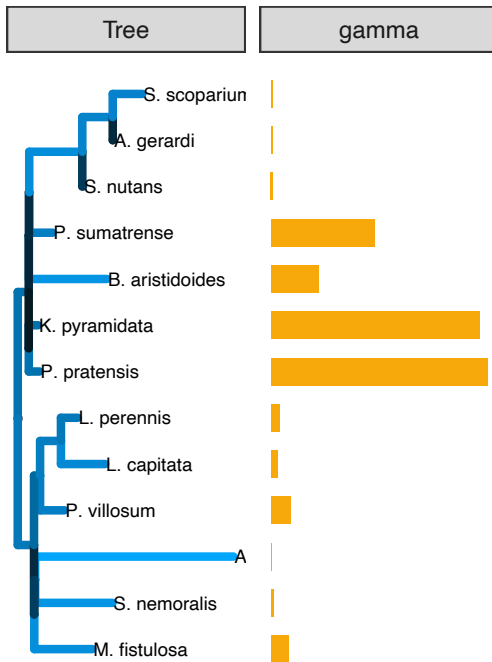
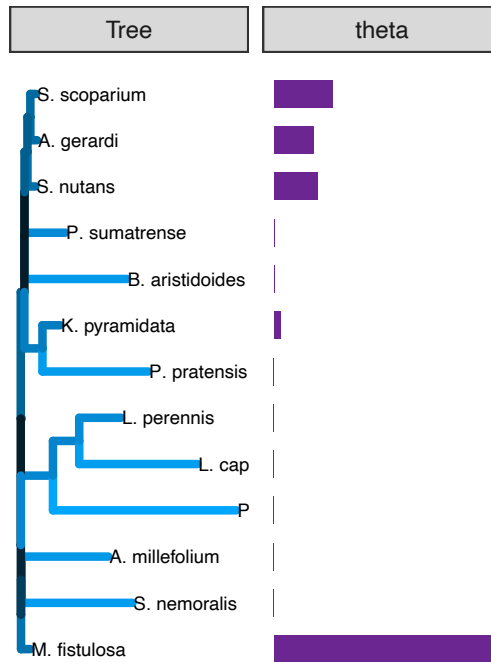


Figure 49: Resulting trees for the Wageningen experiments, fit for phylogenetic tree from model 1 and boxplots of likelihoods for randomizations that kept the selected clades highlighted in the trees. Dashed line represents likelihood of the original tree

bioll\_2001-6\_2 model 2



bioll\_2001-6\_2 model 3



bioll\_2001-6\_2 model 4

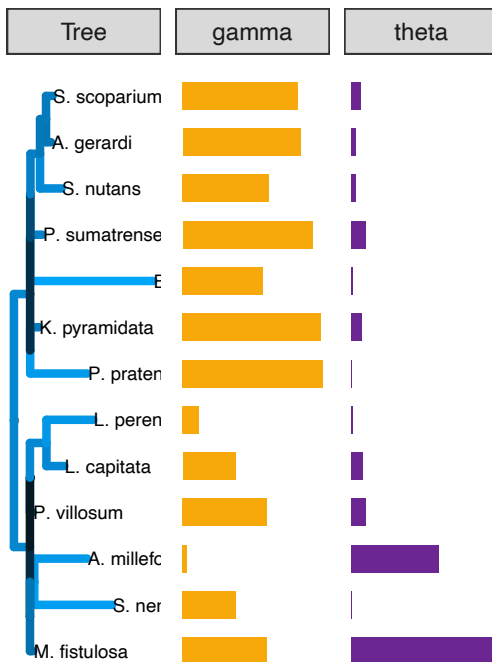
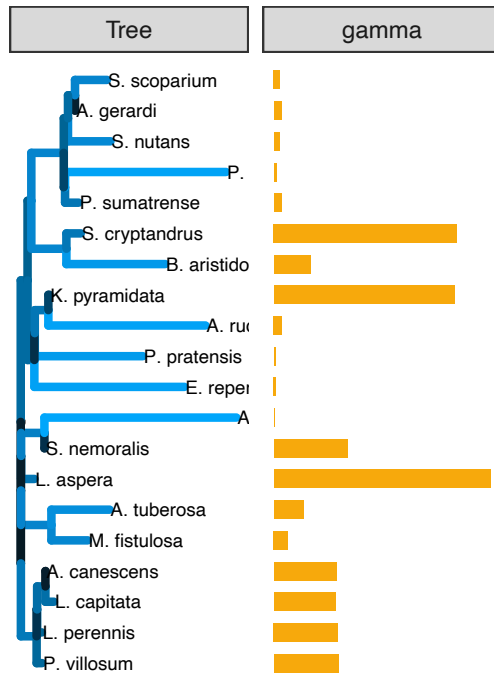
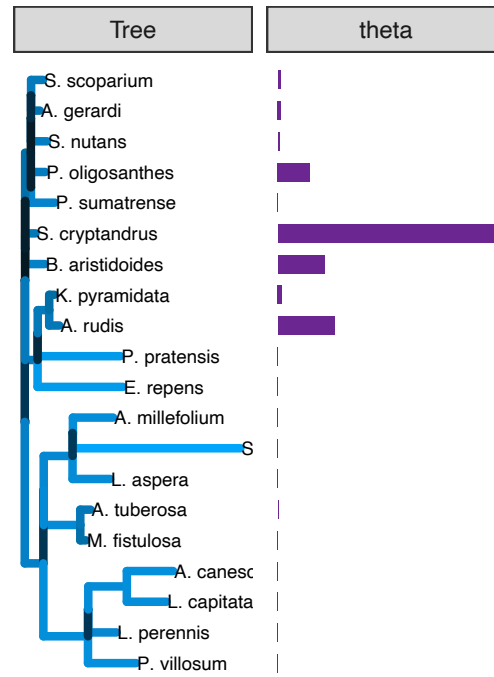


Figure 50: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioII\_2006-7\_2 model 2



bioII\_2006-7\_2 model 3



bioII\_2006-7\_2 model 4

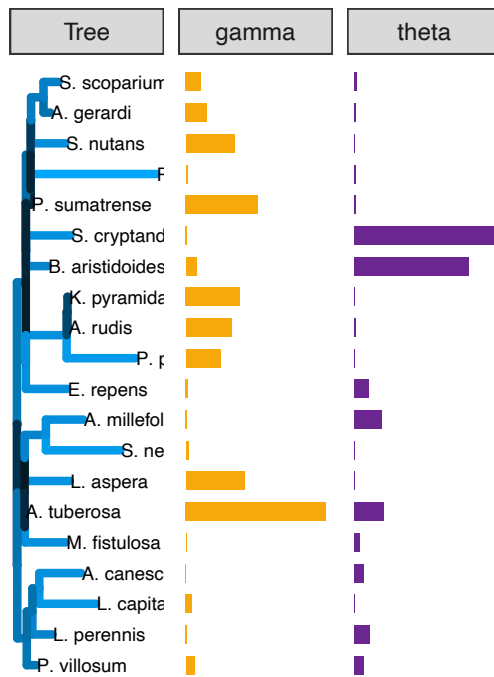
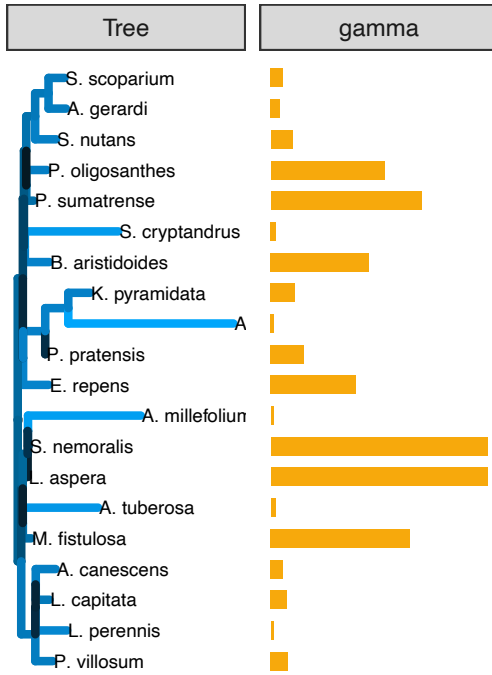
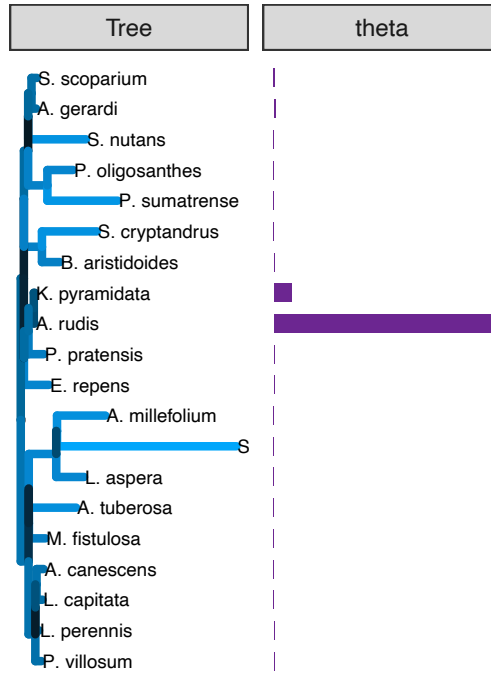


Figure 51: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2007-8\_2 model 2



bioll\_2007-8\_2 model 3



bioll\_2007-8\_2 model 4

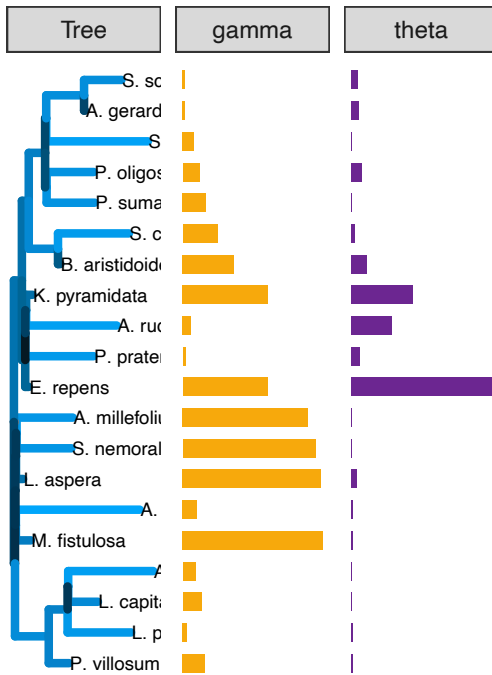
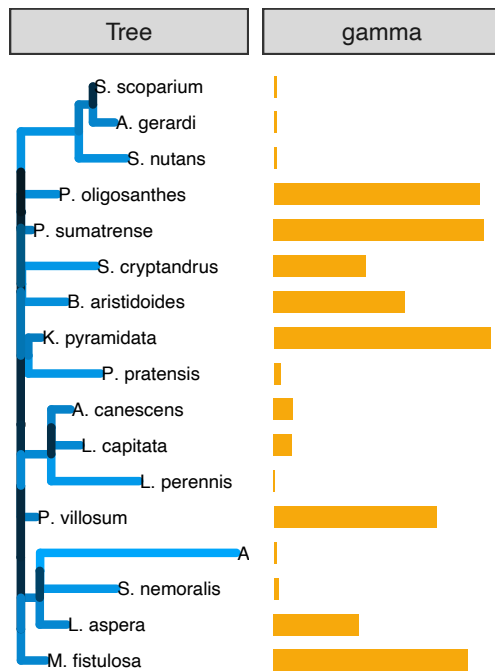
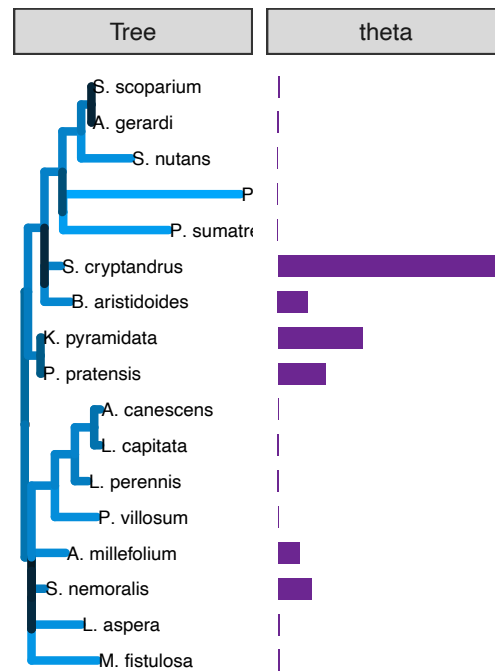


Figure 52: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioII\_2008-7\_2 model 2



bioII\_2008-7\_2 model 3



bioII\_2008-7\_2 model 4

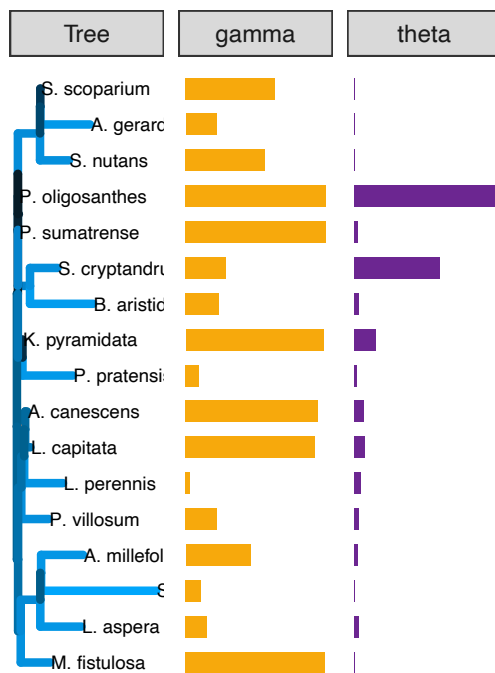
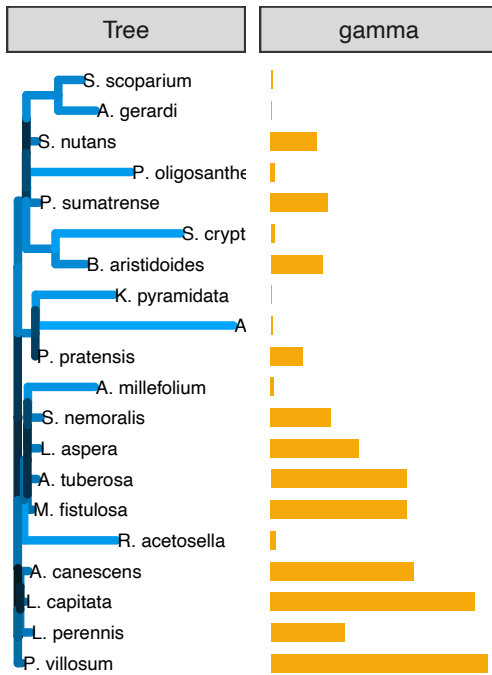
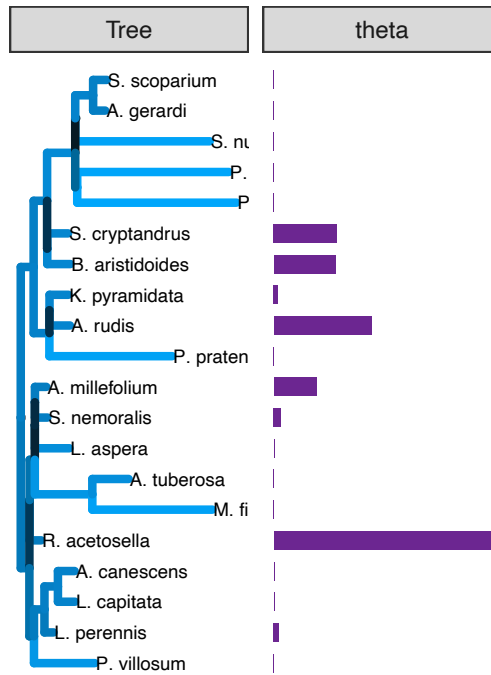


Figure 53: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2011-8\_2 model 2



bioll\_2011-8\_2 model 3



bioll\_2011-8\_2 model 4

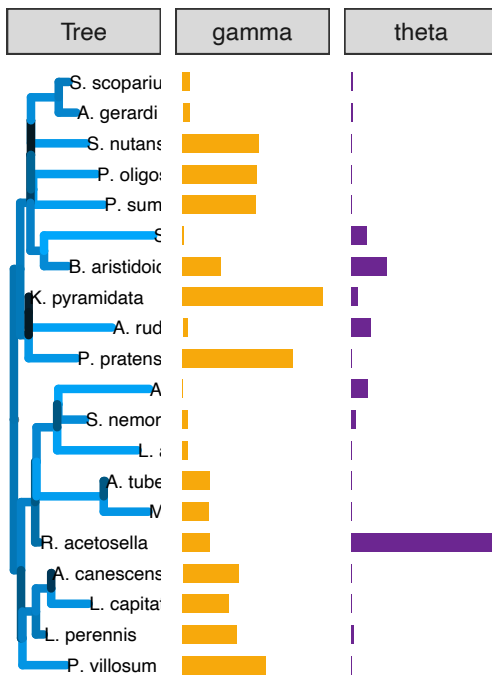
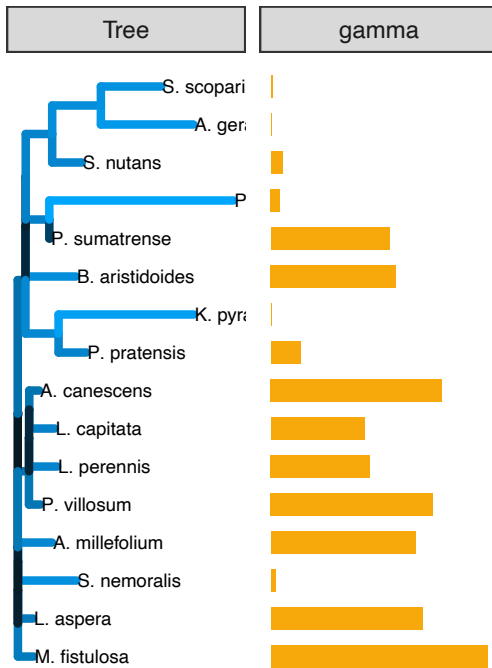
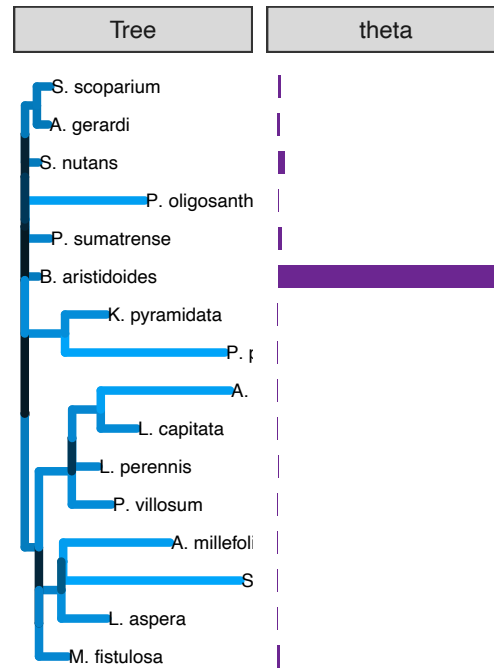


Figure 54: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2012-7\_2 model 2



bioll\_2012-7\_2 model 3



bioll\_2012-7\_2 model 4

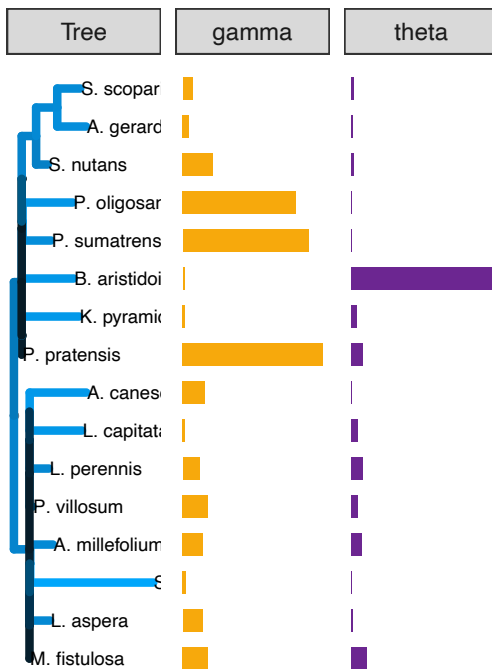
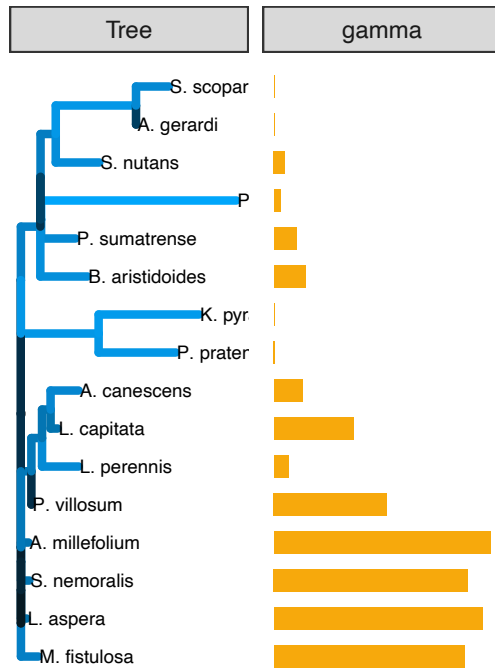
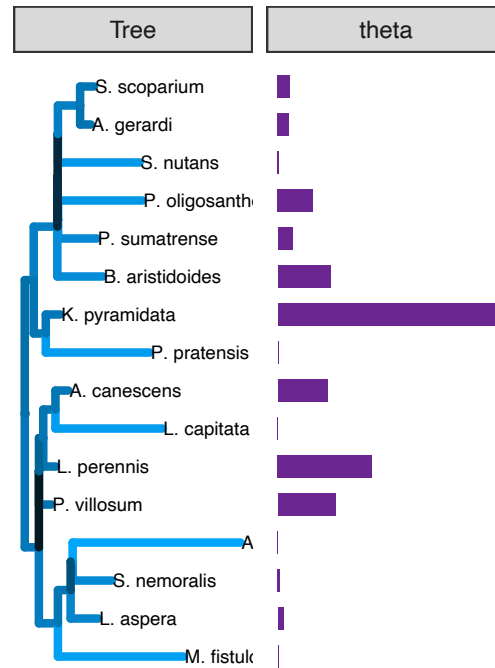


Figure 55: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioll refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2014-8\_2 model 2



bioll\_2014-8\_2 model 3



bioll\_2014-8\_2 model 4

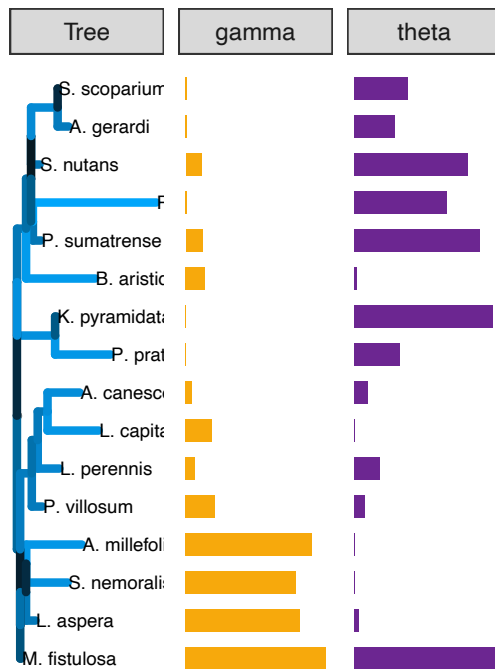
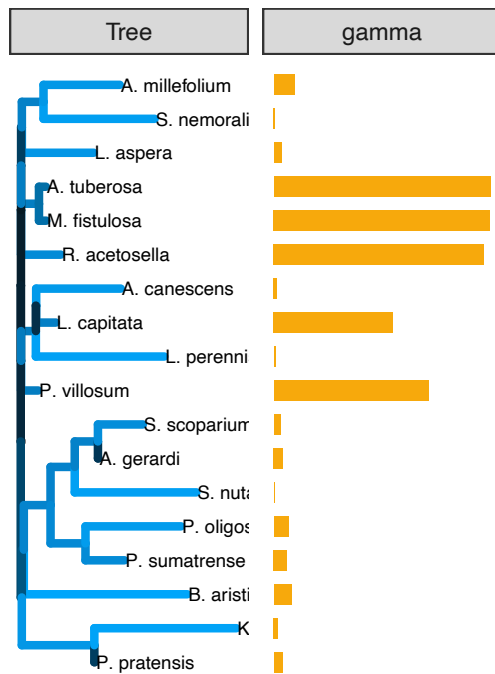
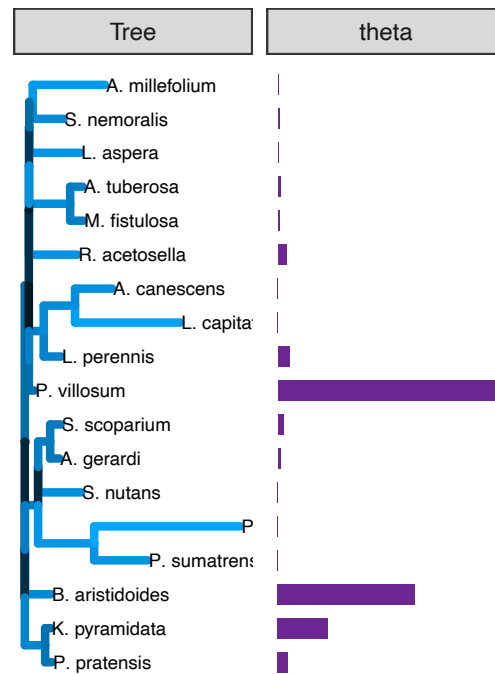


Figure 56: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2015-8\_2 model 2



bioll\_2015-8\_2 model 3



bioll\_2015-8\_2 model 4

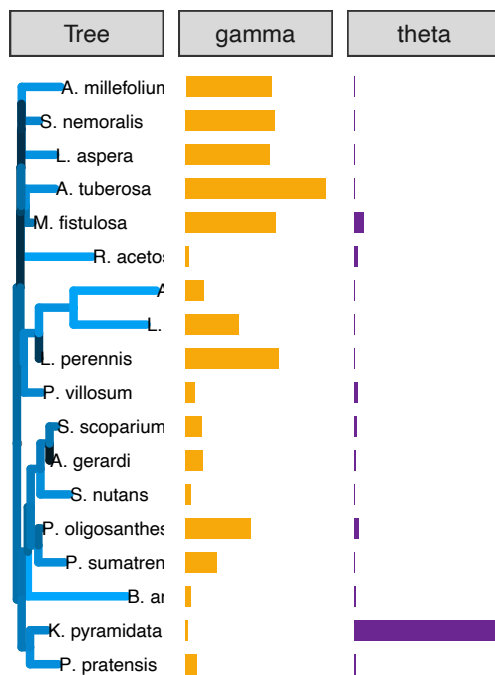
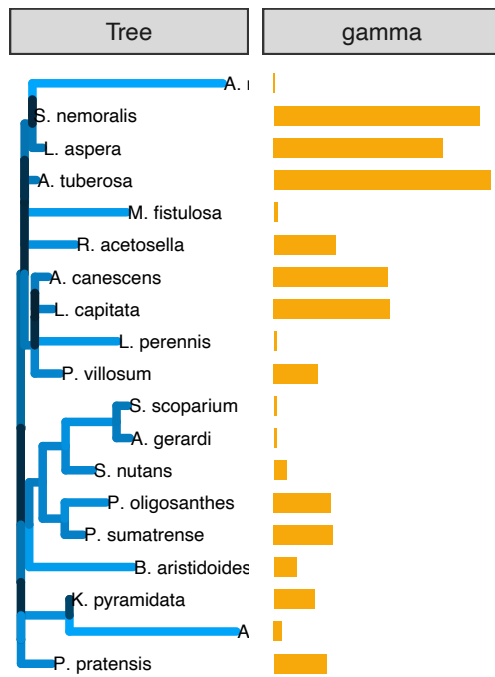
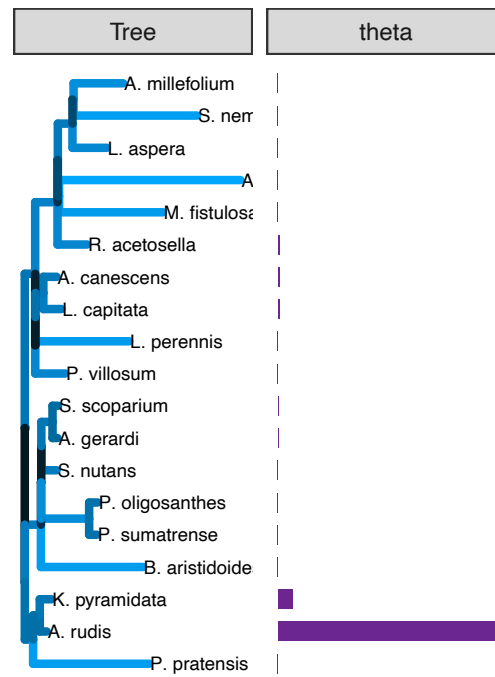


Figure 57: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

bioll\_2017-7\_2 model 2



bioll\_2017-7\_2 model 3



bioll\_2017-7\_2 model 4

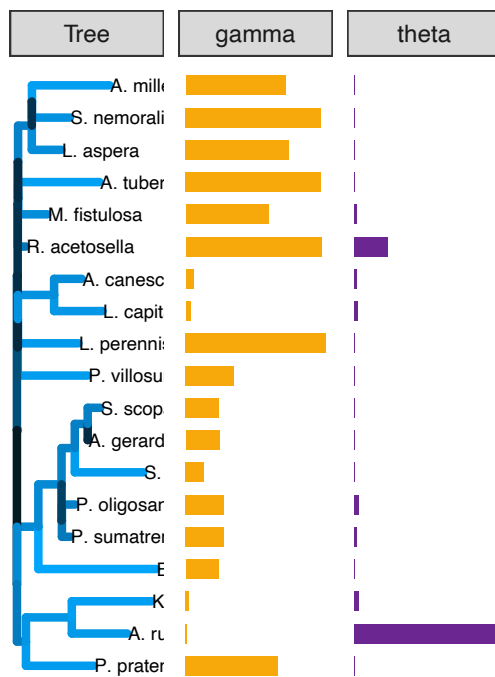
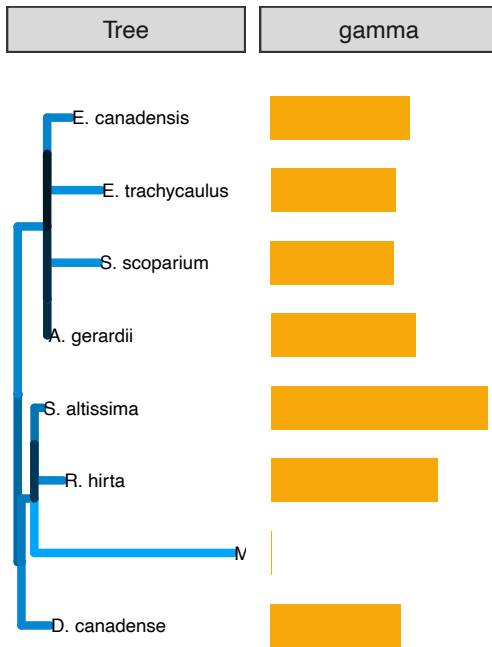
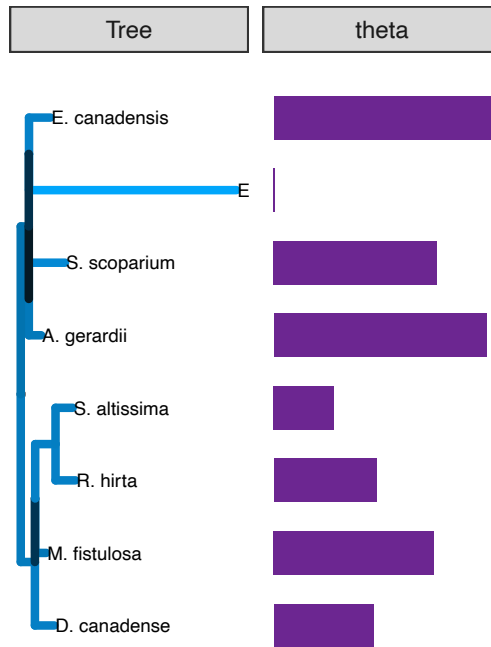


Figure 58: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioll refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

### cadotte\_2013\_2 model 2



### cadotte\_2013\_2 model 3



### cadotte\_2013\_2 model 4

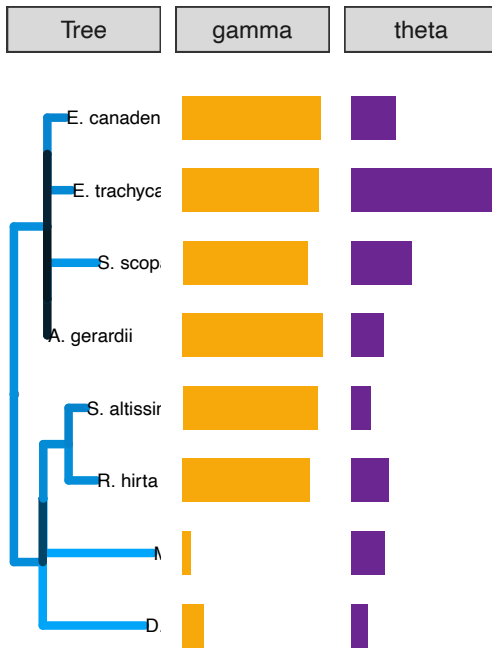
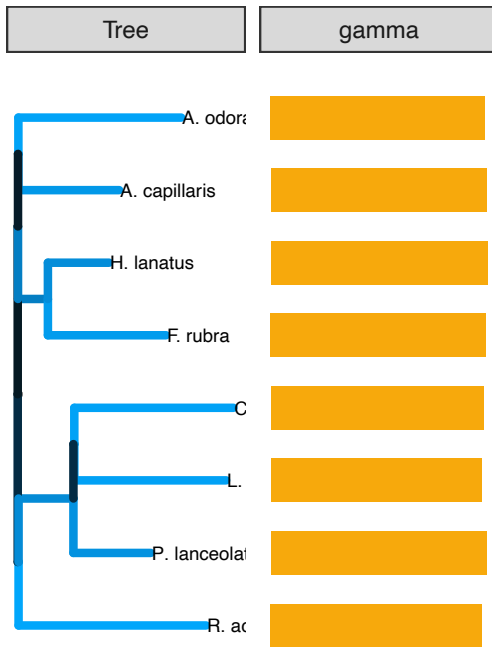
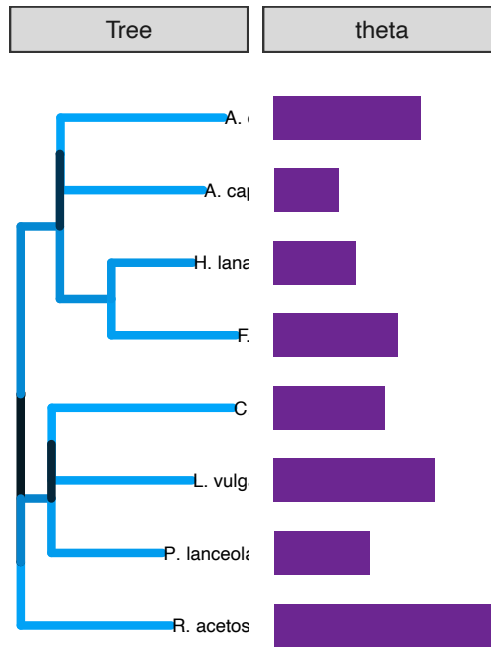


Figure 59: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_1\_2 model 2



vr\_1\_2 model 3



vr\_1\_2 model 4

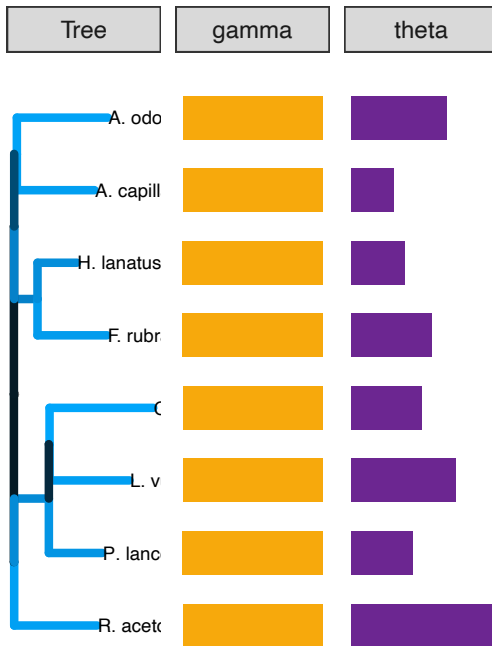
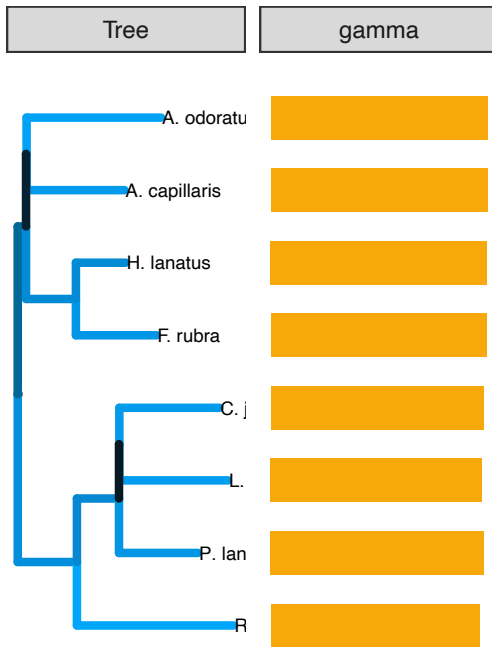
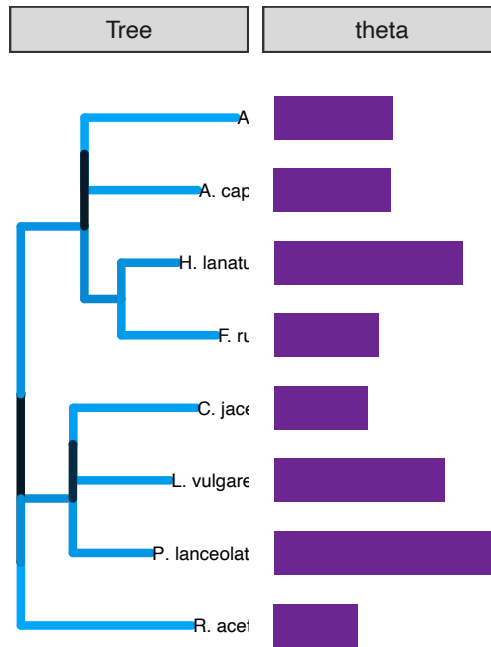


Figure 60: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_2\_2 model 2



vr\_2\_2 model 3



vr\_2\_2 model 4

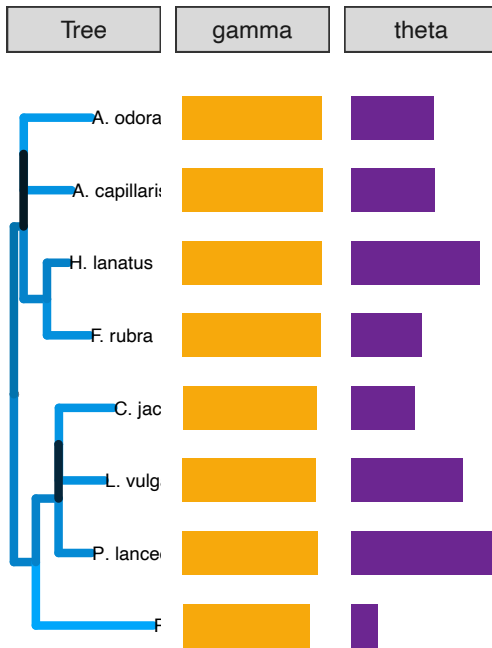
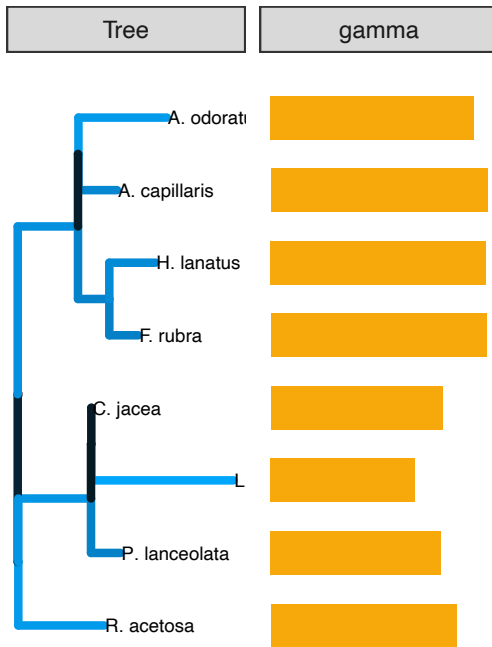
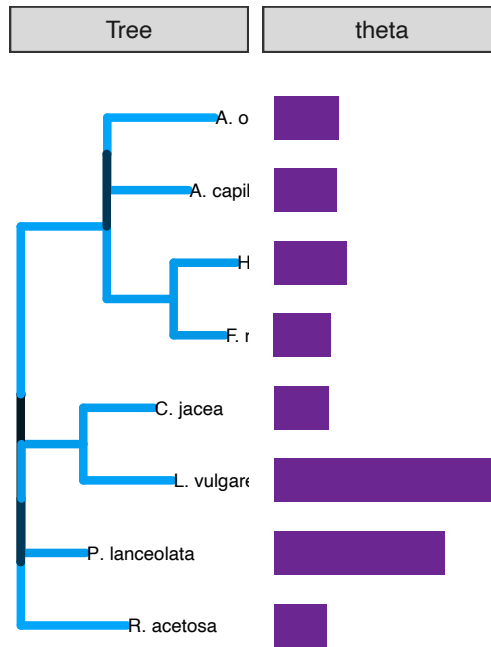


Figure 61: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_3\_2 model 2



vr\_3\_2 model 3



vr\_3\_2 model 4

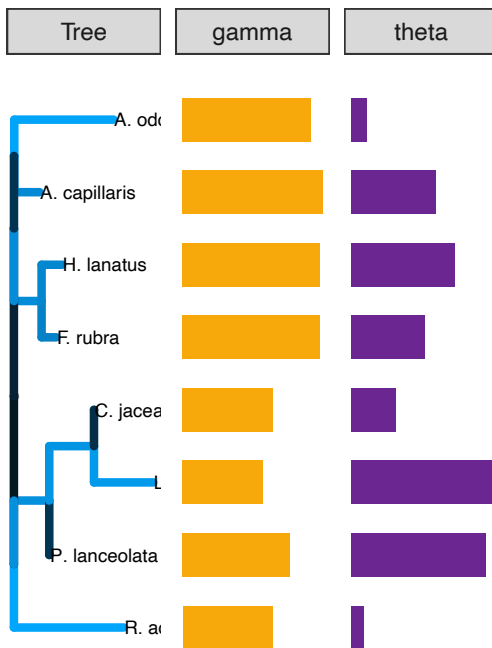
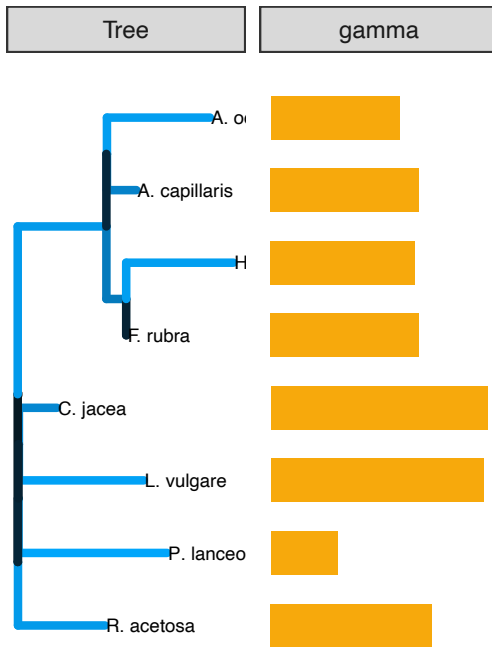
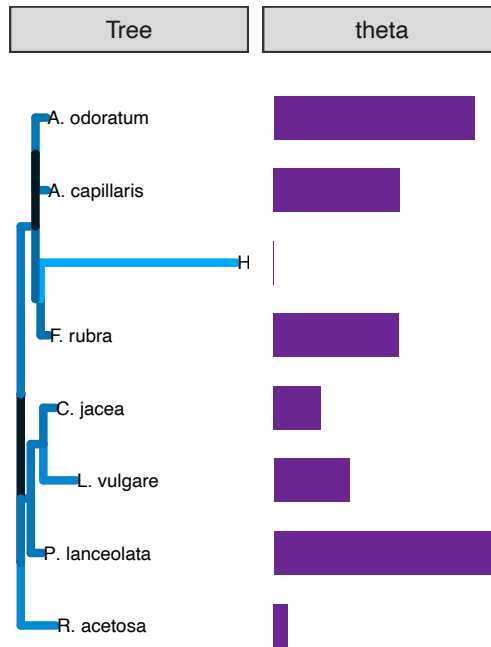


Figure 62: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_4\_2 model 2



vr\_4\_2 model 3



vr\_4\_2 model 4

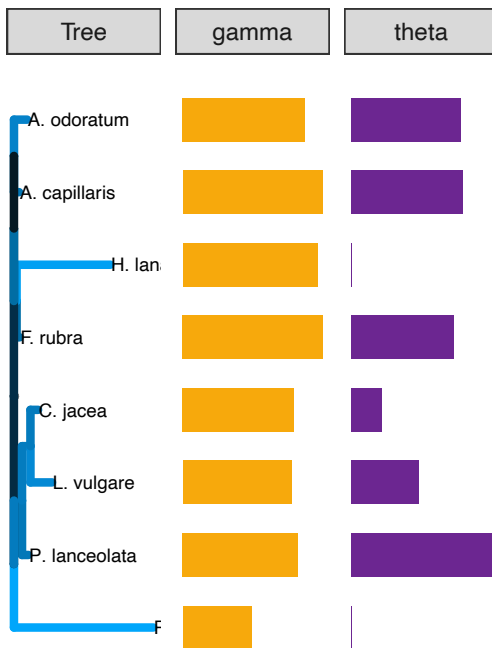
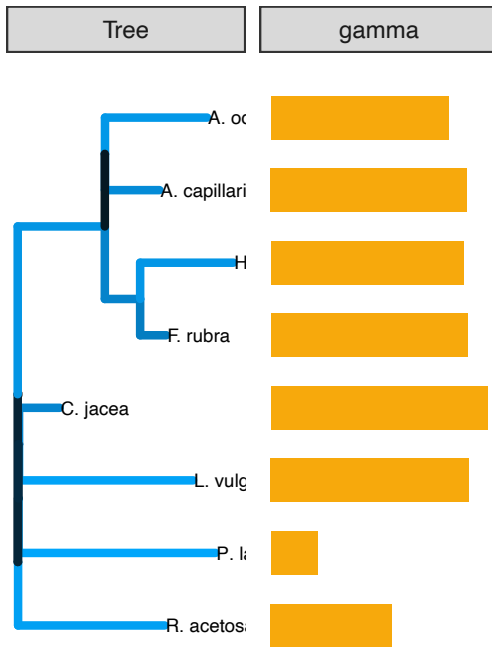
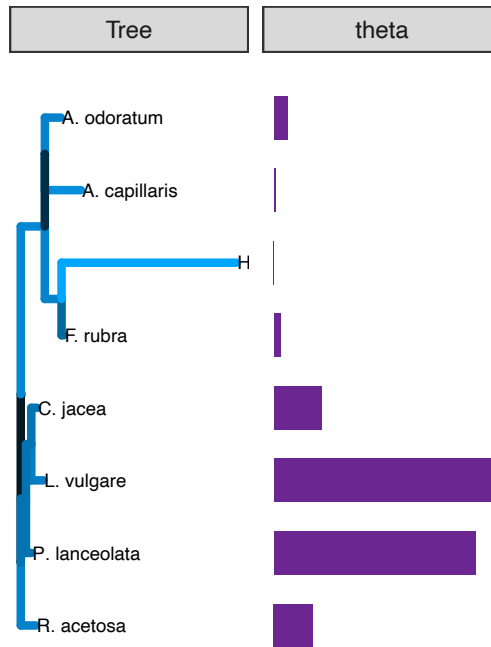


Figure 63: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_5\_2 model 2



vr\_5\_2 model 3



vr\_5\_2 model 4

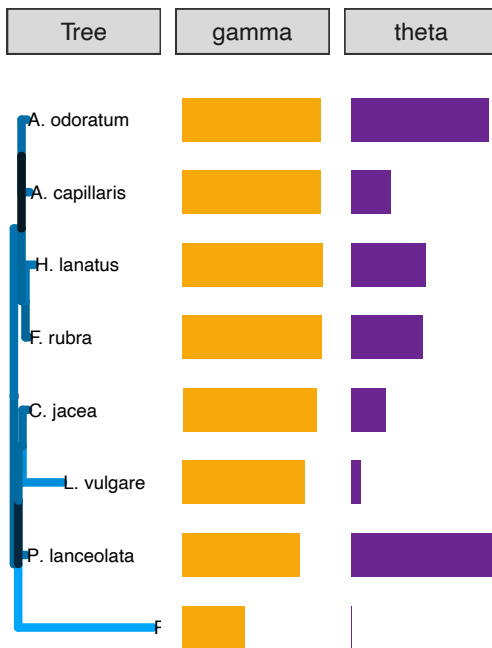
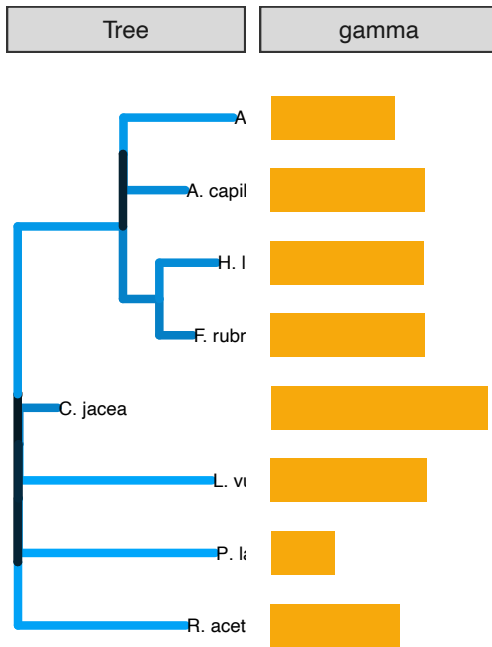
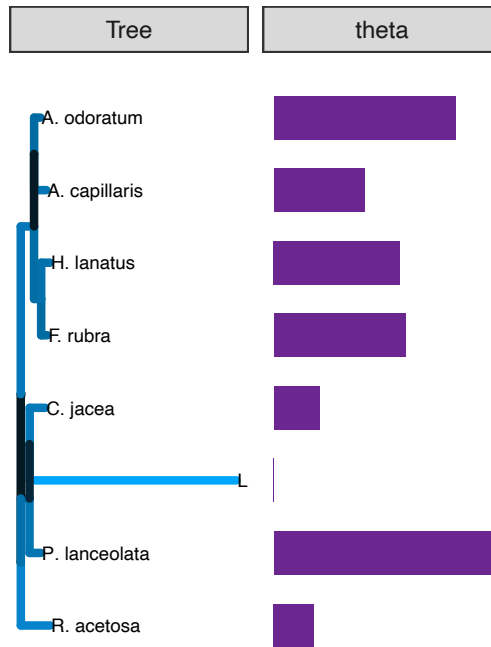


Figure 64: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_6\_2 model 2



vr\_6\_2 model 3



vr\_6\_2 model 4

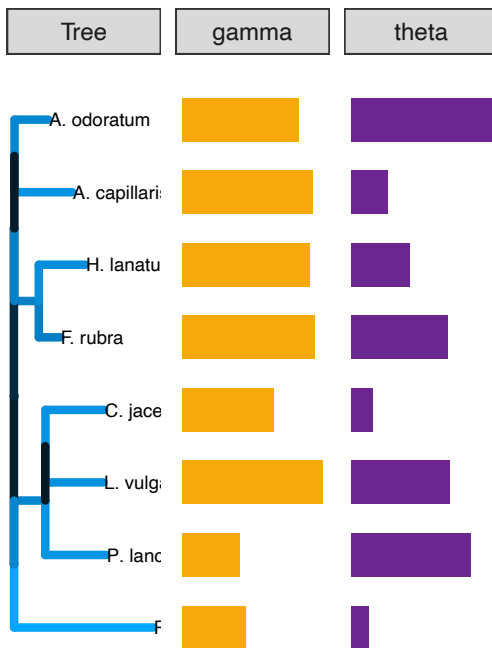
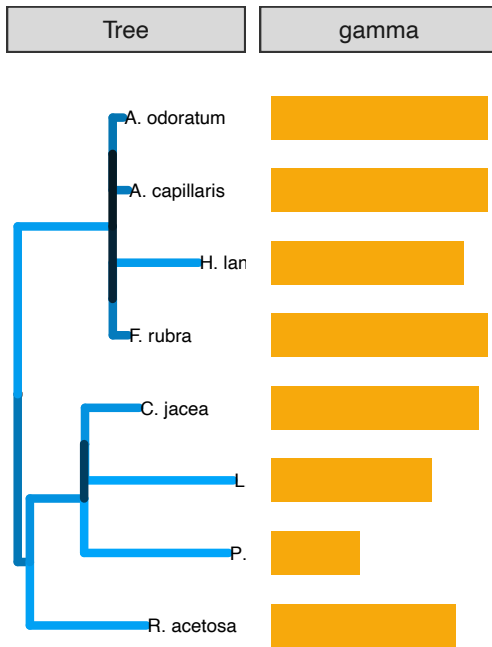
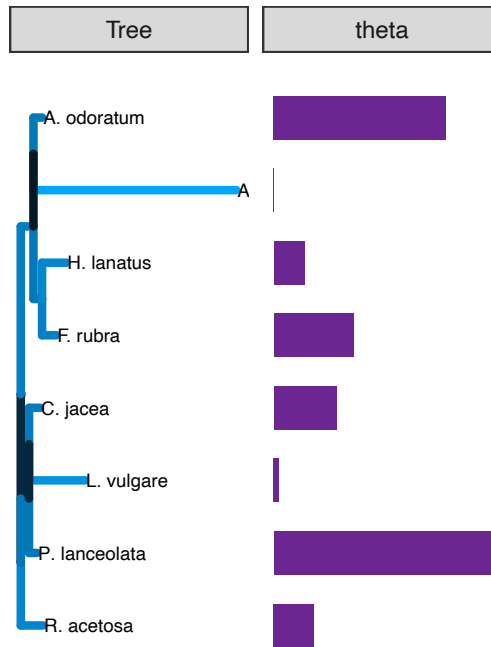


Figure 65: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_7\_2 model 2



vr\_7\_2 model 3



vr\_7\_2 model 4

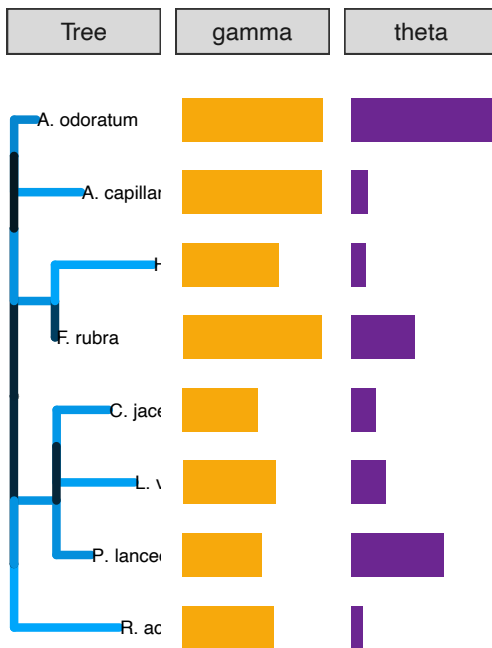
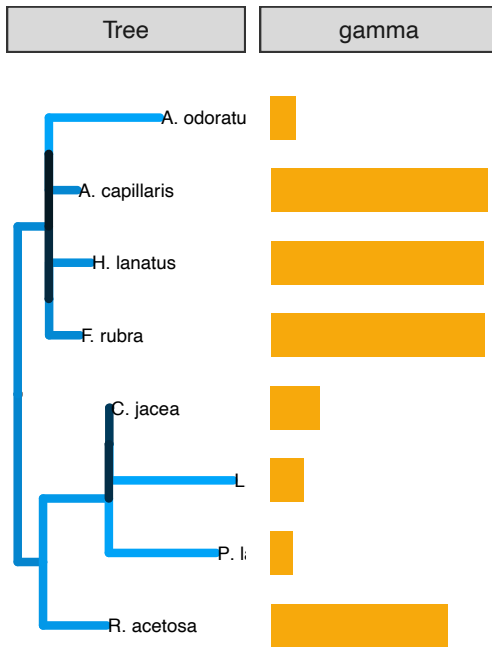
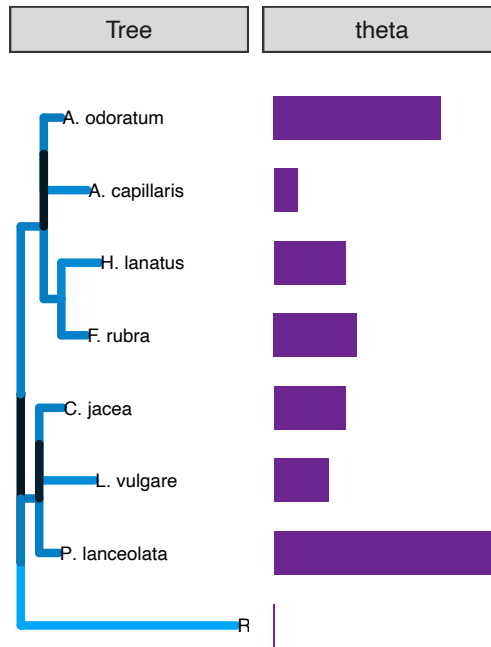


Figure 66: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_8\_2 model 2



vr\_8\_2 model 3



vr\_8\_2 model 4

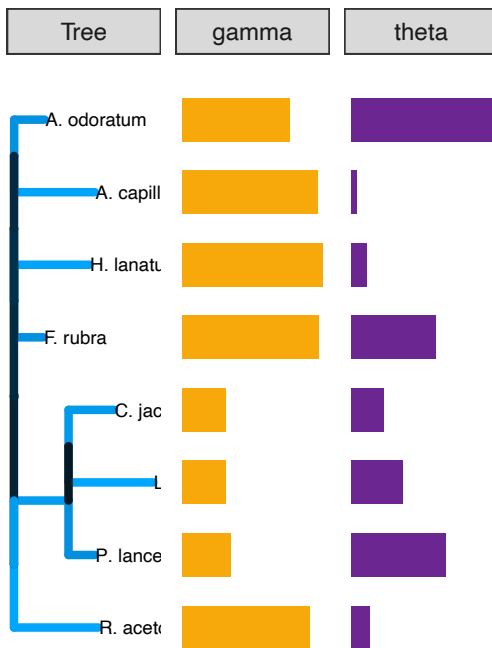
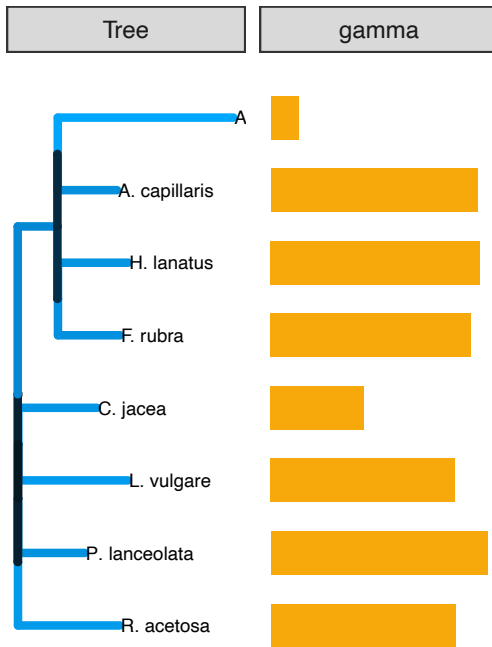
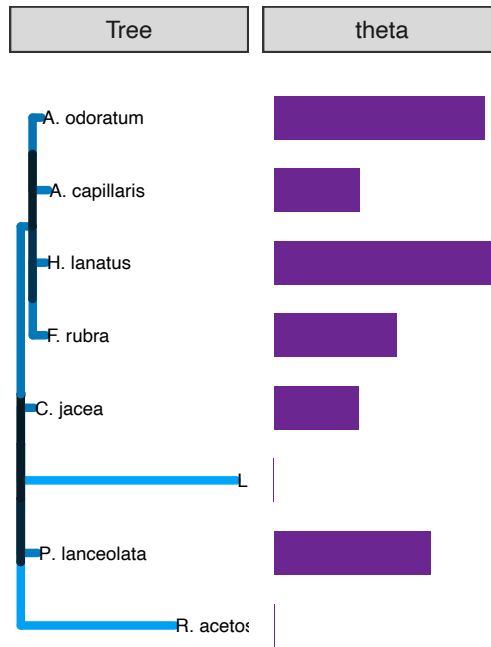


Figure 67: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

vr\_9\_2 model 2



vr\_9\_2 model 3



vr\_9\_2 model 4

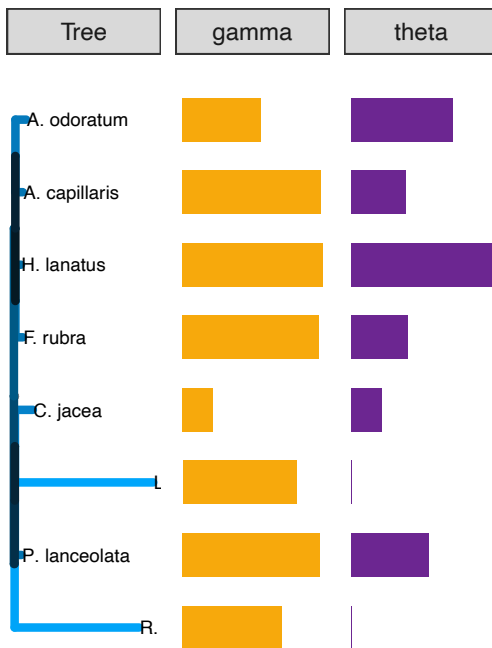


Figure 68: Fit for the phylogenetic tree and associated parameter vectors (Gamma and Theta) for models 2-4. The length and color of the branches correspond to increased strength in competition between the species in the clade and the size of the vector corresponds to the fitted value for the corresponding species in the tree. bioII refers to the Biodiversity II experiment (Tilman et al. (2001)); cadotte is from Cadotte (2013); and vr refers to the Wageningen experiment from Van Ruijven and Berendse (2010).

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